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PREDICTIONS OF PROJECTILE PENETRATION PHENOMENA  
AND COMPARISON WITH EXPERIMENTS IN A SOIL MEDIUM

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Prepared by Sandia Laboratories, Albuquerque, New Mexico 87115  
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COMPARISON WITH EXPERIMENTS IN A SOIL MEDIUM\*

Final Report

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ABSTRACT

Results of calculations are presented to predict effects of earth penetration experiments conducted in mid-July 1974 at the Watching Hill site of the Defense Research Establishment in Alberta, Canada. Calculations were performed with the TOODY Lagrangian code for both a rigid and deformable projectile. Soil cap models describing four layers of the glacial silt target medium were employed in the calculations. All calculations are for a projectile 0.1651 m in diameter (6.5 inches), of mass

181.44 kg (400 pounds) with tangent ogive nose shape impacting the earth target at a velocity of 152.4 m/s (500 ft/sec). A zero friction boundary condition is employed at the projectile-soil interface. Stress, strain, and velocity distributions, produced in the medium by the penetrating projectile, are computed. Axial retarding forces exerted by the medium on the projectile and normal stress distributions on the projectile surface are also calculated. Comparisons of predictions with experimental measurements of rigid body projectile deceleration and soil stress histories indicate that computer simulations can provide a detailed and accurate description of soil response during penetration by projectiles.

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## SECTION I

### INTRODUCTION

The immediate purpose of calculations presented here is to provide predictions of effects associated with earth penetration experiments conducted at the Watching Hill site in Alberta, Canada, in mid-July 1974. In particular, predictions of deceleration history and medium stress histories at specific locations were desired for comparison with experimental measurements of these quantities. Such comparisons permit evaluation of current theoretical prediction capabilities and, in addition, provide insights into the primary mechanisms and relevant phenomena governing projectile penetration into earth media. Ultimate objectives of the computational effort are (1) to develop methods for confidently predicting loads on earth penetrating projectiles in order to facilitate rational design of penetrators with a minimum reliance on empirical testing, (2) to develop an understanding of the detailed mechanisms involved in earth penetration to the extent that the empirical soil factor of Young's penetration equations<sup>1,2</sup> may be correlated with appropriate target medium properties, and (3) to establish the degree of complexity in description of target medium properties necessary for accurate calculation of projectile decelerations, loads, and depths of penetration.

Two finite difference code calculations were made to estimate results of the Watching Hill experiments. The TOODY Lagrangian code<sup>3,4</sup> was employed to predict penetration performance of both a rigid and a deformable projectile. In both cases, the target medium properties were described by using identical soil cap models. With the projectile considered as a

rigid body, the finite difference code is capable of more efficient operations than when the projectile is taken to be a deformable body. Rigid body calculations then permit examination of penetration to deeper projectile depths in reasonable amounts of computer time. To verify the validity of the rigid body assumption, a deformable body calculation was performed until the nose of the projectile was fully embedded. From the deformable body calculation, stress and strain histories and distributions within the projectile are obtained.

Projectile penetration experiments<sup>5</sup> at the Watching Hill site included one for direct comparison with calculations in which the projectile impacted the target medium at a velocity of 152.4 m/s (500 ft/sec). The projectile,<sup>6</sup> fabricated from D6AC steel, had a diameter of 0.165 m (6.5 inches), a length of 1.524 m (60 inches), and a mass of 181.44 kg (400 pounds). Nose shape was 9.25 CRH tangent ogive with a slight blunting of the tip. Accelerometers mounted within the projectile provided deceleration histories during penetration. Integrations of deceleration histories result in projectile velocity and position information including depth of penetration. Projectile deceleration and penetration depth were felt to be insufficient information for critically evaluating results of computer code calculations, particularly the material property models employed in the codes.<sup>7</sup> A much more severe test of target medium constitutive models is provided by measurements of the medium response. For these reasons, lithium niobate pressure or stress transducers<sup>8,9</sup> were incorporated into the Watching Hill experiments. Six stress-history transducers, four of which were to measure mean stress and two radial stress, were emplaced in the target medium in two vertical holes near the vicinity of the projectile penetration locations. Positions of the stress

transducers are indicated in Figure I-1. At the position (range/depth relative to the projectile impact point) of 0.45 m/1.8 m, a mean stress transducer is located. A mean stress and a radial stress transducer are located at 0.45 m/3.6 m, and at 0.45 m/5.4 m, two mean stress gauges are placed. A single radial stress gauge is located at 0.9 m/3.6 m. Gauges shown in Figure I-1 at a range of 1.5 m were used for another projectile penetration experiment but are physically the same set of gauges shown at a range of 0.45 m for the experiment of primary interest. Measurements of target response during projectile penetration apparently have never before been made; the successful recording of medium stress histories<sup>10</sup> during the Watching Hill penetration experiments has provided valuable information for more direct verification of computer code calculations.

Output desired from computer code calculations has been specified in detail<sup>11</sup> and is briefly summarized in Figures I-1 and I-2 for the rigid body calculations. Similarly, for the deformable projectile calculations, desired output is indicated in Figures I-3 and I-4.

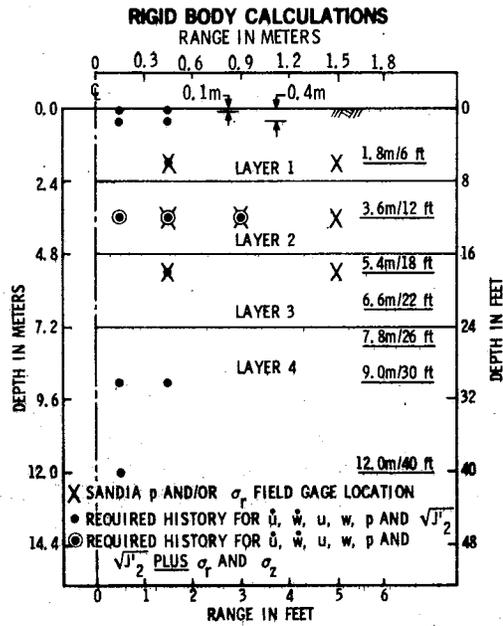


Figure I-1. Rigid Body Calculation. Medium field points for history displays of displacements, velocities and stresses.

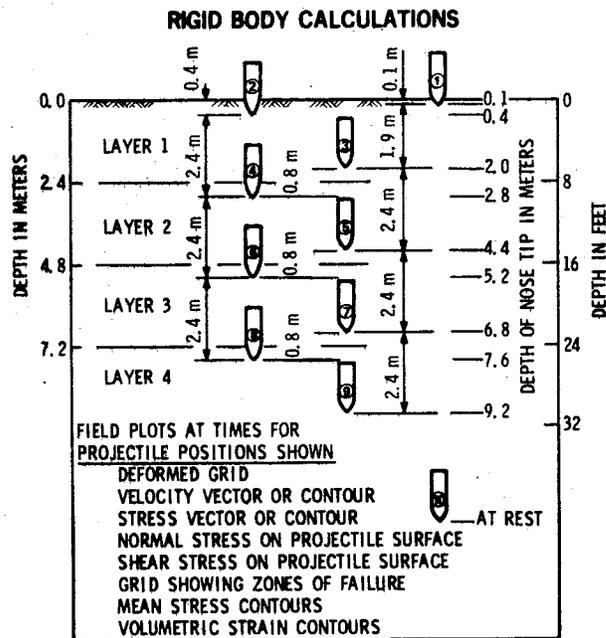
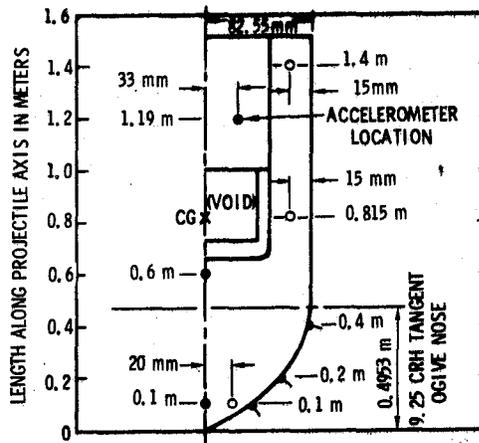


Figure I-2. Rigid Body Calculation. Projectile positions at which times contour plots are required.

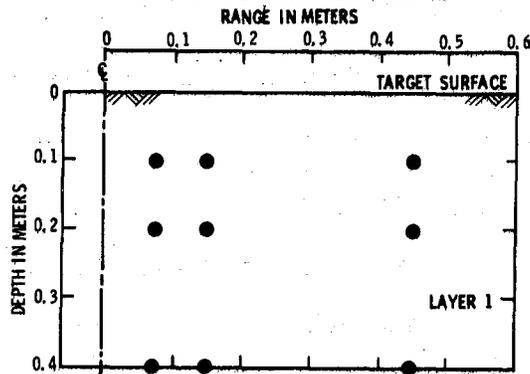
### DEFORMABLE BODY CALCULATION



- REQUIRED HISTORY CALCULATION FOR VERTICAL ACCELERATION, VELOCITY AND DISPLACEMENT
- REQUIRED HISTORY CALCULATION FOR  $p$  AND  $\sqrt{J_2}$  (OR  $\sigma_r, \sigma_\theta, \sigma_z, \sigma_{rz}$ )
- ▲ REQUIRED HISTORY CALCULATION FOR NORMAL STRESS AND SHEAR STRESS ON PROJECTILE SURFACE

Figure I-3. Deformable Body Calculation. Positions in projectile at which displacements, velocities, accelerations and stress are displayed.

### DEFORMABLE BODY CALCULATION



- REQUIRED HISTORY FOR  $\dot{u}, \dot{w}, u, w, p$  AND  $\sqrt{J_2}$
- FIELD PLOTS AT PROJECTILE PENETRATION  
 DEPTHS OF 10, 20 AND 40 cm  
 DEFORMED GRID  
 VELOCITY VECTOR OR CONTOUR  
 STRESS VECTOR OR CONTOUR  
 MEAN STRESS CONTOUR  
 VOLUMETRIC STRAIN CONTOUR  
 GRID SHOWING ZONES OF FAILURE

Figure I-4. Deformable Body Calculation. Medium field points for history displays of displacements, velocities and stresses.

## SECTION II

### MATERIAL MODELS FOR TARGET MEDIUM

The Watching Hill Blast Range of the Canadian Defense Research Establishment, on which site the earth penetrator experiments<sup>5</sup> were conducted, is located about 30 miles north of Medicine Hat near Suffield, Alberta. The target medium at Watching Hill consists of a thick succession of glacial tills and lake deposits; the near surface deposit is composed of thin interbedded layers of lacustrine silt, sand, and clay sediments.<sup>12</sup> The medium is porous and contains varying amounts of water, increasing with depth. For purposes of modeling the target medium in computer calculations of projectile penetration, the medium has been represented by four uniform, homogeneous isotropic layers. The three uppermost layers were each taken to be 2.4 m (7.87 feet) thick. The fourth layer, beginning at 7.2 m (23.6 feet), is below the water table. Material properties derived from uniaxial strain and triaxial stress experiments<sup>12</sup> have been specified<sup>13,14</sup> for each of the four layers.

For the calculations of projectile penetration with both a rigid and deformable projectile, a soil cap model is used to describe each of the four layers of the Watching Hill medium. The cap models<sup>15</sup> employ a failure envelope or fixed plastic yield surface represented by a function of the form  $f_1(\tau, p) = 0$  in which  $p$  is the mean stress or pressure and  $\tau$  is the octahedral shear stress (see Figure II-1). Octahedral shear stress is defined by  $\tau = (\sigma'_{ij}\sigma'_{ij}/3)^{\frac{1}{2}}$ , where the deviator stress,  $\sigma'_{ij} = \sigma_{ij} - p\delta_{ij}$ . The "cap" on this surface is given by  $f_2(p, \tau, \epsilon_p) = 0$ , where  $\epsilon_p$  is the plastic volumetric strain. Position of the cap on the failure envel-

is determined by  $\epsilon_p$ , and the cap expands or contracts as  $\epsilon_p$  increases or decreases. Plastic strain increments are determined from  $f_1$  and  $f_2$  by means of the associated flow rule. Figure II-2 illustrates an example

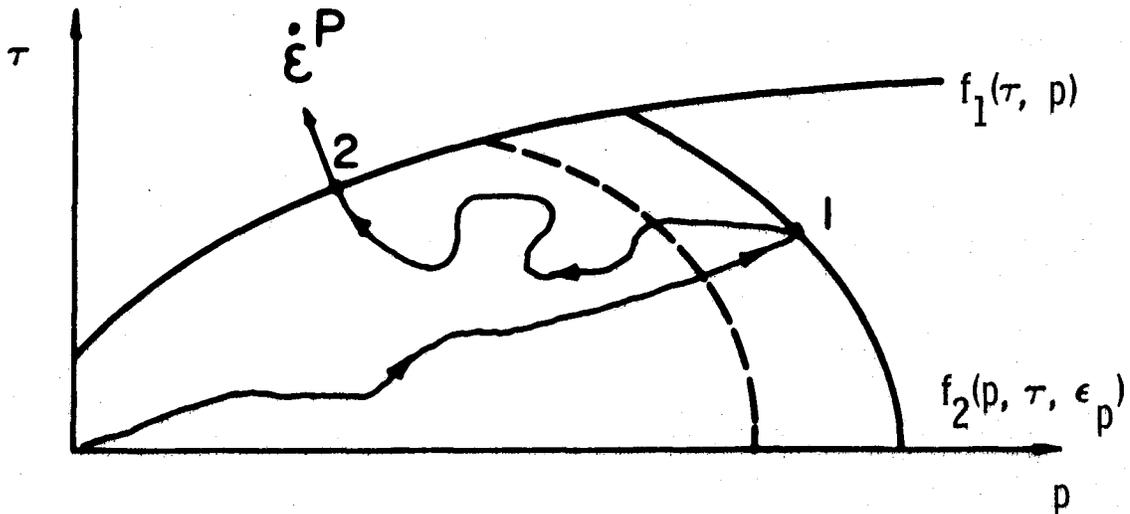


Figure II-1. Cap Model Illustrating Failure Envelope, Cap, a Stress Path, and Cap Contraction

of the hysteresis produced by a cap model description in a series of load-unload cycles of a uniaxial strain test and the corresponding path in  $\tau - p$  space. Information supplied<sup>12</sup> for the Watching Hill target medium consisted of a single uniaxial strain, load-unload path and a failure envelope considered to be representative of each of four layers of the medium. From the data available for each of the idealized four layers, parameters were determined for the functions  $f_1$  and  $f_2$ . For Layers 1, 2, and 3, the failure envelope is given by

$$\tau = A - C \exp(-Bp)$$

and for Layer 4 by

$$\tau = A[1 - 3p/B]^2 + C, p < B/3$$

$$\tau = A + C, \quad p \geq B/3$$

where  $p$  is pressure. The yield surface ellipse for Layers 1, 2 and 3 is described by

$$\tau = [(X - L)^2 - (\sqrt{3}p - L)^2]^{1/2}/R,$$

where  $X$  represents the intersection of the cap with the  $p$  axis and is given by

$$X = -[\ln(1 - \epsilon_p/w)]/D$$

$L$  represents the value of  $p$  at which the cap has a horizontal tangent and is given by

$$L(\epsilon_p) = \begin{cases} l & \text{for } l \geq 0 \\ 0 & \text{for } l < 0 \end{cases}$$

where  $l$  is the solution of the transcendental equation

$$l + R\{A + C \exp(-Bl/\sqrt{3})\} = X(\epsilon_p)$$

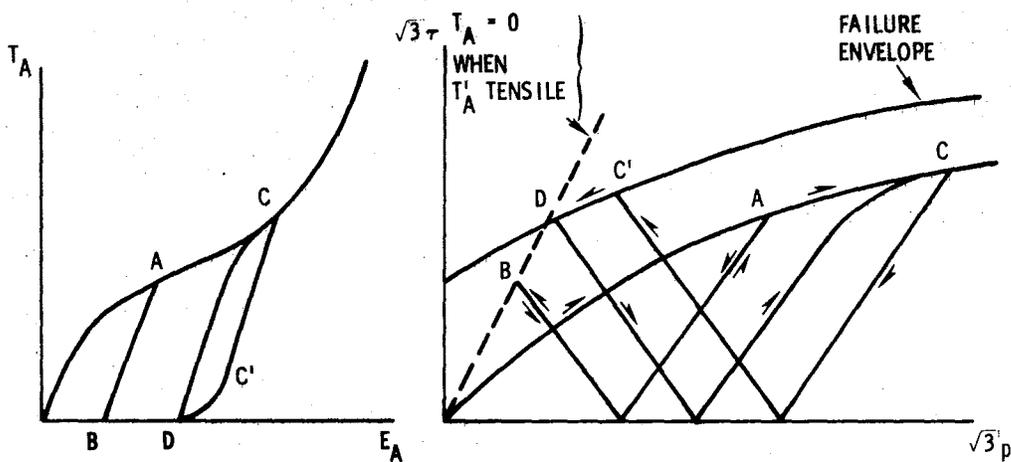


Figure II-2. Loading and Unloading Cycles for Cap Model Material in Stress-Strain and Shear Stress-Pressure Space

For Layer 4, the yield surface is taken as

$$\tau = X/\sqrt{6} - p/\sqrt{2} .$$

Unloading bulk moduli are given by

$$K = B_0 \{ 1 - B_1 \exp(-B_2 p) \}$$

for Layers 1, 2, and 3, and by

$$K = \text{Min} \{ B_0 \exp(B_2 p / B_1); B_0 \exp(B_2 / \sqrt{3}) \}$$

for Layer 4. The shear moduli are

$$\frac{3(1 - 2\nu)}{2(1 + \nu)} \frac{\{ 1 + S_1 \exp(-S_2 p) \}}{(1 + S_1)} K ,$$

in which  $\nu$  is Poisson's ratio. Constants for the various expressions are listed in Table II-1. Figures II-3 through II-6 compare data obtained from the cap models (which are used in code calculations of projectile penetration) with laboratory data from uniaxial strain and triaxial stress experiments. Figures II-7 through II-10 show data for uniaxial strain paths in  $\tau - p$  space and corresponding cap model results. The cap model for Layer 4 fits the data well; however, for Layers 1, 2, and 3, less satisfactory agreement between model predictions and experiment is obtained with the model response being less stiff in shear than indicated by data. This suggests the need, in matching static laboratory data, for a more elaborate model than the 12-parameter model used. One such model has been suggested<sup>16</sup> in which the strain hardening cap is described by an ellipse of variable eccentricity. Cap model formulations with 29 parameters available for fitting data have been described<sup>17,18</sup>; these formu-

TABLE II-1

Cap Model Constants for the Four Layers of the Watching Hill Medium

| <u>Constant</u> | <u>Units</u>         | <u>Layer 1</u> | <u>Layer 2</u> | <u>Layer 3</u> | <u>Layer 4</u>         |
|-----------------|----------------------|----------------|----------------|----------------|------------------------|
| $\rho_0$        | (Mg/m <sup>3</sup> ) | 1.490          | 1.426          | 1.859          | 1.971                  |
| $B_0$           | (GPa)                | 0.6237         | 0.8889         | 1.214          | 1.103                  |
| $\nu$           |                      | 0.31           | 0.14           | 0.257          | 0.48                   |
| $B_1$           |                      | 0              | 0.7622         | 0.8622         | ---                    |
| $B_1$           | (MPa)                | ---            | ---            | ---            | 2.382                  |
| $B_2$           | (MPa) <sup>-1</sup>  | 0              | 0.2087         | 0.3965         | ---                    |
| $B_2$           |                      | ---            | ---            | ---            | 2.139                  |
| $S_1$           |                      | 0              | 0.35           | -0.8           | 0.51                   |
| $S_2$           | (MPa) <sup>-1</sup>  | 0              | 0.3859         | 0.3464         | 0.6603                 |
| A               | (MPa)                | 1.966          | 7.604          | 0.7084         | $8.123 \times 10^{-2}$ |
| B               | (GPa) <sup>-1</sup>  | 346.4          | 91.42          | 468.5          | ---                    |
| B               | (MPa)                | ---            | ---            | ---            | 3.102                  |
| C               | (MPa)                | 1.902          | 7.546          | 0.6368         | $8.123 \times 10^{-2}$ |
| D               | (GPa) <sup>-1</sup>  | 38.61          | 131.2          | 150.0          | 800.0                  |
| w               |                      | 0.37           | 0.16           | 0.12           | $1.0 \times 10^{-4}$   |
| R               |                      | 2.252          | 2.179          | 2.785          | ---                    |

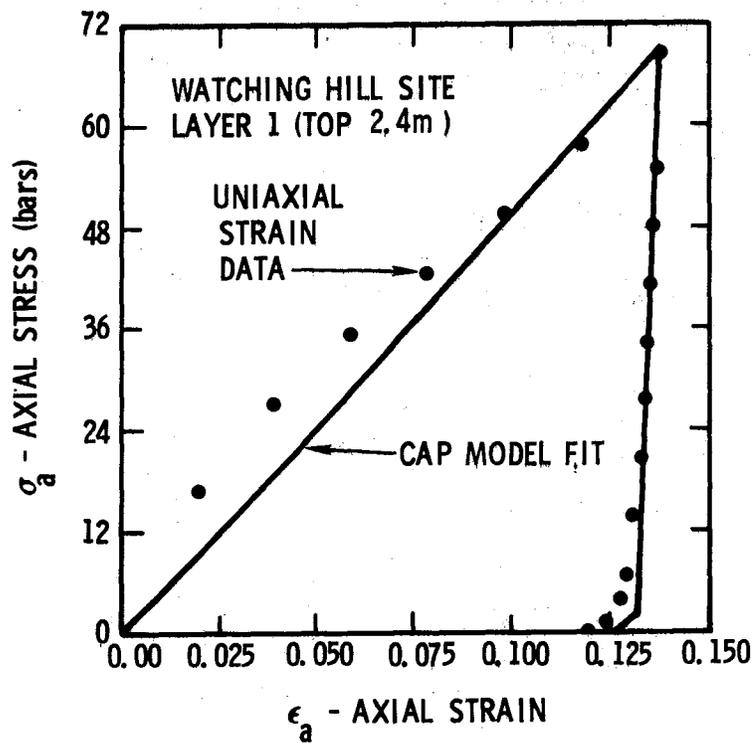
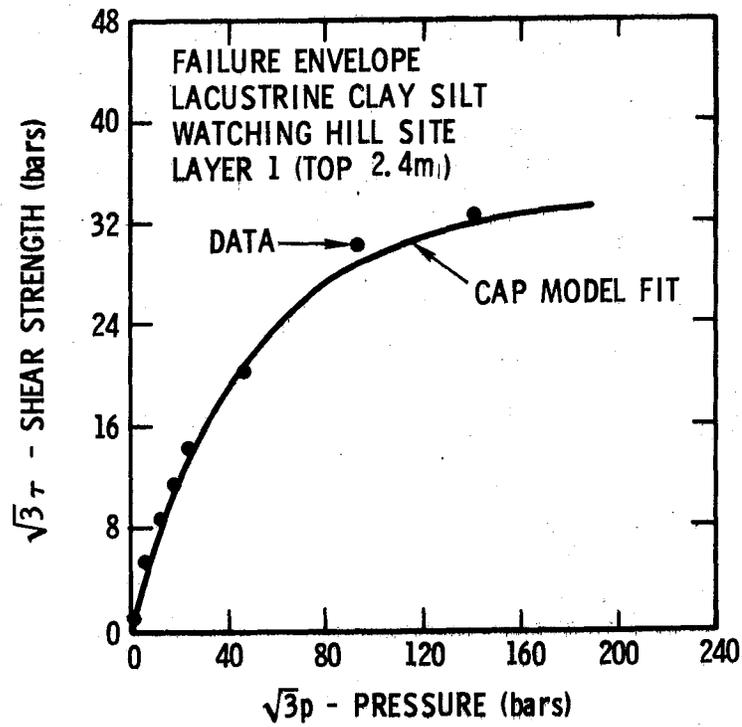


Figure II-3. Cap Model Fit to Uniaxial Strain and Triaxial Failure Envelope Data for Layer 1 at Watching Hill

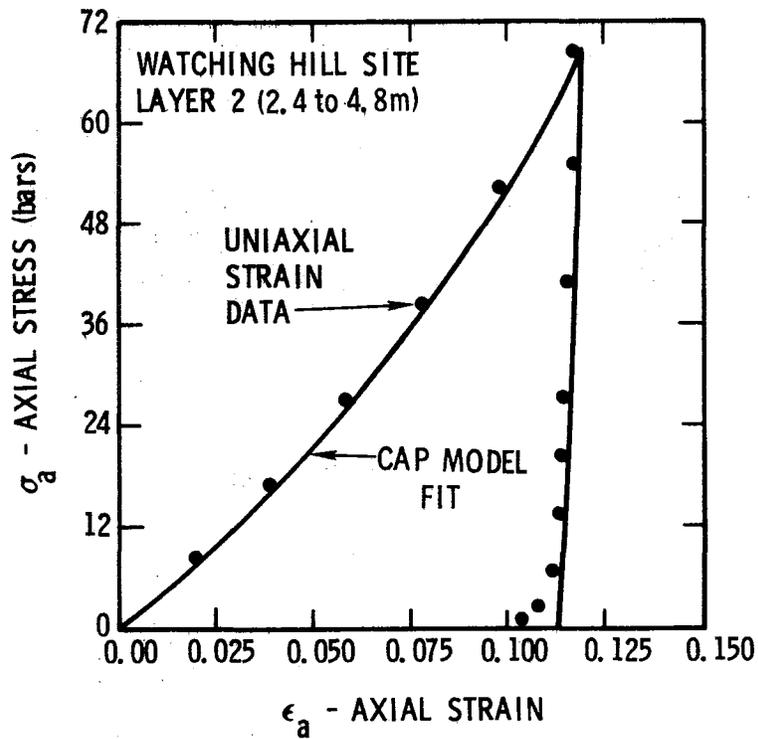
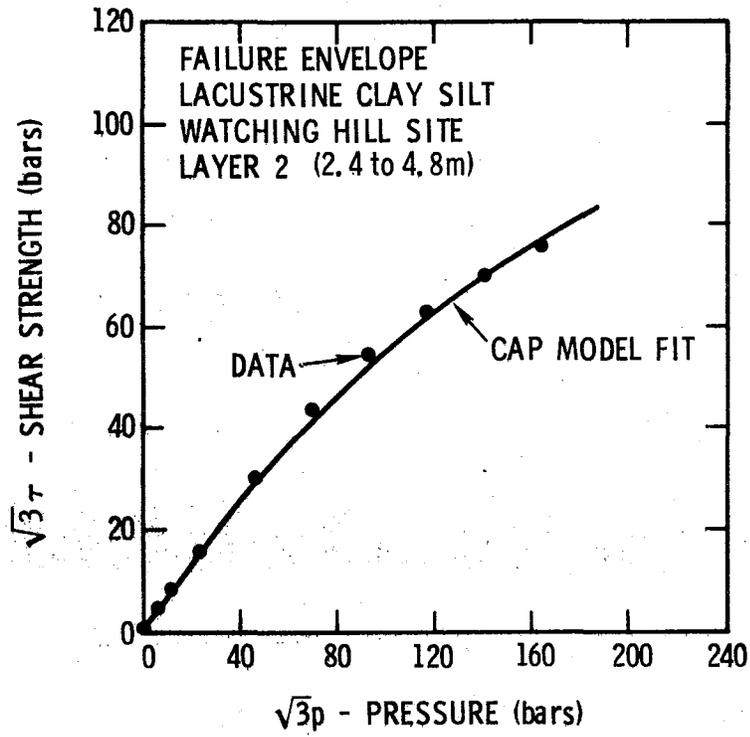


Figure II-4. Cap Model Fit to Uniaxial Strain and Triaxial Failure Envelope Data for Layer 2 at Watching Hill

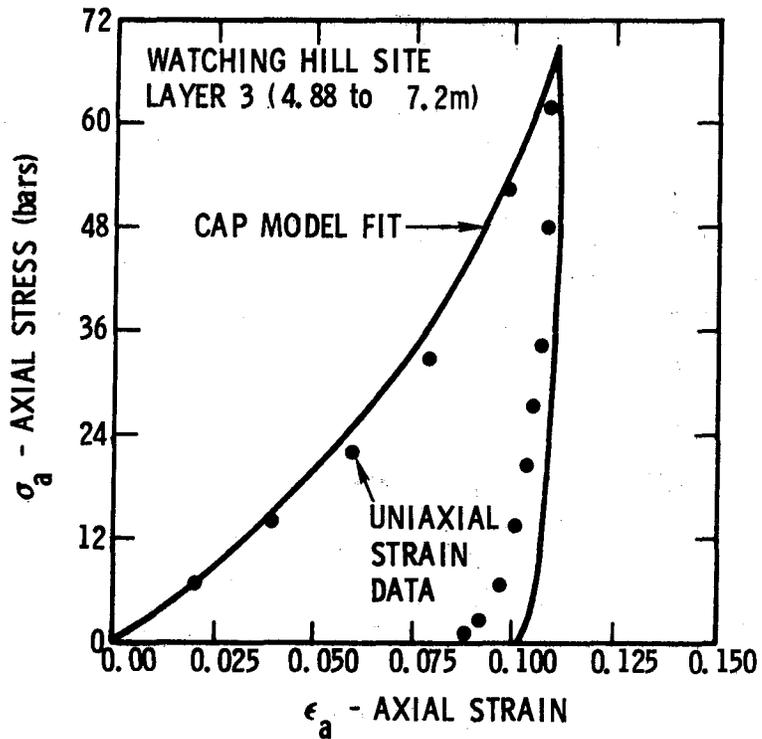
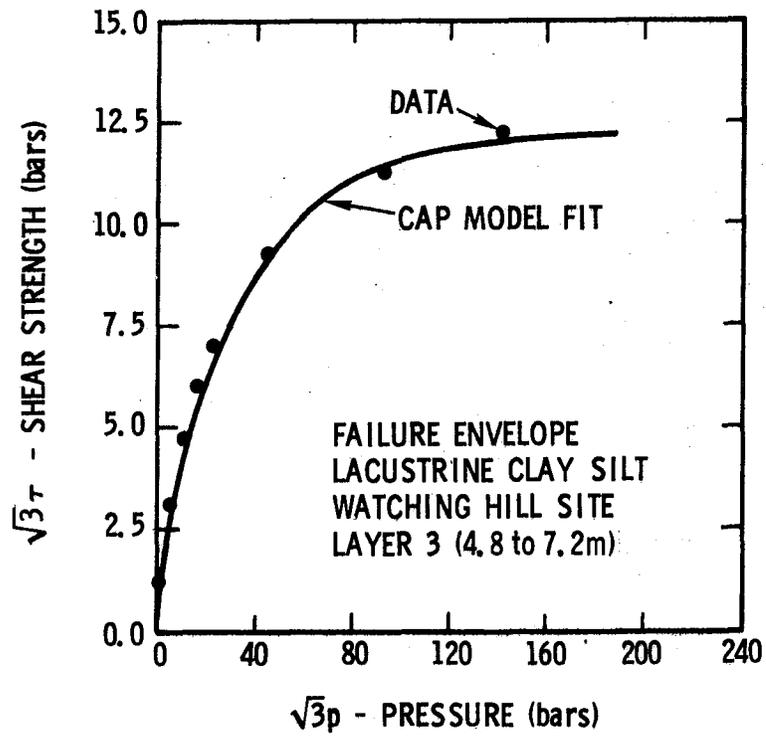


Figure II-5. Cap Model Fit to Uniaxial Strain and Triaxial Failure Envelope Data for Layer 3 at Watching Hill

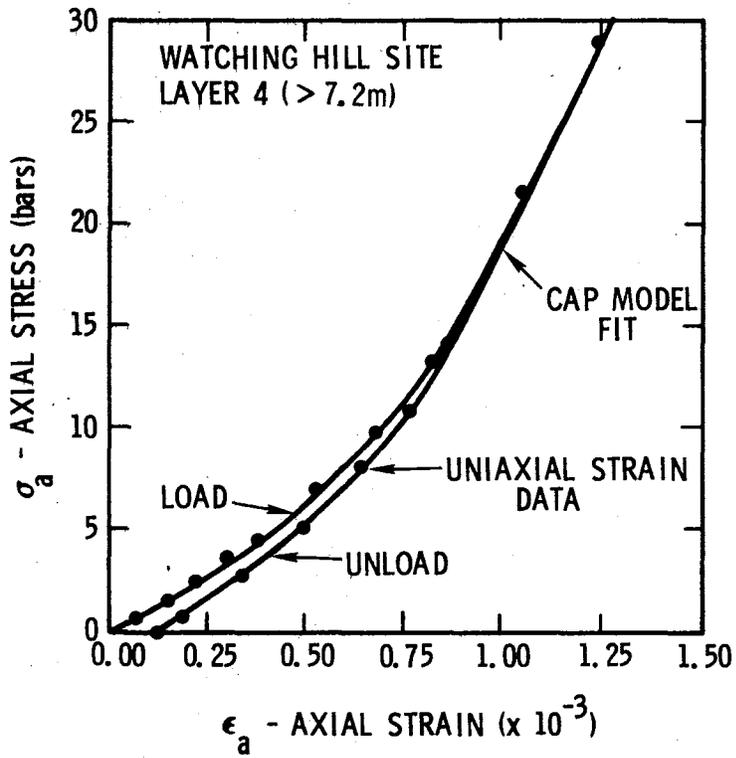
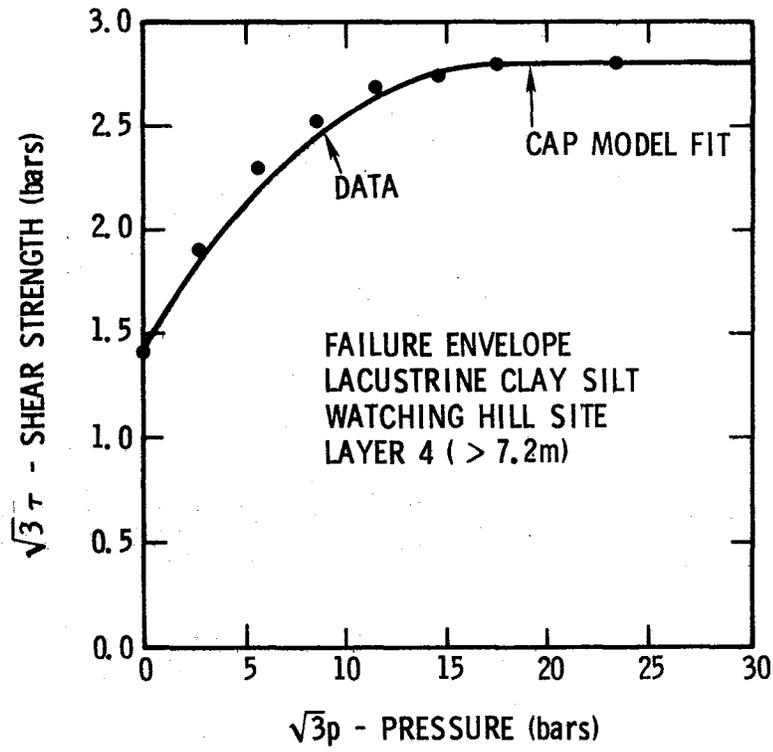


Figure II-6. Cap Model Fit to Uniaxial Strain and Triaxial Failure Envelope Data for Layer 4 at Watching Hill

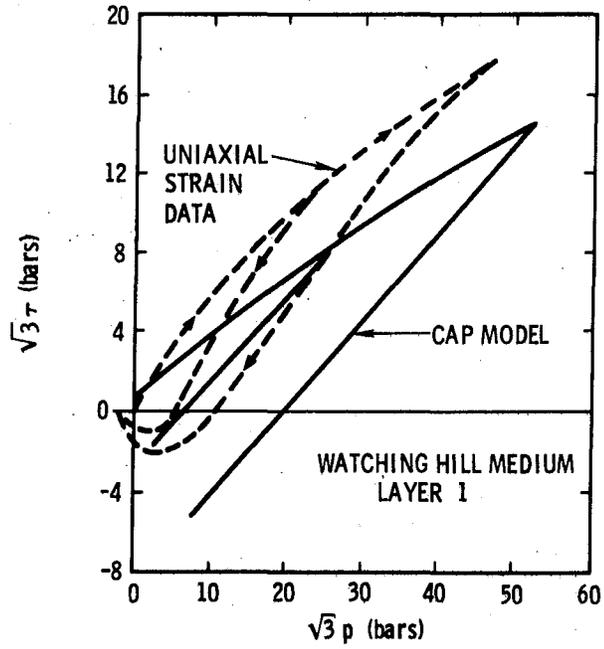


Figure II-7. Uniaxial Strain Path in  $\tau$ - $p$  Space for Layer 1

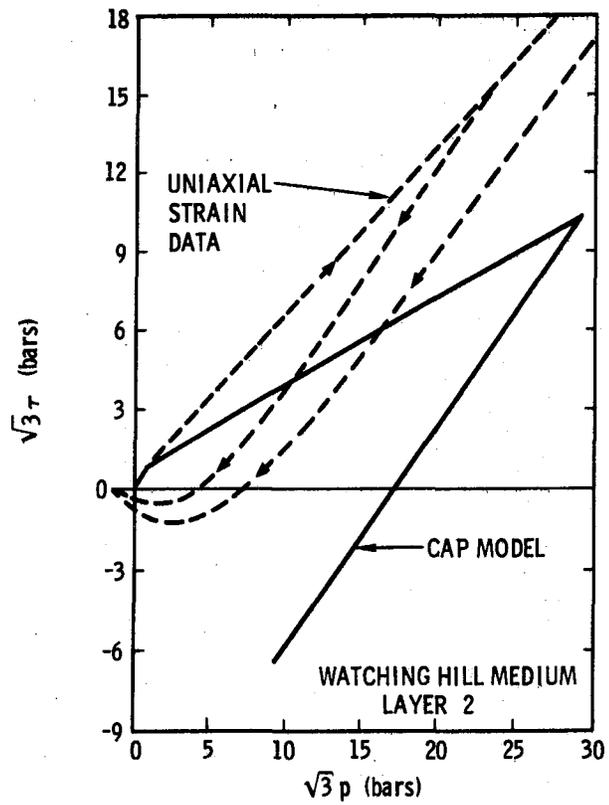


Figure II-8. Uniaxial Strain Path in  $\tau$ - $p$  Space for Layer 2

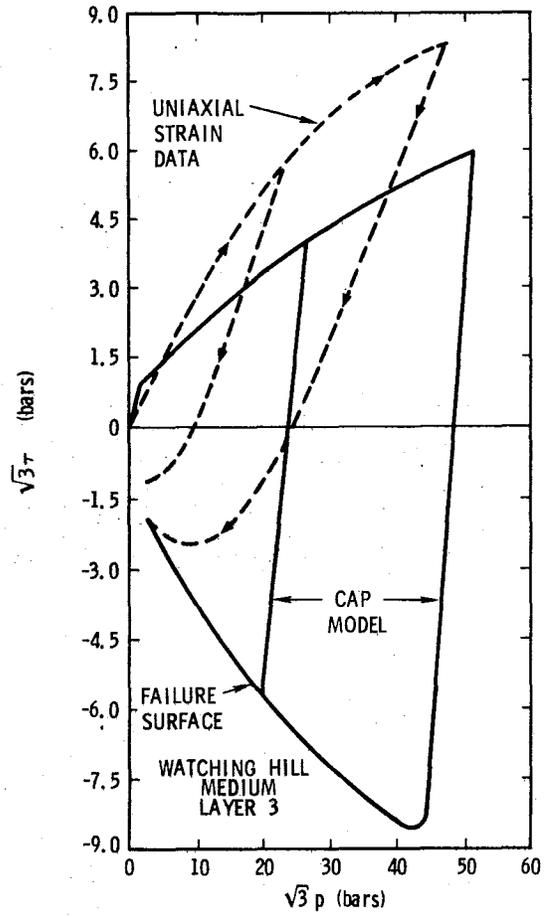


Figure II-9. Uniaxial Strain Path in  $\tau$ - $p$  Space for Layer 3

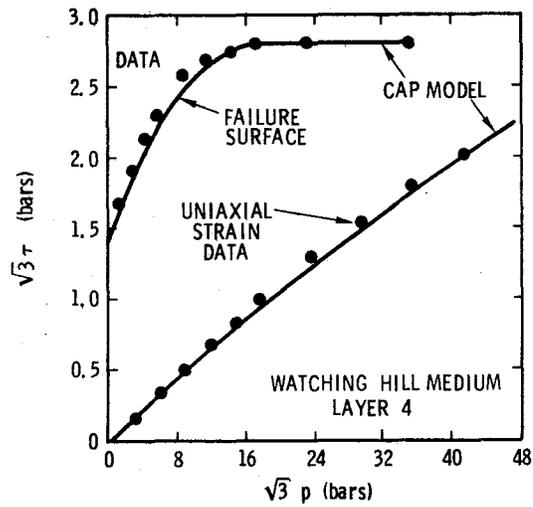


Figure II-10. Uniaxial Strain Path in  $\tau$ - $p$  Space for Layer 4

lations undoubtedly can better fit the available laboratory data and could be employed in future calculations to assess sensitivity of calculated projectile penetration results to cap model expressions and parameters.

It should be pointed out that the cap model, as implemented in TOODY for the calculations reported here, differs in some details from the cap model described by Nelson et al.<sup>15</sup> In particular, the relations for the variation of bulk and shear moduli with  $p$  and  $\tau$  do not satisfy the compatibility requirements which arise from the assumption of the existence of an elastic strain energy function. Also, the particular function chosen to model the cap for Layer 4 exhibits a corner on the pressure axis. The effect of these variations on the particular calculations reported here is difficult to assess.

## SECTION III

### RIGID PROJECTILE CALCULATIONS

The TOODY<sup>3</sup> Lagrangian wave propagation code was used to predict target and penetrator motions and stresses during the experiments planned for the Watching Hill test site. The code is termed Lagrangian because the nodes of the calculational grid move in response to the local stress gradients. The basic process the code performs is to solve difference analogs to the partial differential equations describing the balance of momentum, mass, and energy, and the constitutive relations. This procedure is executed at each node of the grid, the time is then advanced, and the whole process repeated until the desired final time of the calculation is reached.

Since the time-step with which the calculation advances is controlled by the minimum distance on a mesh over the entire grid, large distortions can result in an inefficient calculation. Large distortions can also degrade the accuracy of the numerical methods used in the code, which then yield unrealistic results. For these reasons, the TOOREZ<sup>4</sup> code was developed to permit carrying Lagrangian code calculations past the point where they would otherwise have to be abandoned. TOOREZ allows the user to redistribute the nodes of the calculational grid (i.e. rezone the problem), then repartitions the mass, momentum, and energy in such a way that all these quantities are conserved. Using the output from the rezoning code, the calculation can then be resumed.

The positions of nodes in the calculational grid which originally lie on the axis of rotational symmetry are prevented from occupying the

space occupied by the penetrator. The motion of each of these nodes is first calculated in the standard way from the stress divergence, including the effects of soil-penetrator friction, if any. In this calculation, a condition of perfect slip was assumed for the soil-penetrator interface. If the standard motion calculation for the node yields a position on the surface of, or outside, the projectile, no adjustments are necessary. When a node is calculated to lie inside the penetrator, adjustments to the velocity and position are made so that the normal velocity relative to the penetrator is zero, the tangential velocity has that value already calculated, and the position is on the penetrator surface. In resolving the velocity into normal and tangential components on the ogival nose, the position of the node at the previous time step is used to evaluate the local normal direction. The areas and volumes for material and momentum zones adjacent to the penetrator are adjusted, where necessary, to include the effect of the penetrator surface.

At the beginning of each time step of the calculation, surface tractions for all soil zones in contact with the penetrator are integrated to give the total axial force acting to decelerate the penetrator. For a zone in contact with the penetrator surface the stress is assumed constant, and the axial contributions of the normal stress and frictional stress, if any, are expressed as functions of position on the penetrator surface. These are integrated over the range covered by the zone, so that, on the nose, changes in the local normal direction and surface area are accounted for.

For this calculation, it was desired to model the target to a large depth. Therefore, the initial zoning of the target region utilized expon-

tially increasing zone sizes to allow good resolution near the surface and maintain a reasonable number of zones in the problem. Table III-1 describes the initial zoning. As penetration depth increases to the regions where the zone sizes become too large for good resolution, the rezoning code is used to adjust the zoning, providing smaller zones in front of and on the nose of the penetrator. It was determined early in the calculation that no significant changes occur in the soil once the nose of the penetrator has passed by, so nothing is lost by decreasing the resolution behind the penetrator.

TABLE III-1

Initial Zoning for Rigid Projectile Calculation

FOR ALL REGIONS: 
$$z = z_{j_0} + \frac{\Delta z}{\lambda_z} (\exp((j_0 - j) \ln(1 + \lambda_z)) - 1)$$

$$x = x_{i_0} + \frac{\Delta x}{\lambda_x} (\exp((i - i_0) \ln(1 + \lambda_x)) - 1)$$

| REGION:  | $z_{j_0}$ | $x_{i_0}$ | $\Delta z$ | $\Delta x$ | $\lambda_z$ | $\lambda_x$ | $j_0$ | $i_0$ |
|--|-----------|-----------|------------|------------|-------------|-------------|-------|-------|
| 1<br>( $1 \leq i \leq 25$ ;<br>$67 \leq j \leq 91$ ) | 0.        | 0.        | .03        | .03        | 0.02        | 0.02        | 91    | 1     |
| 2<br>( $1 \leq i \leq 25$ ;<br>$1 \leq j \leq 67$ )  | 0.9127    | 0.        | 0.0483     | .03        | .05         | .02         | 67    | 1     |
| 3<br>( $26 \leq i \leq 46$ ;<br>$1 \leq j \leq 68$ ) | 0.        | 0.9127    | 0.0483     | 0.0483     | 0.05        | 0.05        | 68    | 26    |

Figure III-1  
 DECELERATION vs DEPTH FOR ZONE SIZE TEST PROBLEMS

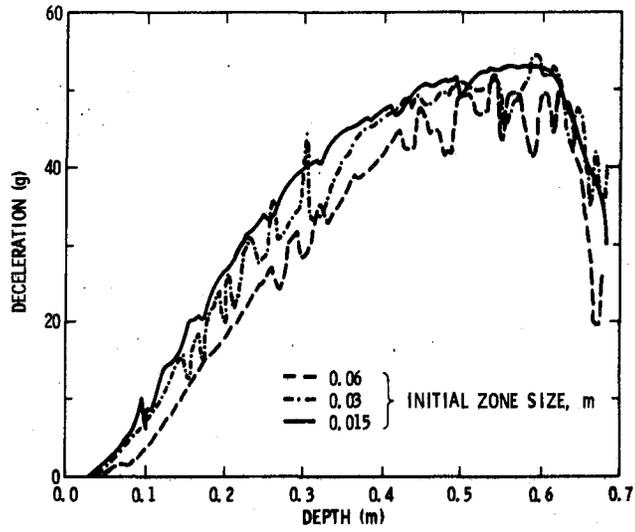


Figure III-3

Figure III-2  
 NORMAL STRESS DISTRIBUTION ON PROJECTILE NOSE FOR ZONE SIZE TEST PROBLEMS

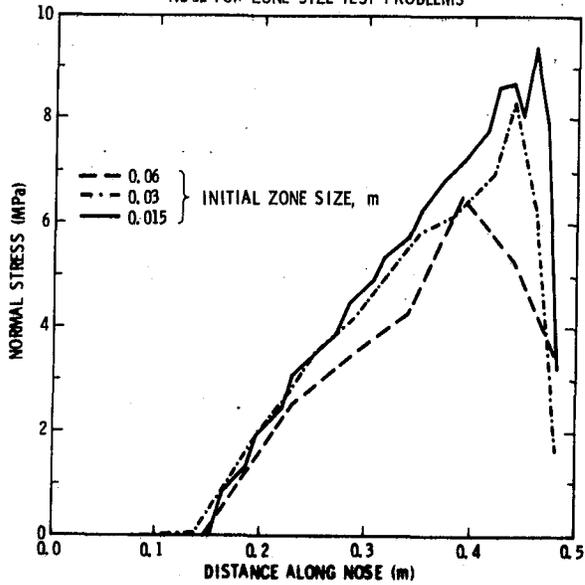
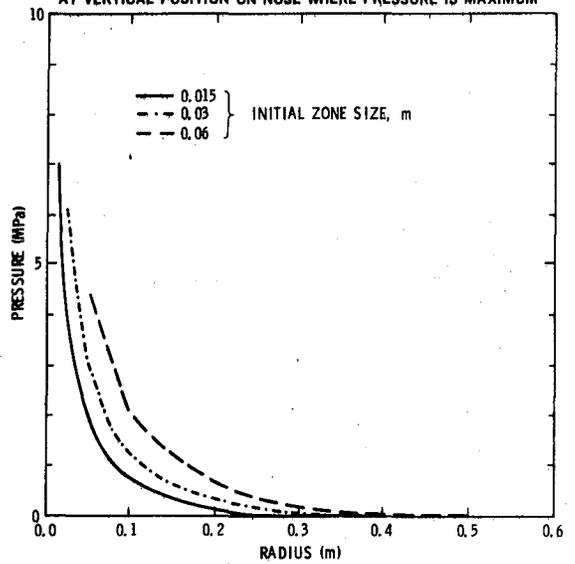


Figure III-3  
 PRESSURE vs RADIAL POSITION FOR ZONE SIZE TEST PROBLEMS AT VERTICAL POSITION ON NOSE WHERE PRESSURE IS MAXIMUM



The calculation was carried out to a time of approximately 52.5 ms, at which time the penetrator had reached a depth of 7.3 m, and retained a velocity of 129 m/sec. The peak deceleration encountered by the penetrator was approximately 55 g's, and at the end of the calculation the deceleration appeared to be decreasing, as the nose begins to enter layer 4, to a value less than 20 g's.

Taking a constant deceleration of 20 g's in the assumed uniform material of layer 4 below 7.2 m leads to a value of about 0.7 sec for total time to penetration depth and a value of 50 m for final depth of penetration. These are the results expected, based on calculated projectile motion through the first three layers, had the calculation been carried out until the penetrator comes to rest. The duration of projectile penetration and final depth thus predicted are much larger than observed in experiment, suggesting a shortcoming in the calculation due possibly to friction effects or to use of a material response model for Layer 4 which is not an accurate representation of the actual medium encountered by the penetrator (see Section V for further discussion).

The calculations indicated that the value of deceleration achieved was somewhat sensitive to zone size, although the precise degree of this sensitivity was not known. For this reason, an analysis of the effect of zone size was undertaken. Three calculations were run with a projectile penetrating 0.6 m of Layer 1, with initially square zones of 0.015, 0.03, and 0.06 m. Initial conditions were identical to those of the main problem. Figures III-1 and III-2 show deceleration-depth curves and normal stress distribution along the nose at a penetrator depth of 0.4 m, respectively. It may be noted from these graphs that while alterations in initial zone

size have a marked effect on the normal stress distribution, the deceleration is much less affected for the range of zone sizes considered. This is evidently due to the fact that where disparities in the normal stress distributions are largest, the area over which the normal stress acts is relatively small. That is to say that for the smaller mesh calculations the normal stress distribution along the projectile nose has its maximum shifted toward the nose tip (see Figure III-2). Figure III-3 shows pressure vs radial position at the depth of peak normal stress, at a penetrator depth of 0.4 m. As expected, the finer zoning allows resolution of steeper gradients. Some sort of extrapolation to obtain the stress at the soil-projectile interface, rather than one half-zone away, would have yielded somewhat higher decelerations, but probably not enough higher, taken by itself to cause a large change in duration of the calculation or to influence significantly the values of projectile deceleration calculated. A combination of considerably finer zoning than was used in the main calculation, and extrapolation to find stress at the soil-projectile interface would provide a slightly more realistic calculation, but would also be quite expensive in terms of computer time. Increases in calculated normal stress and projectile decelerations due to finer zoning and extrapolation are estimated to amount to at most 20% using the techniques employed in the rigid body calculation.

It was hoped that the rezones of the problem could be accomplished with no significant effects on the histories being accumulated at the selected points in the soil. This goal is really only a reasonable one for those quantities and their integrals which are conserved during the rezoning process. The higher degree of smoothness of the velocity histories as compared to the stress measure histories reflects this fact.

Rezoning of the problem were performed at

| TIME (ms) | DEPTH (m) |
|-----------|-----------|
| 1.38      | .21       |
| 3.05      | .46       |
| 8.0       | 1.2       |
| 11.9      | 1.78      |
| 14.6      | 2.18      |
| 23.4      | 3.45      |
| 33.8      | 4.88      |
| 41.6      | 5.91      |

Due to tape handling problems, history information for the period from 11.9 ms to 14.6 ms was lost.

Appendix A presents results of the calculation in graphical form. Figures A-1 through A-5 show deceleration, velocity and depth vs. time, and deceleration velocity vs. depth. Figures A-6 through A-9 show projectile kinetic energy, soil kinetic energy due to radial velocity, soil kinetic energy due to vertical velocity, and total kinetic energy of the soil, all per radian, and all vs. time. Table A-1 and Figure A-10 provide keys to figures A-11 through A-78, which show histories of various quantities at selected points in the soil. (Where they appear, radial and axial stress components are plotted positive in compression). Figures A-79 through A-141 show the calculational grid near the projectile, normal and shear stress distributions along the projectile, and contours of selected quantities in the soil. Due to the rezoning method used, only the grid lines with depths near that of the nose region are representative of target deformation. Also, for projectile depths greater than 0.4 m, the spatial scaling is distorted, so that radial distances appear twice as large as their actual value. The grid plots contain "x" in the

center of a zone calculated as failing in tension, and "c" where the stress state is on the failure envelope. When a mesh is calculated to fail in hydrostatic tension, its pressure is set to zero, and its stress deviator is limited by the smaller of the deviator stress on the cap and the failure envelope at zero pressure. Therefore, a zone may, in some cases, contain both x and c. It should also be noted that the normal and shear stresses plotted are actually those at zone centers; i.e., one-half zone away from the projectile. For these plots, a positive normal stress and a negative shear stress would retard the projectile.

Table A-2 provides a key to Figures A-79 through A-141. It should be noted that the sign convention for stress components is opposite that used for the history plots; i.e. consistent with a positive normal stress being one of extension.

## SECTION IV

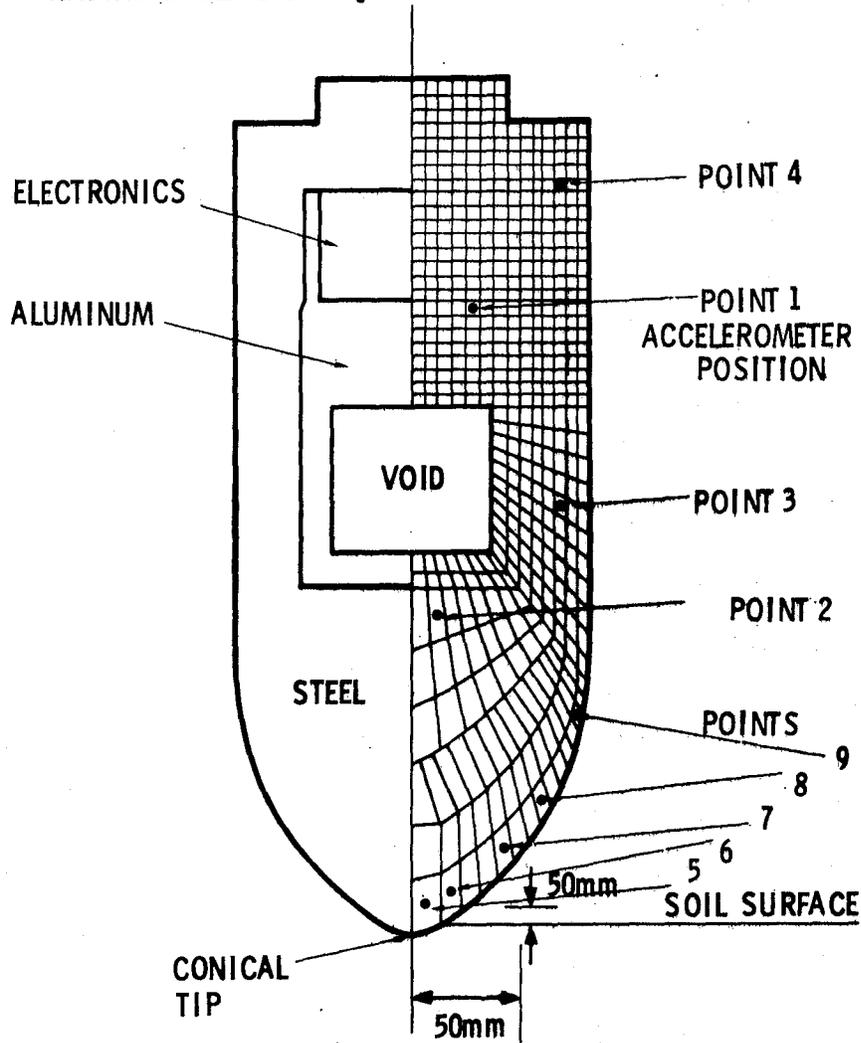
### DEFORMABLE PROJECTILE CALCULATION

To test the assumption of a rigid body and to calculate the response of the vehicle to the imposed loads, a second TOODY calculation was performed. The vehicle was zoned as shown in Figure IV-1, and the ground was defined by 30-mm squares to a radius of 0.6 m and a depth of 0.9 m. For this calculation the 45° conical tip was included, as on the actual vehicle, rather than the idealized perfect ogive used in the rigid body calculation. Figure IV-1 also shows points in the projectile at which the progress of the calculation was recorded and plotted. Plots were also made for points in the soil corresponding to depths of 0.1 m, 0.2 m, and 0.4 m, with distances from the central axis of 75 mm, 0.14 m, 0.28 m, 0.44 m, and 0.58 m.

The spacer was treated as an aluminum shell containing a vacuum. The electronics package was modeled with a hydrodynamic "foam" equation of state. The rest of the vehicle was treated as steel. The ground was represented by the cap model for Layer 1. The input parameters for the vehicle materials were

FIGURE IV-1

ZONING OF THE DEFORMABLE PENETRATOR,  
 • POINTS AT WHICH HISTORY WAS RECORDED  
 RADIAL DIMENSIONS QUADRUPLED TO SHOW DETAIL



• Points Used for Plotting Histories

| ID       | R(m) | Z(m)   | Figs. (App. A) |
|----------|------|--------|----------------|
| 1        | .022 | -1.155 | 22, 23, 24     |
| 2        | .010 | -.580  | 25, 26, 27     |
| 3        | .069 | -.785  | 31, 32         |
| 4        | .069 | -1.388 | 33, 34         |
| 5        | .006 | -.028  | 28, 29, 30     |
| 6        | .017 | -.048  | 35, 36         |
| 7        | .041 | -.136  | 37             |
| 8        | .060 | -.225  | 38             |
| 9        | .077 | -.376  | 39             |
| Nose tip |      | + .003 |                |

|                               | <u>Steel</u> | <u>Aluminum</u> | <u>Electronics</u> |
|-------------------------------|--------------|-----------------|--------------------|
| $\rho_0$ (Mg/m <sup>3</sup> ) | 7.850        | 2.700           | 1.400              |
| $c_0$ (km/s)                  | 4.610        | 5.390           | 2.000              |
| $\nu$                         | .296         | .333            | --                 |
| $K = \rho_0 c_0^2$ (GPa)      | 166.8        | 78.4            | 5.6                |
| $Y_0$ (GPa)                   | 1.324        | 0.02            | --                 |
| $c_e$ (m/s)                   | --           | --              | 500                |
| $\alpha_0$                    | --           | --              | 2                  |
| $p_e$ (MPa)                   | --           | --              | 1                  |
| $p_s$ (MPa)                   | --           | --              | 10                 |

The last four parameters pertain to the p- $\alpha$  foam model<sup>19</sup>;  $c_e$  is the ambient value of the sound speed in the virgin foam at the initial distention  $\alpha_0$ ,  $p_e$  is the elastic limit, and  $p_s$  is the compaction pressure for which all voids are assumed to be closed. Therefore,  $c_0$  is the bulk sound speed of the fully compacted solid.

Friction at the vehicle-soil interface was neglected, and separation of soil from projectile surface was not permitted. The calculation was run to a time of 2.40 msec, at which time the nose tip had reached a depth of 0.398 m. This calculation consumed 2.94 hours of CDC-6600 central processor time. The problem was not rezoned.

Figures B-1 through B-7 in Appendix B describe the configuration, velocities and stresses 0.40 msec after impact, with the nose tip 0.094 m below the ground surface. The situation at 1.10 msec is shown in Figures B-8 through B-14, corresponding to a penetration depth of 0.20 m. Figures B-15 through B-21 give the final configuration. Velocity and

stress contours are not shown for the projectile material because the high-frequency ringing of the vehicle renders contours there incomprehensible. A few contours are shown as passing through the projectile region; these are intended to clarify the relationship of the contours and are unrelated to actual values in the projectile material.

Figures B-22 through B-30 display motion history for three points in the projectile. The motion of points away from the tip is dominated by ringing that masks the rigid body deceleration of the vehicle. Point 5, 40.5 mm back from the tip and 6.35 mm from the axis, experienced an initial acceleration associated with deformation of the nose on impact, followed by a deceleration as the nose absorbed the initial ground resistance (Figure B-28).

Stress histories at selected points within the vehicle are shown in Figures B-31 through B-36. In these and subsequent plots, "J2" is the label for the quantity  $\sqrt{\sigma'_{ij}\sigma'_{ij}/2}$ , which was the requested output quantity, where  $\sigma'$  is the deviator stress tensor. This quantity is proportional to octahedral shear stress,  $\sqrt{\sigma'_{ij}\sigma'_{ij}/3}$ . At a point in the projectile 61 mm from the tip and 12 mm from the axis, the peak mean stress exceeded 0.14 GPa and  $\sqrt{\frac{1}{2}\sigma'_{ij}\sigma'_{ij}}$  exceeded 0.28 GPa (Figures B-35 and B-36). At the tip of the vehicle (not plotted), mean stresses in excess of 0.5 GPa and axial stresses in excess of 1.3 GPa were noted both in compression and tension, and plastic yielding occurred.

Figures B-37 through B-39 contain normal stress histories at three points along the nose of the projectile (see Figure IV-1); the shear stresses were assumed to be zero. Because stresses were not calculated at the interface, the values given were calculated within the vehicle,

one-half mesh width from the surface. The largest stress in these figures is 43 MPa, which occurred at the point closest to the nose tip (Figure B-37).

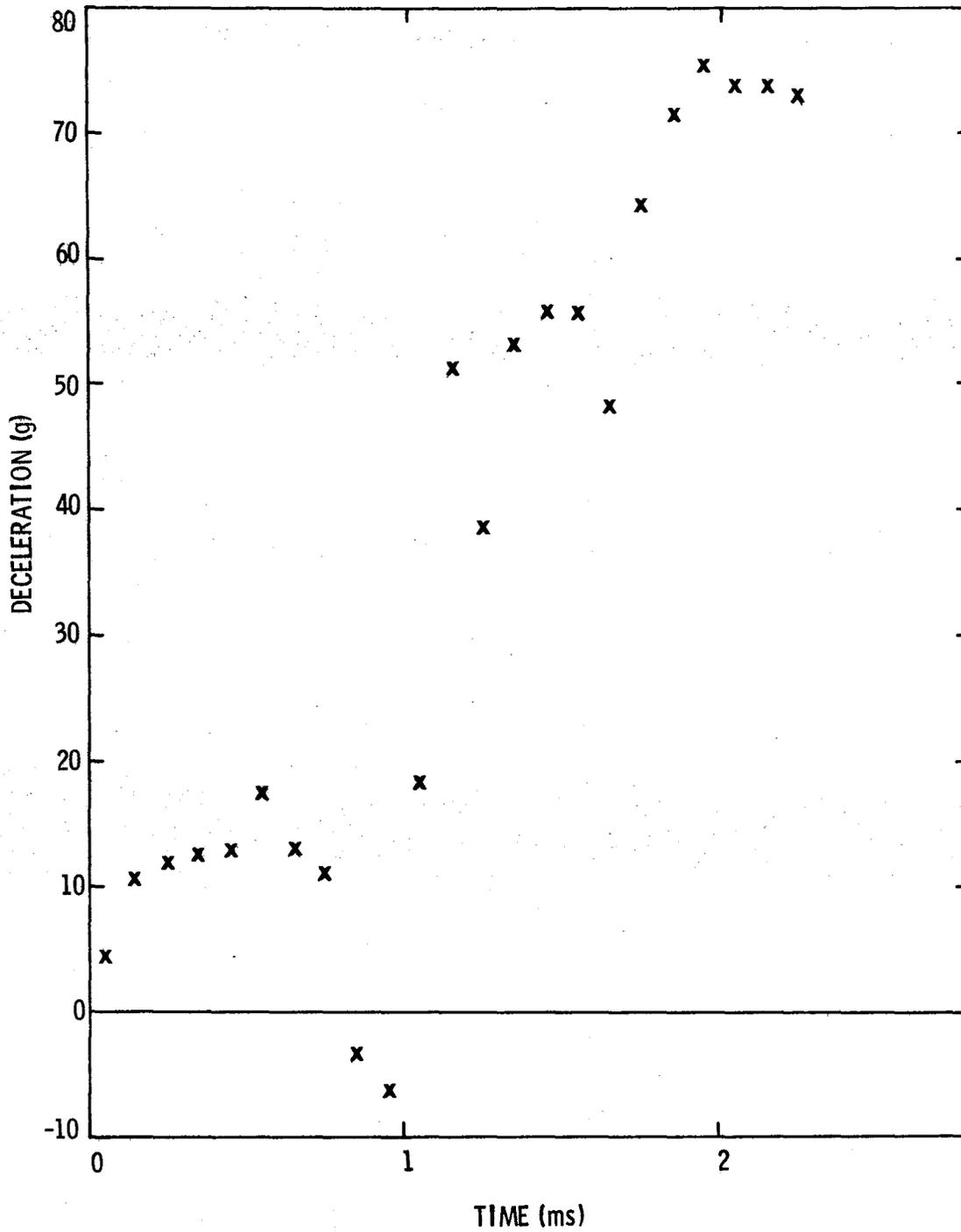
The total kinetic energy calculated for the soil followed the history shown in Figure B-40. The saw-tooth pattern is caused by numerical noise, a peak occurring each time the nose tip encounters a new grid point in the soil. The noise is accentuated because the total kinetic energy in the soil is small, because it is concentrated in a few zones near the axis of symmetry, and because the approximation used to sum the kinetic energy has undesirable characteristics when applied near the axis of symmetry. This effect was not seen in the rigid body calculation (Fig. A-9) because the time interval chosen for recording the energy happened to be almost exactly one period for this oscillation, and because the omission of the conical tip allowed a smoother solution in the rigid case.

The history of motion and stresses at the selected points in the soil are shown in Figures B-41 through B-46. Histories were also recorded at three points with range 0.6 m from the impact line, but the mean stress never exceeded 10 kPa, the level required to activate calculation of motion. Before comparing these results to the rigid projectile calculation, the times shown must be increased by 0.4 msec to account for the nose tip being 26 mm shorter and for the tip being buried 33 mm at the beginning of this calculation. With this adjustment, the soil histories are in excellent agreement. The peak mean stress observed at the closest point (range .105 m, depth 75 mm) was 2 MPa, and the largest radial velocity was 16 m/s (Figures B-41 through B-46).

The total momentum in the vehicle was summed at 0.2-ms intervals and then differenced to obtain the deceleration history shown in Figure IV-2. The deceleration is up to thirty six percent larger than the results for the rigid body calculation (Figure III-1). This difference is related, in part, to the use of an ideal ogive in the rigid body calculation, compared with the 45° tip appearing on the actual vehicle and included in the deformable body calculation. The soil velocity reaches 180 m/s on the 45° nose tip, whereas in the rigid body calculation the soil velocity does not exceed 60 m/s. In the case of the perfect ogive, the soil must reach a velocity of at least 50 m/s to get out of the path of the oncoming vehicle. The higher velocity produces larger stresses in the soil; with the deformable body stress components as large as 14 MPa were calculated, whereas no stress in excess of 8.5 MPa was noted for the rigid body calculation.

Unfortunately, there are no hard experimental data with which to compare the calculated transient vehicle response. However, the experience with this deformable body calculation demonstrates that calculation of the early-time vehicle loads and response is a reasonable and straight-forward application of existing numerical methods, in sharp contrast to the difficulties in calculating penetration depth or to the impossibility of obtaining this information from force law or cavity expansion theories.

FIGURE IV-2  
DECELERATION HISTORY FOR DEFORMABLE PROJECTILE



## SECTION V

### COMPARISON OF PREDICTIONS WITH EXPERIMENT

More than a dozen projectile penetration experiments were conducted<sup>5</sup> at the Watching Hill site with projectiles of various diameters, weights, lengths and nose shapes and with projectile impact velocities ranging from 93 to 202 m/s (305 to 660 ft/sec). Test number 6 had an impact velocity of 150 m/s (493 ft/sec), a 0.1651 m (6.5 in) diameter projectile of mass 181.44 kg (400 lb) with 9.25 CRH tangent ogive nose. This test closely matches conditions employed in calculations and provided projectile motion data for comparison with predictions. Test number 4 was performed<sup>5</sup> with a 0.1524 m (6 in) diameter projectile of mass 127.12 kg (280 lb), 6.25 CRH tangent ogive nose and impacted at a velocity of 158.5 m/s (520 ft/sec). From this test, medium stress histories were obtained with which calculated results can be compared.

#### Projectile Motion

Projectile motion measurements<sup>5</sup> were obtained from accelerometers mounted within the projectile and consist of deceleration versus time during penetration, together with projectile velocity and position histories derived from integrations of deceleration data.<sup>5</sup> Medium response measurements<sup>10</sup> were made with six lithium niobate stress transducers<sup>9</sup> at four locations within the top three designated layers of the target medium. From projectile deceleration data, information is obtained regarding the nature of the resistive forces offered by the soil medium in retarding the projectile's motion. Also, together with calculations, inferences regarding frictional forces acting on the projectile may be made.

Further, from the deceleration history indications are obtained of the gross layering structure within the target medium. From dynamic stress data amplitudes, durations and arrival times are obtained of the pressure disturbance produced in the medium by projectile penetration. The comparison of this information with calculated results provides one measure of how accurately the medium response is modeled in calculations.

Figures V-1 and V-2 illustrate projectile decelerations, calculated and measured (Test No. 6, real time, 200 Hz LPF).<sup>5</sup> The rigid body calculation with zero friction predicts a deceleration of about 55 g's which remains roughly constant during projectile penetration through layers 1 and 2 (each 2.4 m thick). After projectile entry into layer 3 (also 2.4 m thick) calculated deceleration falls to about 35 g's and in layer 4 deceleration again drops to 20 g's or less. This stair-step result is related to the material properties assigned to each of the four idealized layers (Section II). Layers 1 and 2 have shear strengths which differ at most by a factor of 2 at pressures below 10 MPa (see Figures II-3 and II-4). Layers 3 and 4 both have shear strengths much less than layers 1 and 2 and the strength of layer 4 material is considerably less than that of layer 3 over the pressure range of interest (see Figures II-5 and II-6). Assuming that the soil medium's resistance to shear deformation is the primary mechanism influencing projectile deceleration level then the shear strength properties attributed to the four layers, and utilized in calculations, account for the stair-step deceleration history calculated as the projectile penetrates layers 3 and 4. Measured deceleration levels in layers 1 and 2, as indicated by the data trace, the smoothed (by  $\bar{a} = \int_0^t a(t)dt / \int_0^t dt$ ) data curve, and the average deceleration over each designated layer are greater than calculated.

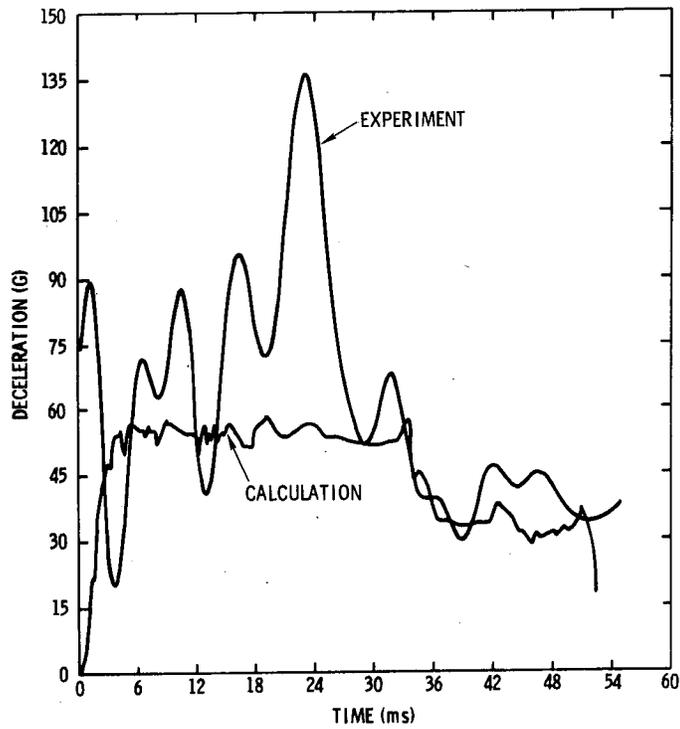


Figure V-1a

Comparisons of Predicted and Measured Projectile Deceleration History.

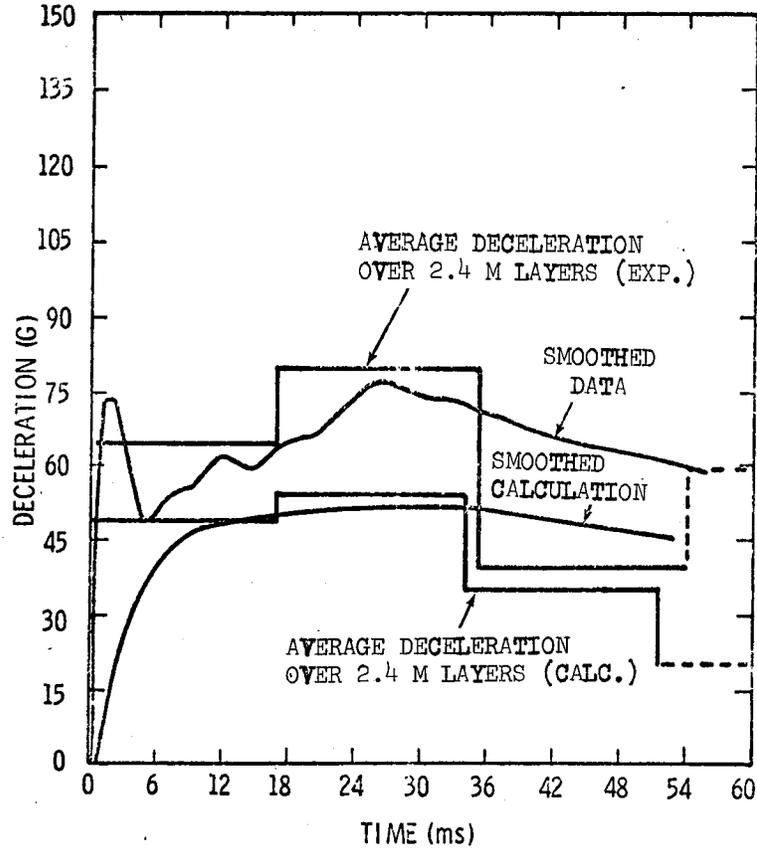


Figure V-1b

Comparisons of Predicted and Measured Projectile Deceleration History.

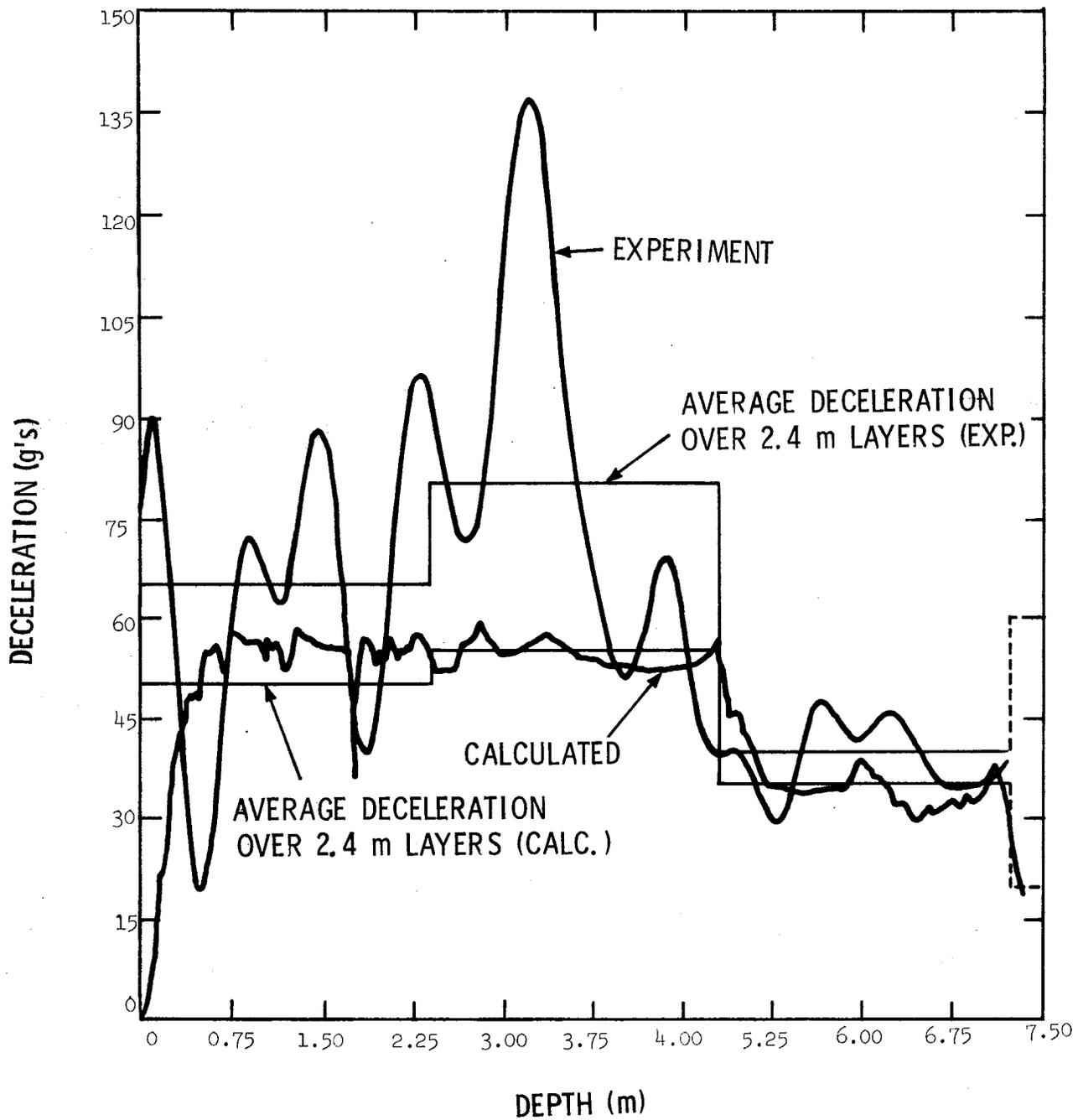


Figure V-2

Comparison of Predicted and Measured Projectile Deceleration versus Depth.

Comparing calculated and measured average deceleration levels (Table V-1) for each of the first 3 layers it is seen that predicted values are 23, 31 and 13% lower, respectively than observed. For layer 4 the difference is considerably greater and the reasons for this are discussed further below.

Since the average decelerations, predicted by the no friction calculation, are less than those observed one may speculate whether or not the differences are a measure of the friction forces operative. For layers 1, 2 and 3, it is seen (Table V-1) that the difference is greatest for the layer 2 of highest shear strength and least for the layer 3 of lowest shear strength. It is apparent that the differences between experimental and predicted average decelerations are in monotonic correspondence to shear strengths of the materials at the normal stress experienced on the projectile nose (Figures A-98, A-116 and A-134). This suggests that a form of the friction law involving the second invariant of the deviator stresses, such as  $\tau_f \propto \tau$  ( $\tau_f$  = frictional stress along soil projectile interface,  $\tau$  = octahedral shear stress), is not inconsistent with data. Similarly, the data of Table V-1 suggests that a friction law related to projectile velocity is probably not correct.

It is of interest to explore the possible sources of discrepancy between calculations and experiment to determine whether or not more definitive information regarding friction forces may be obtained

Table V-1

Difference Between Predicted and Measured Average Projectile  
Decelerations in the Four Layers Assumed for the  
Watching Hill Medium

| Layer | Average Deceleration (g's) |          |                |
|-------|----------------------------|----------|----------------|
|       | Calculated*                | Observed | Difference (%) |
| 1     | 50                         | 65       | 23             |
| 2     | 55                         | 80       | 31             |
| 3     | 35                         | 40       | 13             |
| 4     | ~ 20                       | > 60     | > 67           |

\* No Friction

in order to refine or perfect the prediction technique. Sources of discrepancy include errors in the deceleration measurement, errors in laboratory measurements of material properties, approximations or assumptions made in calculation of the penetration problem and possible inaccuracies associated with the computational method. Approximations and assumptions made in calculation of the penetration problem include neglect of variations in lithostatic pressure with depth, neglect of friction forces, layering in target and use of the soil cap material response model to represent the target medium. Inaccuracies in the computational method involve size of mesh and the closeness with which the cap model is made to represent laboratory data on material properties of the medium.

While the uncertainty associated with each of these sources of error is not known, it is expected that taken in combination all the sources of error from both experiment and calculation are great enough to account for the 13 to 31% discrepancies noted between predictions and

observations. As a result, no definitive conclusions can be drawn regarding the absolute magnitude of friction forces contributing to deceleration of the projectile in layers 1, 2 and 3. However, it appears that the friction forces are most likely less than 50% of the total axial force acting on the projectile. California Research and Technology predictions,<sup>20</sup> obtained with friction on the projectile specified by  $\tau_f = 0.6 \sqrt{J'_{2\max}}$ , yielded deceleration amplitudes of 110 g and 125 g for layers 1 and 2 respectively. Here,  $\sqrt{J'_{2\max}}$  is the function describing the failure envelope, evaluated at the normal stress acting on the projectile. The contribution from friction to the total axial retarding force was about 55% and 56%, respectively. This amount of friction is clearly too great, producing decelerations larger than observed. At most, the amount of friction for layers 1, 2 and 3 is that suggested by differences indicated in Table V-1.

The difference between measured and calculated decelerations in layer 4 material is likely greater than can be accounted for by uncertainties in the experimental data on deceleration and in the computational method. The large discrepancy is felt to be a consequence of material property data and the resultant material response model which is not representative of the actual material of layer 4. Credence to this supposition is given by the full experimental deceleration record<sup>5</sup> shown in Figure V-3. At a depth of 7.2 m, where layer 4 is assumed to begin, projectile deceleration begins to increase and from 7.2 m to 10 m the projectile experiences an increase in retarding force which implies a layer of greater shear strength than that of layer 3. Below a depth of 10 m the projectile enters another layer of lesser strength than the last (but still greater than layer 3 strength) and maintains a nearly

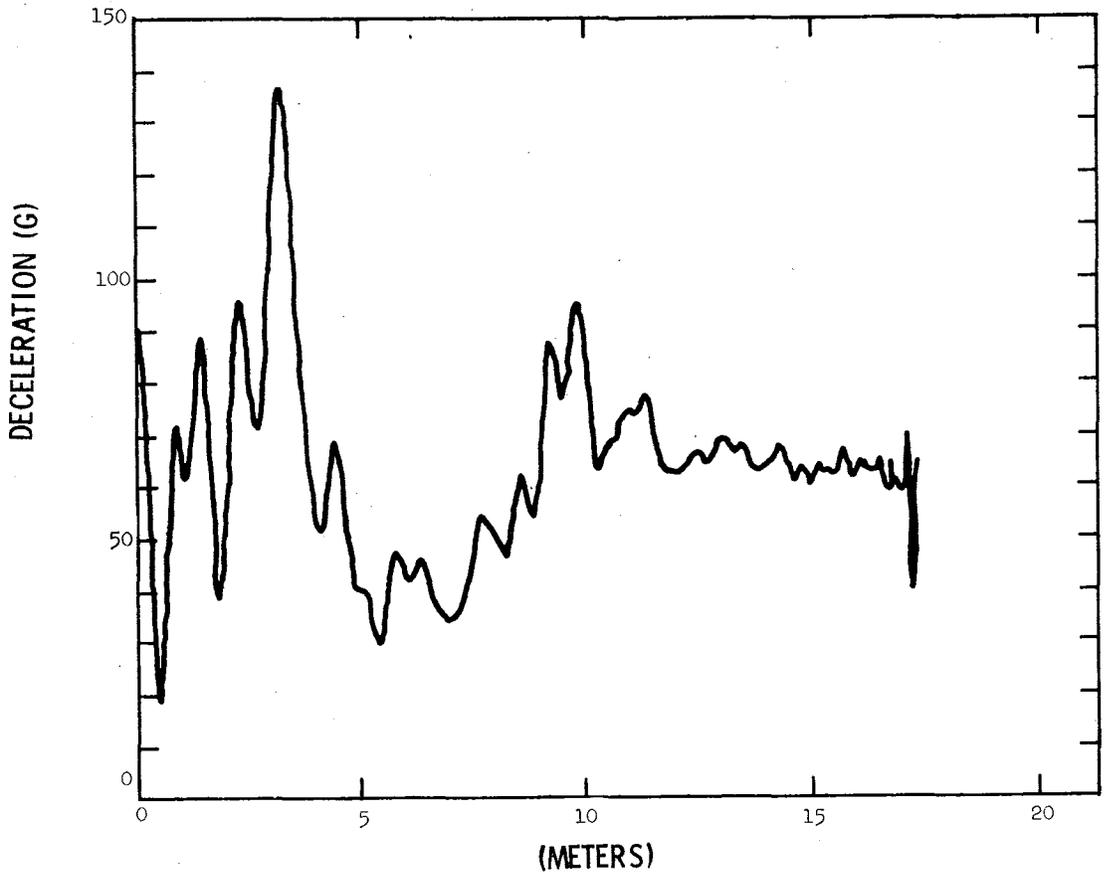


Figure V-3  
Measured Projectile Deceleration versus Depth.

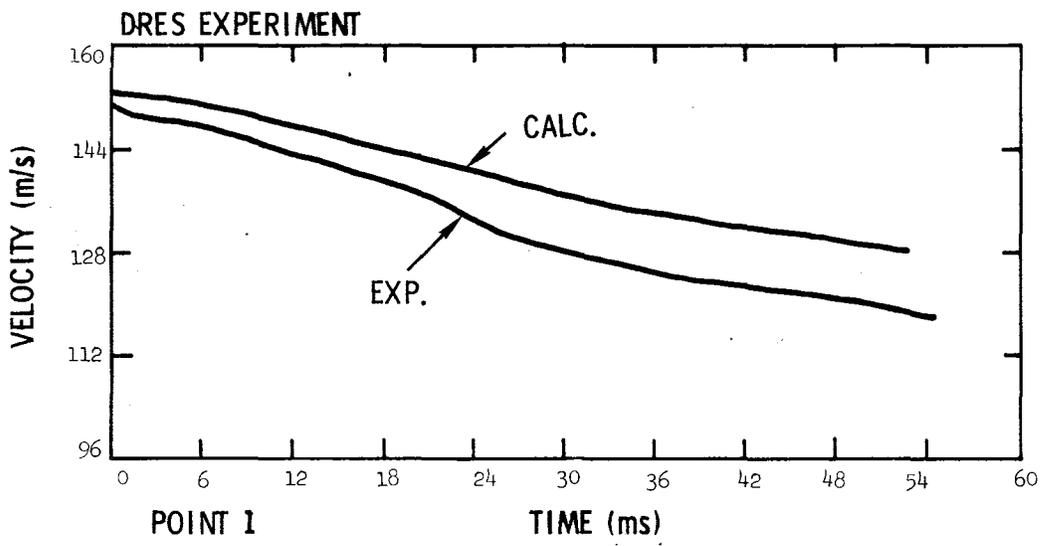


Figure V-4  
Comparison of Predicted and Measured Velocity Histories.

constant deceleration of slightly more than 60 g's. These observations indicate that the target medium would have been modeled better with five layers rather than four and also that the material properties used for layer four are not representative of any of the layers assumed for the penetrated area of the Watching Hill medium. In retrospect, it is apparent that a prior choice of four layers for use in calculations was not the best. Considerably improved results for predicted deceleration history would be obtained in a recalculation of the problem by using five layers rather than four, by taking layer four to be much stiffer in shear than that used in the first calculation, and also by employing a small amount of friction.

Further comparisons of calculated projectile motion with information derived from deceleration data are shown in Figures V-4 through V-8. Of particular interest among these is Figure V-7 for deceleration versus velocity. Within a given layer the calculated curve is independent of projectile velocity indicating a constant retarding force within each uniform layer of material. This result for the Watching Hill medium confirms the force law relationship proposed by Robins and Euler<sup>1</sup> and must eliminate from consideration those, such as Resal's,<sup>1</sup> which require an explicit dependence on projectile velocity.

#### Target Medium Response

To measure medium response during projectile penetration, six lithium niobate stress gauges were located<sup>10</sup> at positions as indicated in Figure V-9a. Figure V-9b illustrates the orientation of four penetration experiments about the stress transducer locations and Table V-3 lists particulars for those four penetrator experiments.<sup>5</sup>

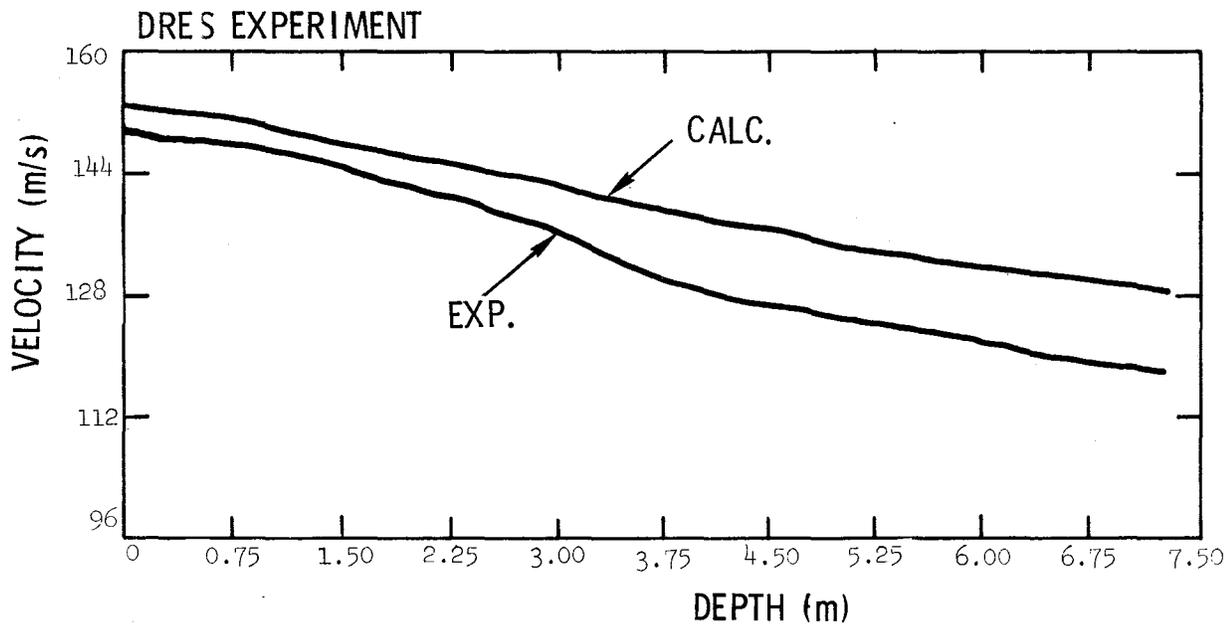


Figure V-5

Comparison of Predicted and Measured Projectile Velocity versus Depth.

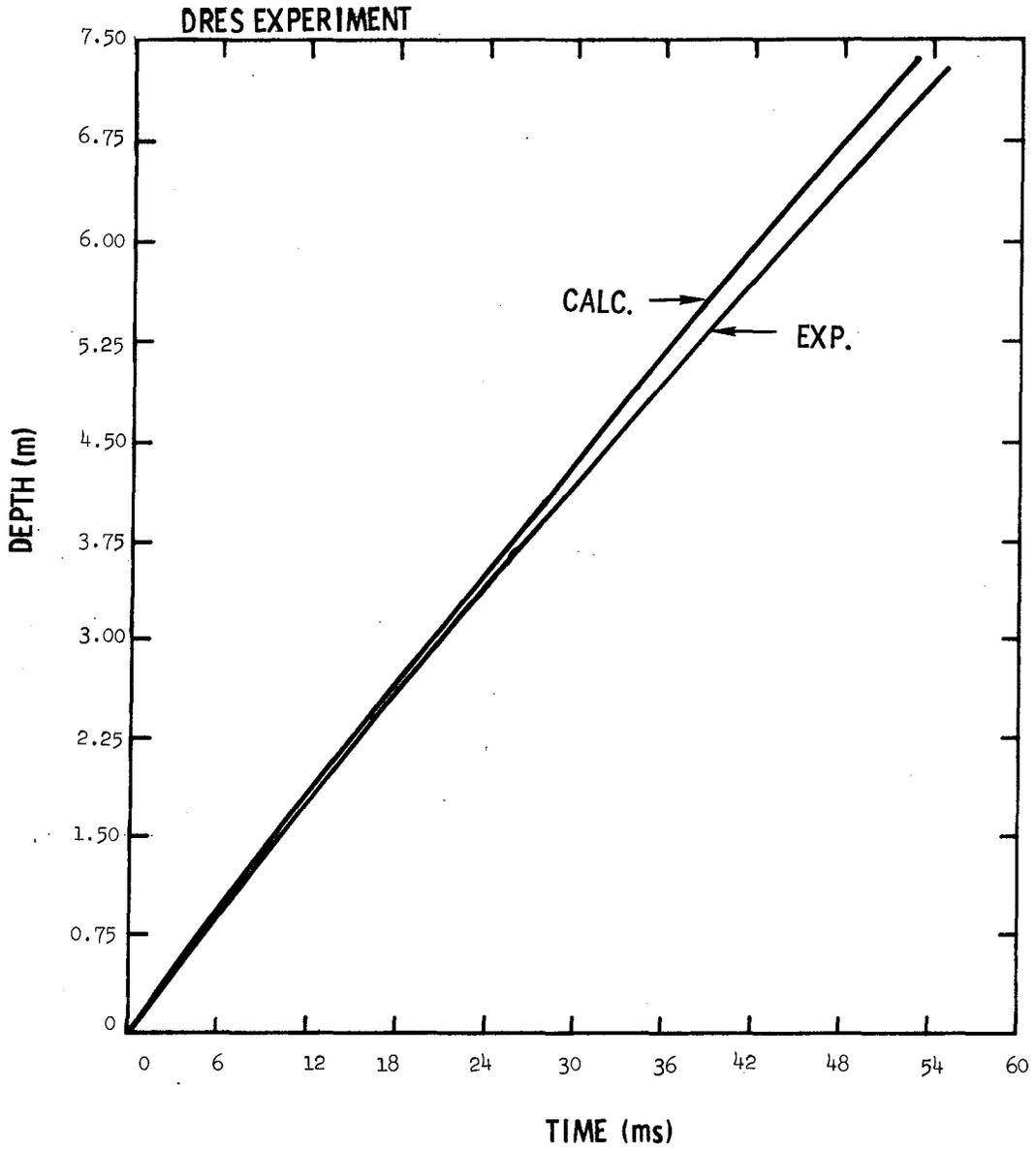


Figure V-6

Comparison of Predicted and Measured Depth versus Time Curves.

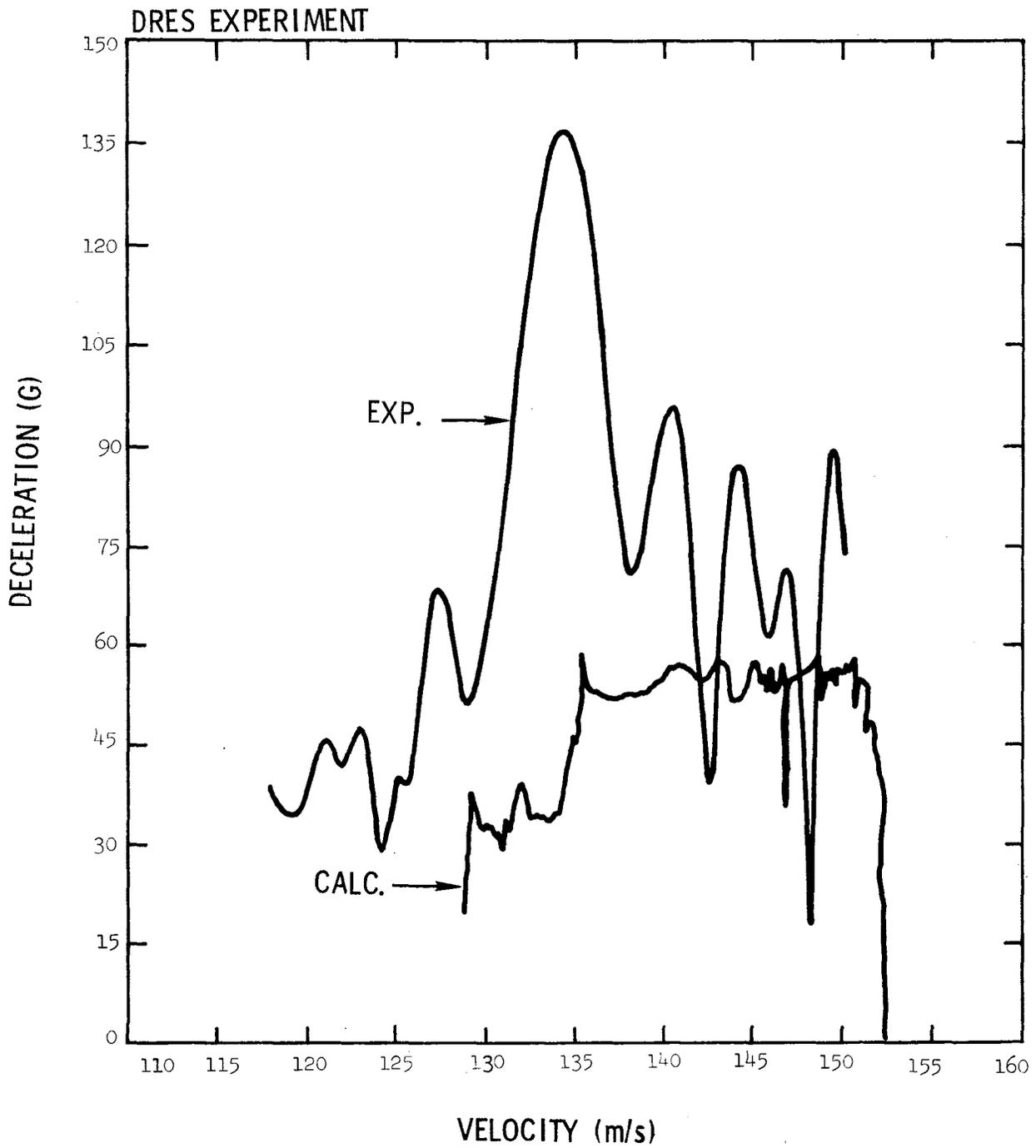


Figure V-7

Projectile Deceleration versus Projectile Velocity, Measured and Predicted.

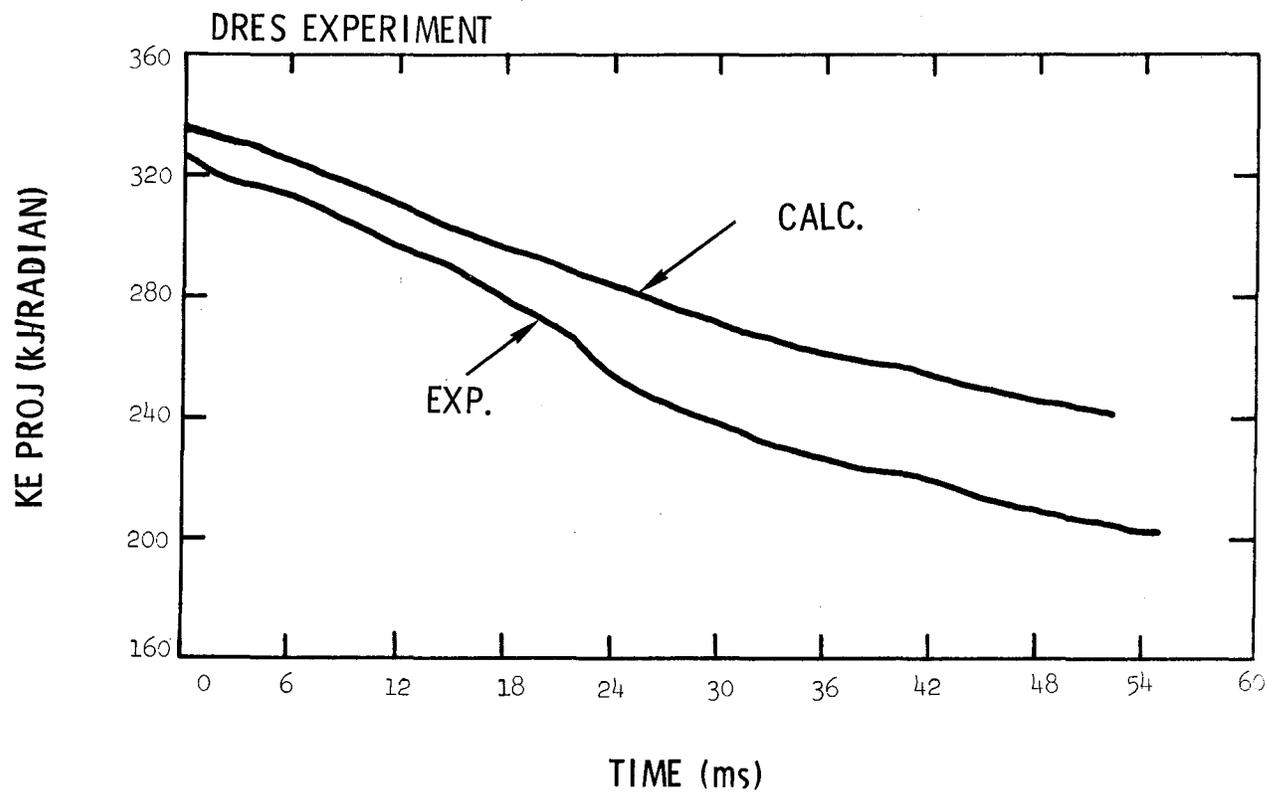


Figure v-8

Projectile Kinetic Energy versus Time, Measured and Predicted.

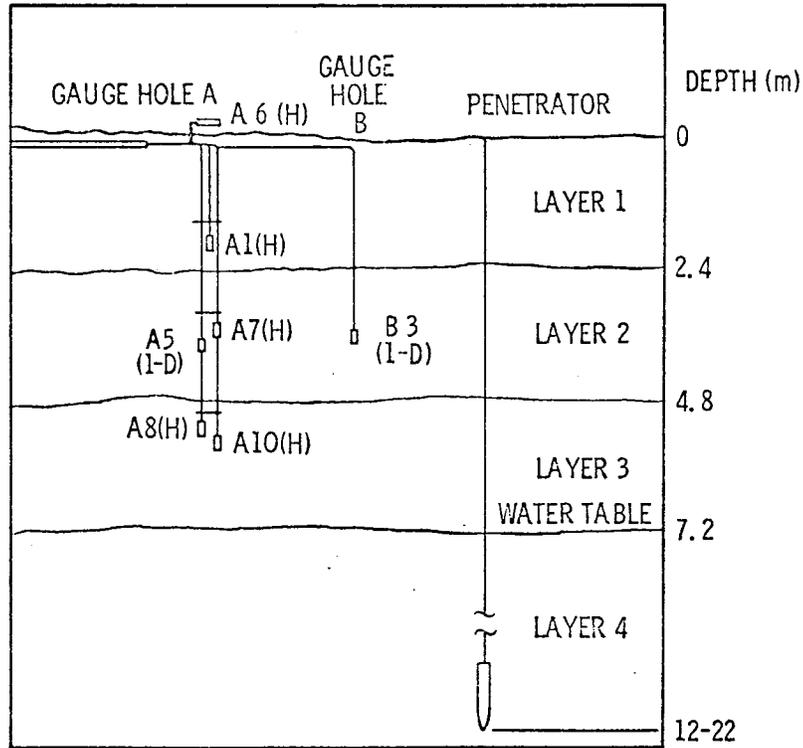


Figure V-9a

Vertical Location of Earth Stress Transducers and Orientation of Stress Gauge Holes Relative to Penetrator Impact Positions.

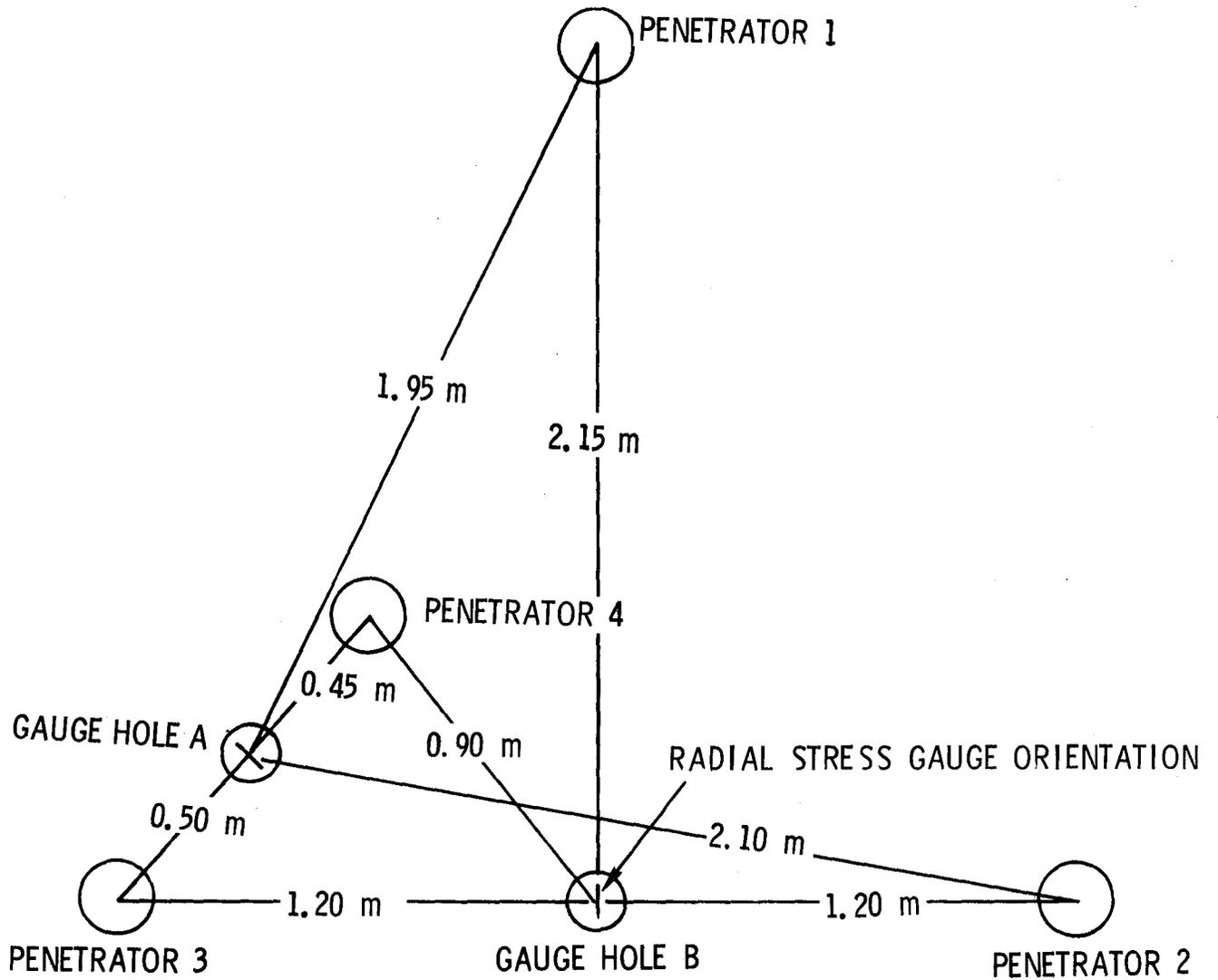


Figure V-9b

Vertical Location of Earth Stress Transducers and Orientation of Stress Gauge Holes Relative to Penetrator Impact Positions.

Table V-3

Characteristics of Projectiles Penetrating  
Medium in Neighborhood of Stress Gauges

| Test No. | Projectile |              | Velocity (m/s) |
|----------|------------|--------------|----------------|
|          | Mass (Kg)  | Diameter (m) |                |
| 1        | 127        | 0.152        | 174            |
| 2        | 181        | 0.165        | 125            |
| 3        | 127        | 0.152        | 122            |
| 4        | 127        | 0.152        | 156            |

No detectable signals were sensed by any stress transducers which were more than 1.2 m horizontal distance from the projectile path. Excellent stress histories were measured for penetrator test number 4. Also, the gauge in hole B measured a signal from penetrator test number 2. Data were obtained from penetrator test number 3 also, but were unfortunately lost during playback of recording tapes.

Measured stress histories are compared with those calculated in Figures V-10 through V-15, where it is seen that amplitudes, pulse shapes and arrival times are all in generally good agreement with predictions. Zero time in Figures V-10 through V-15 is when the projectile is 0.3 m above target surface.<sup>10</sup> Peak values of stresses are summarized in Table V-4 where uncertainties in measured peak stresses associated with base line shift are also tabulated. Error in peak stresses is 11% or less for stress transducers closest to the impact axis (0.45 m). At greater distances from the impact axis, error due to base line shift increases appreciably as the magnitude of the signal goes down. Errors from other possible sources are difficult to estimate. The extent to

Table V-4

| STRESS GAGE         |                  | Depth (m) | Distance From<br>Impact Axis (m) | Penetrator<br>Test No. | Predicted<br>Peak<br>Stress (MPa) | Measured<br>Peak<br>Stress (MPa) | Maximum<br>Base Line<br>Shift (MPa) | Uncertainty<br>In Peak<br>Stress (%) |
|---------------------|------------------|-----------|----------------------------------|------------------------|-----------------------------------|----------------------------------|-------------------------------------|--------------------------------------|
| Number <sup>a</sup> | Type             |           |                                  |                        |                                   |                                  |                                     |                                      |
| A-1                 | Pressure         | 1.83      | 0.45                             | 4                      | 0.25                              | 0.29                             | ~ 0                                 | 0                                    |
| A-7                 | Pressure         | 3.56      | 0.45                             | 4                      | 0.23                              | 0.36                             | 0.04                                | 11                                   |
| A-5                 | Radial<br>Stress | 3.76      | 0.45                             | 4                      | 0.49 <sup>b</sup><br>(0.23)       | 0.33                             | 0.02                                | 6                                    |
| A-8                 | Pressure         | 5.39      | 0.45                             | 4                      | 0.35                              | 0.61                             | 0.04                                | 7                                    |
| A-10                | Pressure         | 5.59      | 0.45                             | 4                      | 0.35                              | 0.37                             | 0.02                                | 5                                    |
| B-3                 | Radial<br>Stress | 3.66      | 0.90                             | 4                      | 0.16 <sup>b</sup><br>(0.064)      | 0.059 <sup>d</sup>               | 0.01                                | 17                                   |
| B-3                 | Radial<br>Stress | 3.66      | 1.20                             | 2                      | 0.019 <sup>b,c</sup><br>(0.0048)  | 0.025                            | 0.01                                | 40                                   |

a) See reference 10

b) Radial stress value, mean stress given in parenthesis below radial stress

c) Radial and mean stress values for 3.6 m depth and 1.5 m range

d) On penetration test, No. 4 gage B-3 was not oriented normal to radial from impact axis.

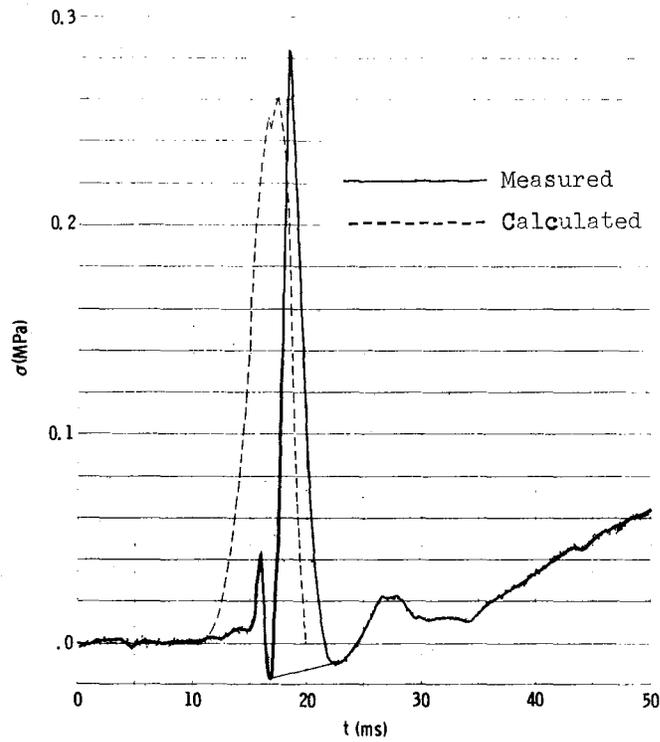


Figure V-10

Mean Stress History Measured at Depth (Z) of 1.83 m and Radius (R) of 0.45 m (Time of Impact = 2 ms).

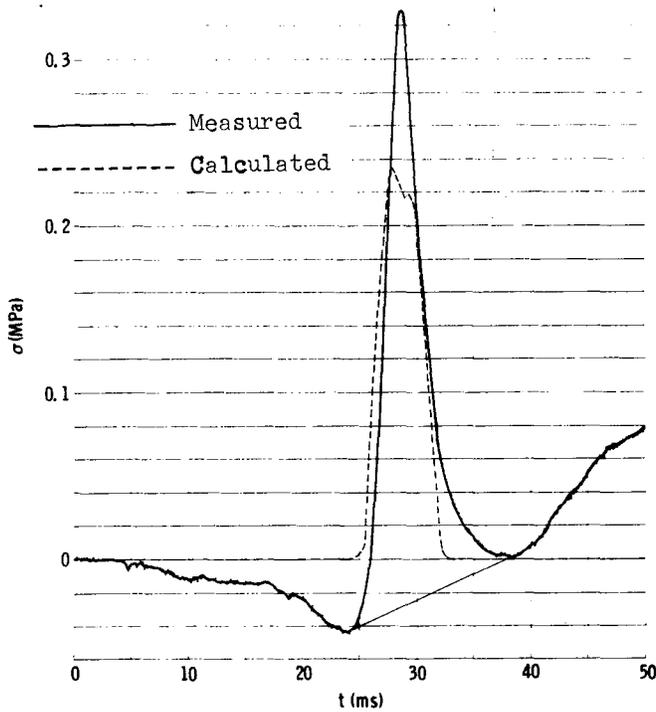


Figure V-11

Mean Stress History Measured at Z = 3.56 m and R = 0.45 m (Time of Impact = 2 ms).

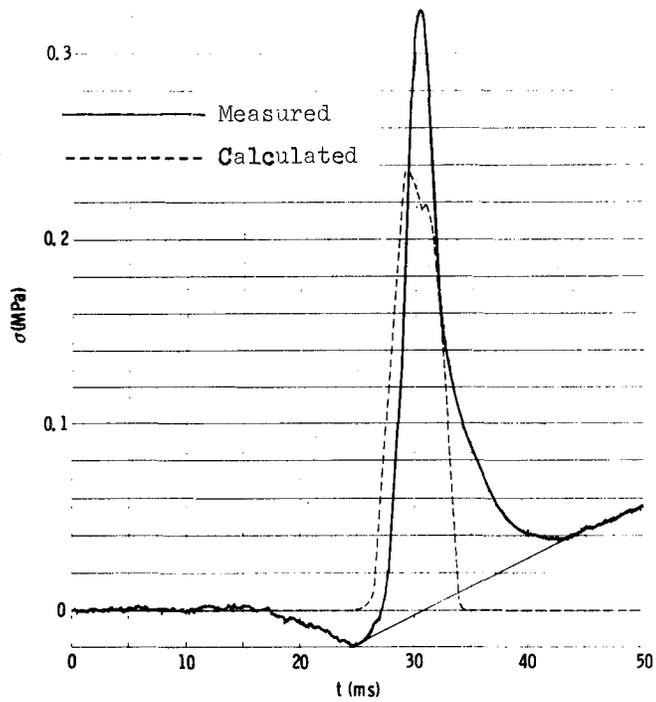


Figure V-12

Radial Stress History Measured at  $Z = 3.76$  m and  $R = 0.45$  m  
(Time of Impact = 2 ms).

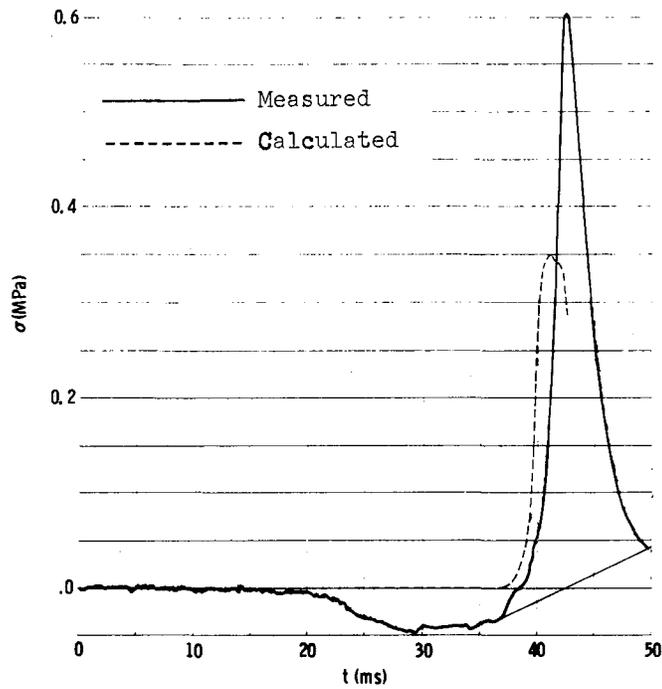


Figure V-13

Mean Stress History Measured at  $Z = 5.39$  m and  $R = 0.45$  m  
(Time of Impact = 2 ms).

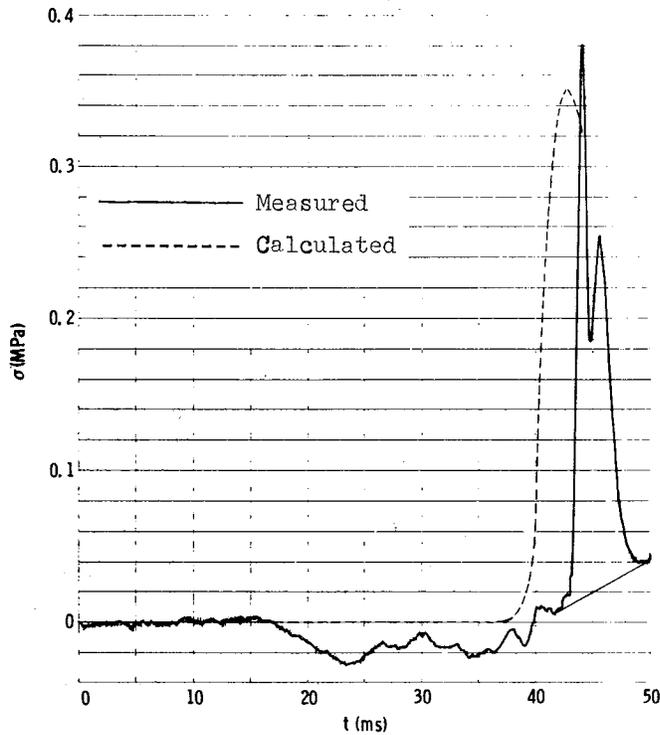


Figure V-14

Mean Stress History Measured at  $Z = 5.59$  m and  $R = 0.45$  m  
(Time of Impact = 2 ms).

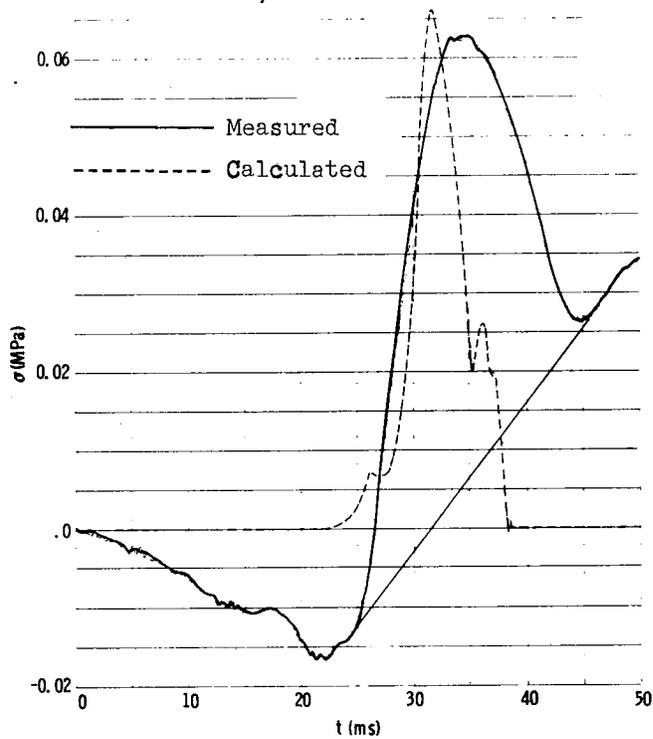


Figure V-15

Radial Stress History Measured at  $Z = 3.66$  m and  $R = 0.90$  m  
(Time of Impact = 2 ms).

which earlier penetration experiments disturb the medium and possibly influence the accuracy of stress history measurements on subsequent experiments cannot be ascertained with available data. The disturbance produced by penetrator test number 3 (Figure V-9b) in terms of calculated peak displacement at the gauge positions amounts to about 10 mm. Further experiments are necessary to evaluate whether or not this magnitude disturbance affects the measurements made on penetrator test number 4. It is clear that penetrator tests numbers 1 and 2 produced relatively much smaller disturbances at the gauges.

Shown in Figure V-16 are peak pressure and radial stress data from gauges in hole A plotted as a function of gauge depth. Also shown are the calculated curves for peak pressure and radial stress. Except for the datum from gauge A-8, all the data fall within a band bounded by the calculated curves. Also, all data are closer to the predicted mean stress curve than to the radial stress curve. The datum at 3.76 m from the radial stress gauge (A-5) appears to be essentially identical to the pressure measurement from gauge A-7 suggesting that both gauges are measuring the same quantity. Lithium niobate transducers for measurement of total stress components are still under development. More work is necessary to establish their capability in this mode. Mean stress gauges of lithium niobate, however, have received much more attention<sup>9</sup> and use<sup>21</sup> and should be considered the more reliable transducer in examination of data from the penetration experiments.

Attenuation of peak pressure and peak radial stress with radial position from impact axis is illustrated in Figure V-17. Predicted curves shown are for stress attenuation at a depth of 3.6 m and may be compared with data at that depth (circle and triangles). It is seen

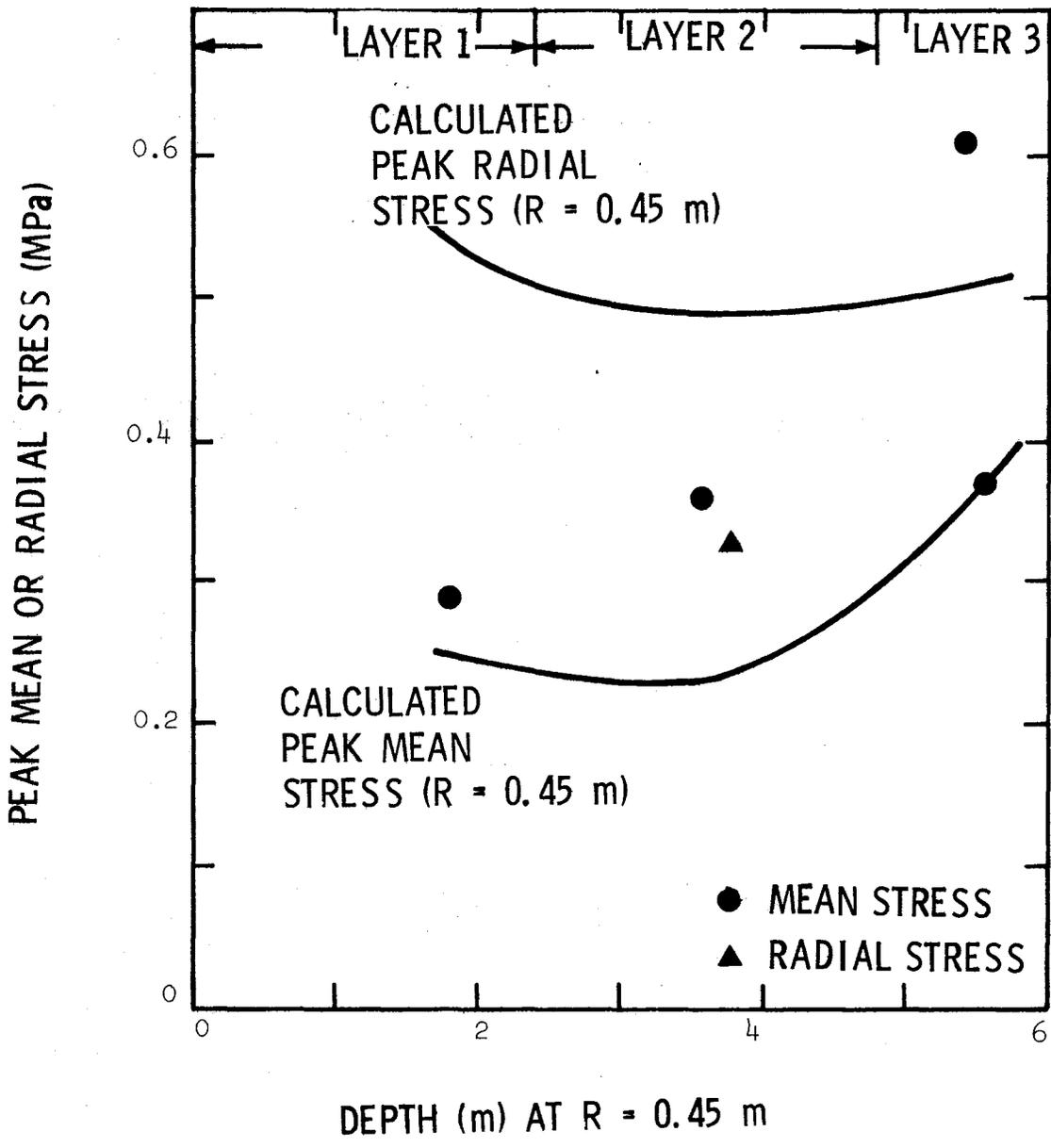


Figure V-16

Predicted Peak Radial and Peak Mean Stress versus Depth at Constant Radial Position  $R = 0.45$  Compared with Measurements.

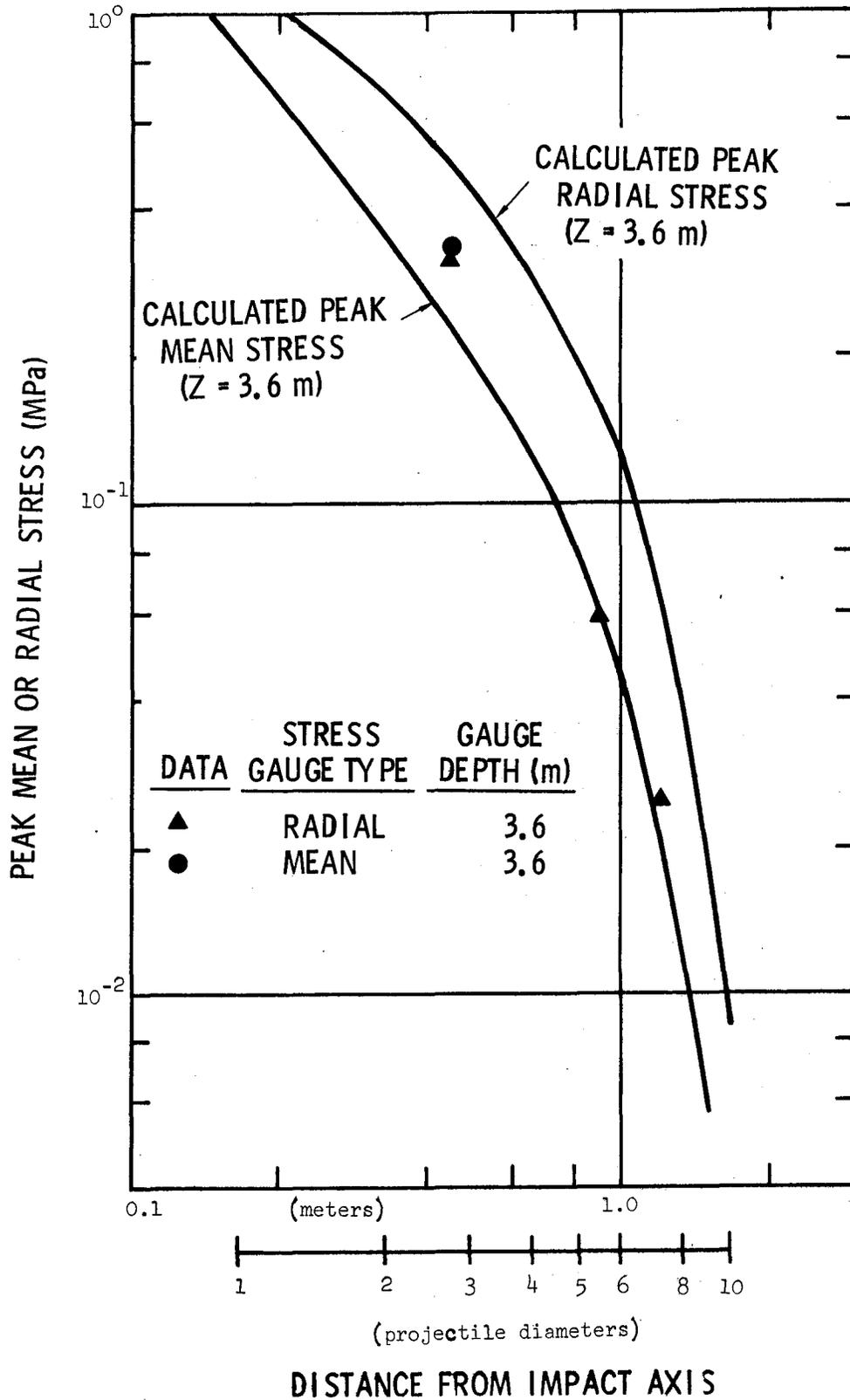


Figure V-17

Predicted Peak Radial and Peak Mean Stress versus Distance from Impact Axis at Constant Depth  $Z = 3.6$  m Compared with Measurements.

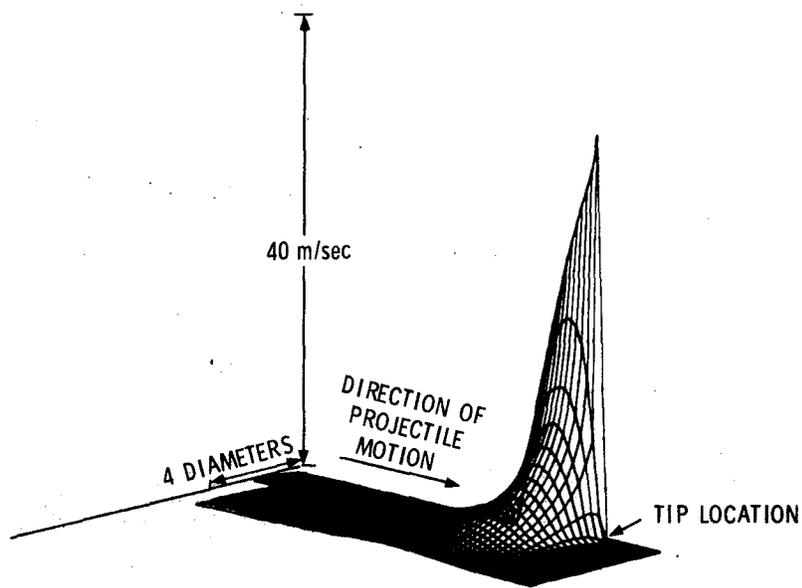
that the 3.6 m data compare reasonably well with the predicted mean stress attenuation curve and that peak stress amplitude falls off rapidly (faster than  $r^{-2}$ ) with distance away from the projectile path axis.

In general, it is felt that the soil stress measurement technique has been demonstrated and that the information obtained provides confidence regarding validity of the material property data and material response models used in calculations for layers 1, 2 and 3. The satisfactory agreement between measurement and calculation of stress pulse shape and amplitude also verifies methods employed in the computational technique. Without the earth stress data much less credibility might have been attached to results of computations. Penetration tests (numbers 2 and 4), which provided the earth stress history data were conducted with projectiles of 127 kg mass and diameter 0.152 m rather than the 181 kg, 0.165 m diameter projectiles assumed in calculations. While another calculation would be required for the slightly smaller projectile in order to definitely establish differences, it is felt that stress history results for the smaller projectile would be similar to those of the larger projectile within the uncertainties that exist.

## SECTION VI

### SUMMARY AND CONCLUSIONS

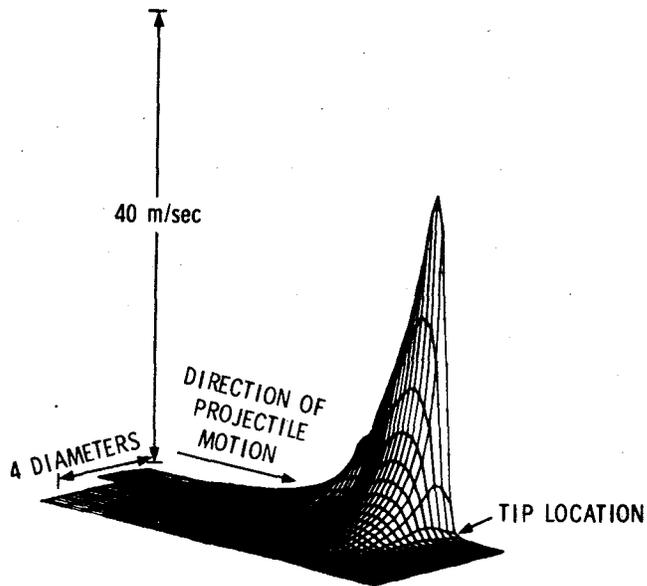
All phenomena connected with producing significant loads on the projectile occur in a relatively small region of the target medium about the projectile nose. Shown in Figure VI-1 are three-dimensional plots of radial and vertical soil velocity as a function of depth in target and distance from projectile path axis at a time when the projectile nose is at 4.4 m depth (see also Figures A-122 and A-123). It is seen that the region of greatest disturbance in the soil is small and confined to the immediate vicinity of the nose. Figure VI-2a also illustrates how rapidly the disturbance in soil vanishes with distance from the projectile. With the projectile nose tip at 4.4 m, at a depth of 4.2 m (0.2 m behind projectile nose) soil pressure is about 3 MPa (30 bars, 450 psi) at a distance of slightly less than one projectile radius from the projectile axis. At a distance 2.5 projectile diameters from the axis, the soil pressure is down an order of magnitude to 0.3 MPa and at 5 projectile diameters another order of magnitude reduction is found. Figure VI-2b indicates in yet another way the highly isolated nature of the projectile generated disturbance in the soil. For the zones of the computational mesh originally on the symmetry axis and later adjacent to the penetrator, mean stress is plotted as a function of vertical position relative to nose tip location. The pressure profile ahead of and along the projectile surface is shown in Figure VI-2b for the penetrator in layer 1 (nose tip at 2 m depth) and in layer 2 (4.4 m depth). For materials similar to those of the Watching Hill target medium, it is



**RADIAL VELOCITY**

Figure VI-1a

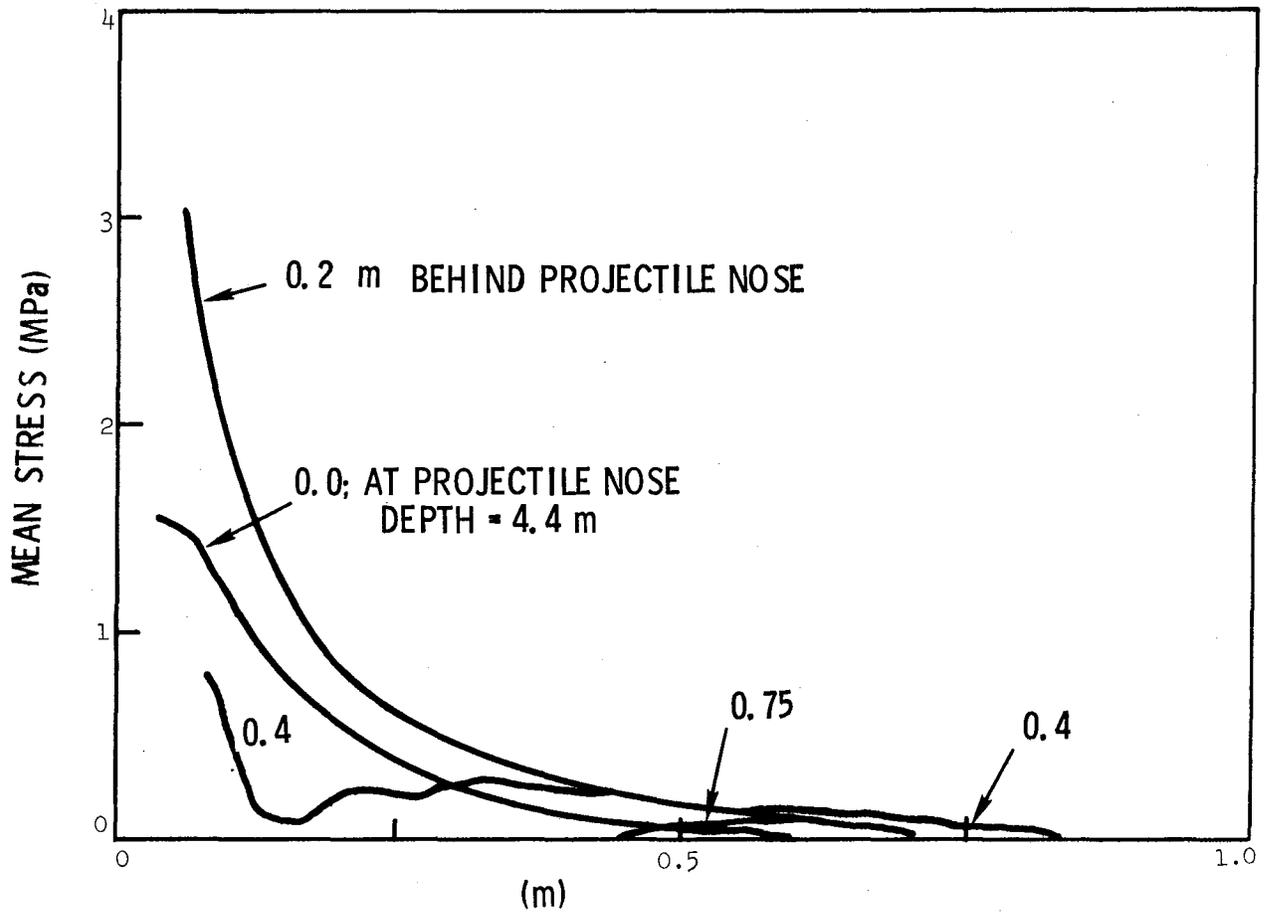
Radial Velocity (a) and Vertical Velocity, (b) in Soil as a Function of Depth and Distance from Impact Axis when Projectile is at 4.4 m Depth.



**VERTICAL VELOCITY**

Figure VI-1b

Radial Velocity (a) and Vertical Velocity, (b) in Soil as a Function of Depth and Distance from Impact Axis when Projectile is at 4.4 m Depth.



PROJECTILE DIAMETERS

RADIAL DISTANCE FROM PROJECTILE AXIS

Figure VI-2a

(a) Decay of Mean Stress in Soil with Radial Distance from Projectile at Time when Projectile is at 4.4 m Depth.

p vs. Z NEXT TO PROJECTILE

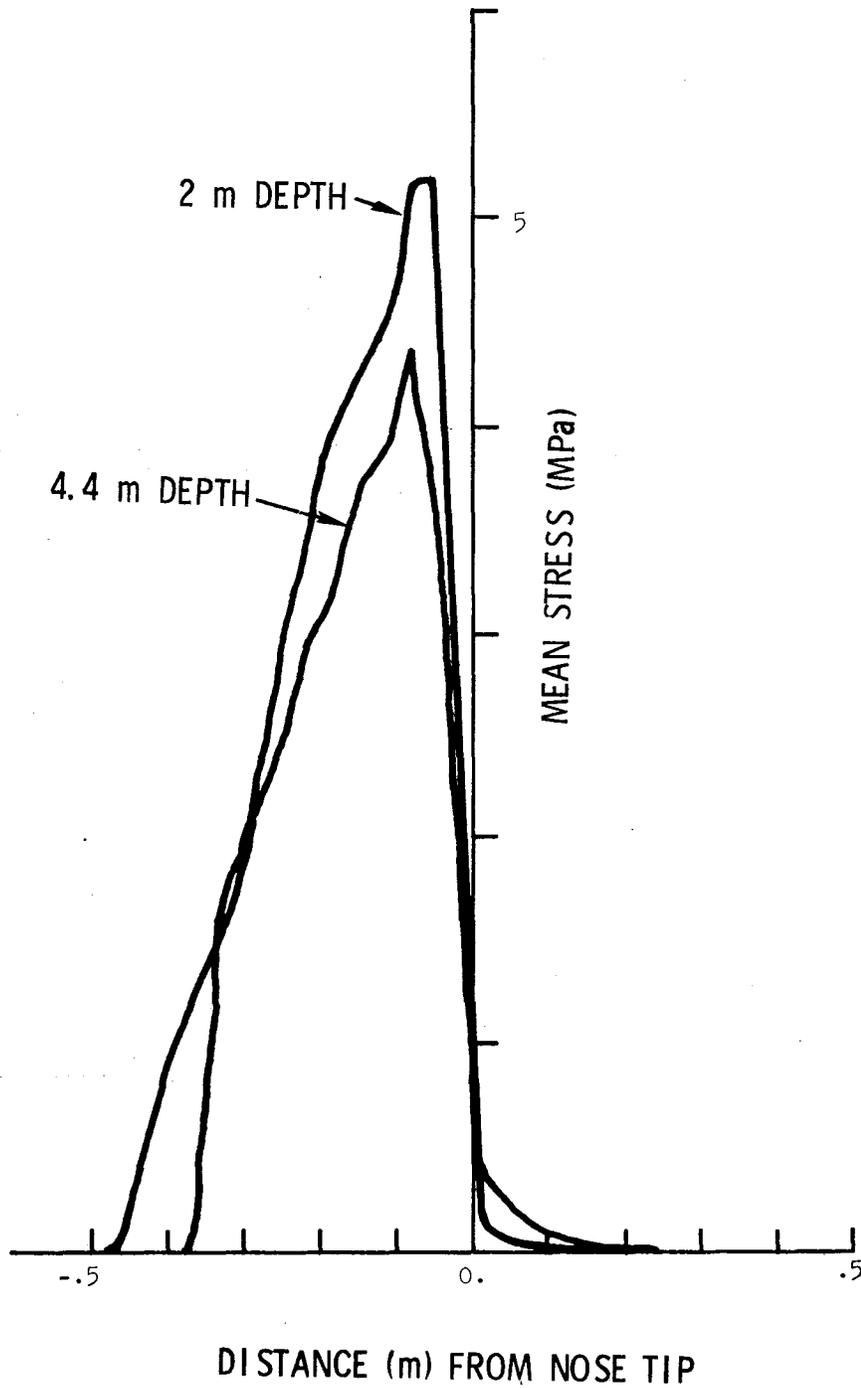
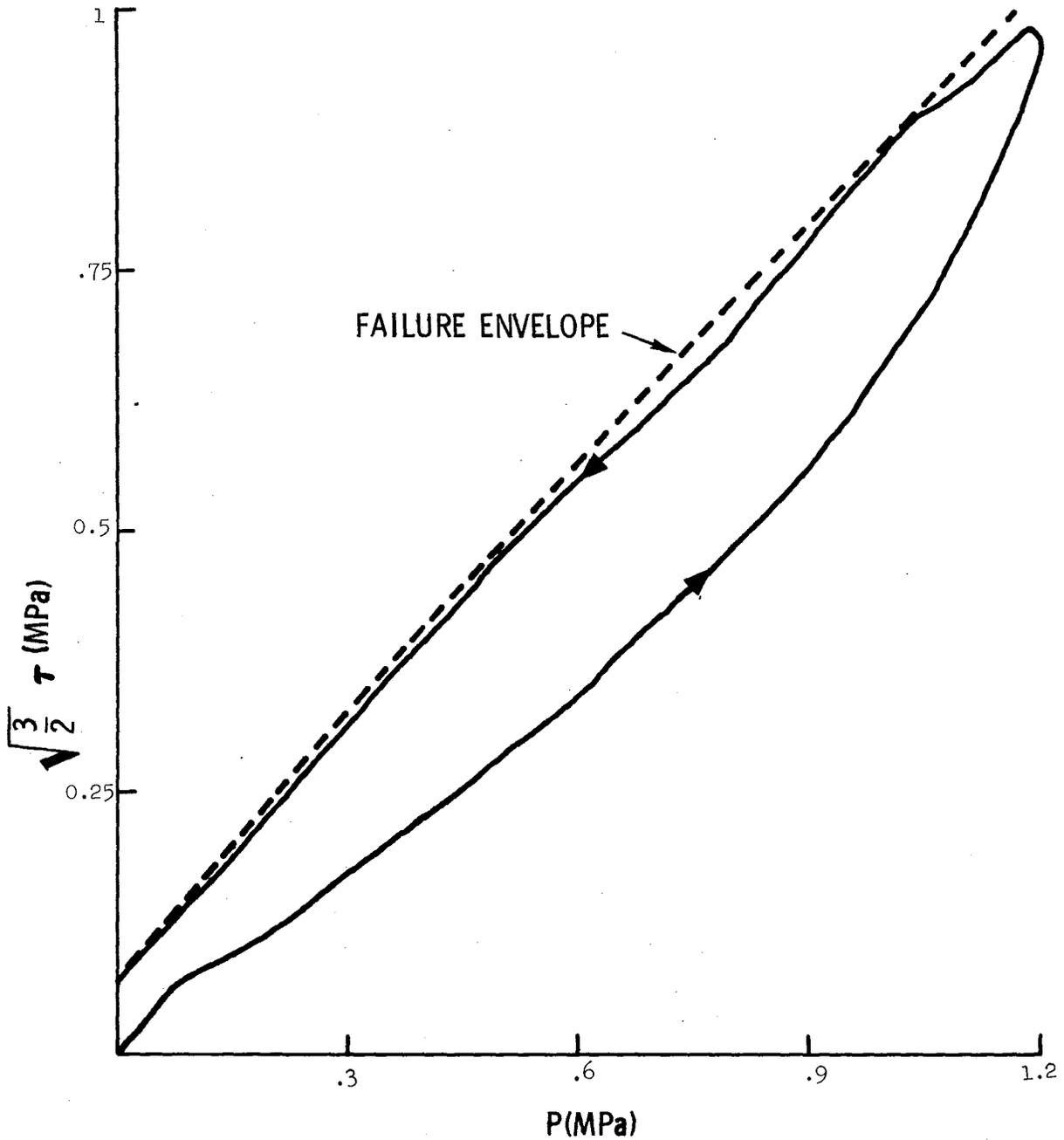


Figure VI-2b  
(b) Mean Stress in Soil versus Depth Next to Projectile at Projectile Depths of 2 and 4.4 m.

seen that essentially all of the disturbance produced in the soil occurs within a cylindrical volume with radius equal to 3 projectile diameters. For purposes of calculating loads on penetrators, radial extent of the target need not be more than about 5 penetrator diameters in materials like those of this calculation.

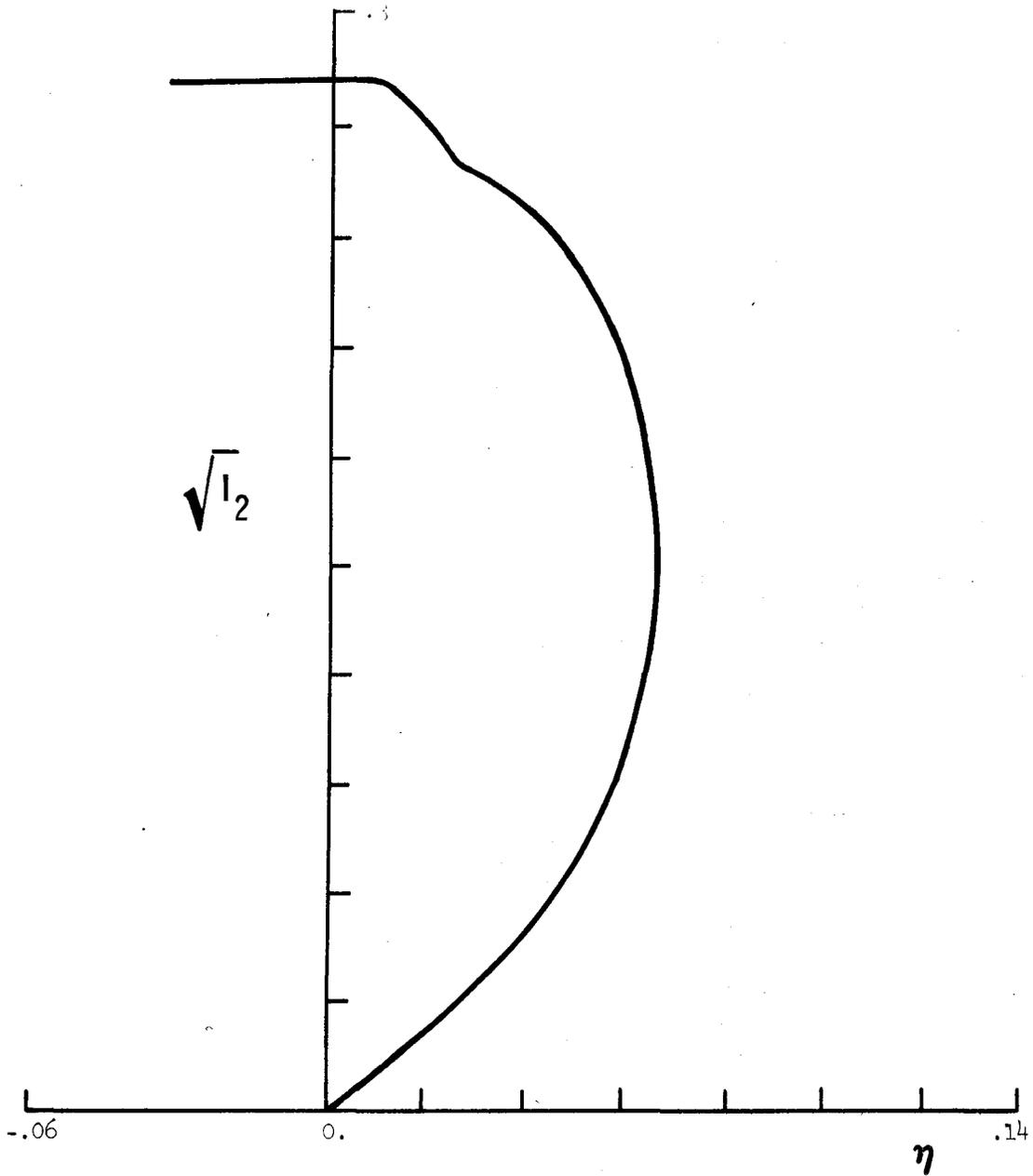
Figure VI-3 shows the path a soil particle follows in the stress plane,  $\sqrt{\frac{3}{2}} \tau$  vs.  $p$ . The particle of Figure VI-3 is identified by its initial coordinates  $Z = 3.6$  m,  $R = 0.15$  m and so is located in layer 2 material at a distance less than one projectile diameter from the impact axis. During loading the particle follows the path shown. On unloading the particle finds itself very close to the failure envelope and follows it to zero pressure. A close examination of the calculation reveals that the stress state for the particle should actually be at the intersection of the cap and the failure envelope: the fact that it does not quite coincide with this point is a consequence of a slight "over-shrinking" of the cap caused by the finite difference approximation used for the constitutive equations. Figures VI-2b and VI-3 taken together indicate that accurate modeling of the failure envelope and unloading behavior for the material are important parts of the calculation. Similarly, Figure VI-4 illustrates the path of the same soil particle in the strain invariant plane,  $\sqrt{I_2}$  vs.  $\eta$ , where  $I_2$  is the second moment of the strain deviators and  $\eta$  is volumetric strain. After unloading, the particle finds itself with a large deviatoric strain and at a density less than its initial density. These paths experienced by soil particles as a result of target penetration by projectiles are considerably different from paths attained in conventional uniaxial strain and triaxial stress experiments. Strain energy density of a particle within the region of



**STRESS PATH FOR A PARTICLE AT Z = 3.6 m, R = 0.15 m**

Figure VI-3

Stress Path, During Projectile Penetration, for a Soil Particle at  
Z = 3.6 m, R = 0.15 m in Shear Stress-Pressure Space.



POINT 3:  $\sqrt{I_2}$  vs.  $\eta$

$$(I_2 = E'_{ij} E'_{ij})$$

Figure VI-4

Strain Path, During Projectile Penetration, for a Soil Particle  
at  $Z = 3.6$  m,  $R = 0.15$  m.

soil highly disturbed by the projectile is of the order of 0.1 to 0.5 MJ/m<sup>3</sup> for the Watching Hill medium. Consequences of the dilatancy inherent in the soil cap model, as indicated in Figure VI-4, appear to be manifested in two ways. These are lack of a definitive soil separation point on the projectile and the size of the projectile-produced borehole. Results of the rigid body calculation indicate that the diameter of the borehole is never greater than the projectile diameter and may in fact be less. Accurate determination of borehole diameter behind the projectile is not possible owing to the continual rezoning to a coarser mesh in this region. It is known, however, that soil rebound occurs and boreholes have been observed<sup>22</sup> whose final diameters are less than the projectile diameter. Unfortunately, no attempt was made to measure borehole sizes for the penetrator experiments at Watching Hill. The rigid body calculations also suggest that the Watching Hill soil does not separate from the projectile but appears to remain attached throughout the entire length of the projectile. This occurs even though the normal stress on the projectile is significantly larger than zero only on the nose. (What appears to be a soil separation position in Figures A-97, A-106, A-115, A-124 and A-133 is interpreted, rather, to be a perturbation in the calculation resulting from the transition from a region of fine to coarser zoning). That soil separation or detachment from the projectile may not occur has been observed<sup>22</sup> experimentally. Those experimental results, however, cannot distinguish between soil detachment on the projectile nose with later reattachment and complete lack of soil separation.

To investigate this point further, additional calculations should be performed which include friction and a response model such as the cap model which demonstrates dilatancy. As appears to be the case here

in calculations with no friction, dilatancy in the response model prevents or retards soil detachment from the projectile surface. By the inclusion of friction in such calculations even a small frictional stress, acting over the large area of the projectile afterbody, could contribute a large axial retarding force comparable to or possibly greater than that contributed by the nose area of the projectile. Results from such a calculation, when compared with projectile deceleration data, would imply a smaller friction coefficient than one inferred from calculations with response models having no dilatancy in which soil separation might occur, for example, at the position on the projectile where the nose meets the afterbody.

Figure VI-5 illustrates the partitioning of energy to the penetrated medium at the expense of projectile kinetic energy. From the zero friction calculation, it is apparent that projectile kinetic energy losses manifest themselves primarily in the form of plastic work done in deformation of the penetrated medium. Energies associated with motion of the soil and with recoverable elastic work are very small, each being on the order of 1/10 or less of the plastic work (internal energy = plastic work + elastic work).

The calculated deceleration history indicates that sudden changes in the problem occur only when the nose region of the projectile is entering a new layer of material. Also, Figure VI-5 shows that the dominant mode of the rate of energy transfer from projectile to soil is nearly constant through a layer in which there is little velocity change. Moving pictures made of numerous plots of normal stress distribution and three-dimensional plots of pressure vs. axial and radial position, for example, confirm that the process being calculated is primarily quasi-static. Thus, the

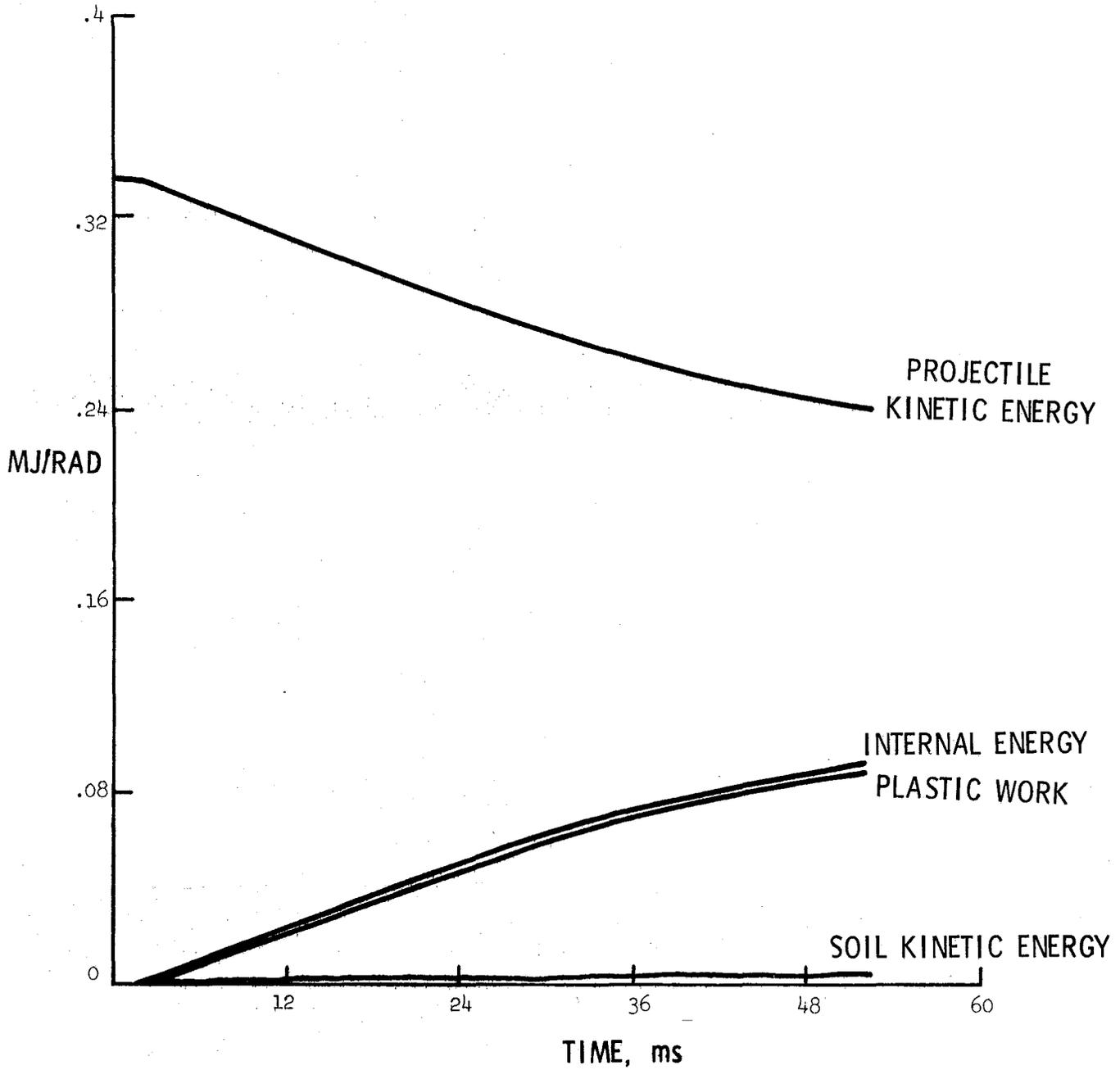


Figure VI-5  
 Projectile Kinetic Energy, Soil Kinetic Energy, Soil Plastic Work and Soil Internal Energy versus Time.

method of "skipping" through layers, and calculating only transition periods, as employed by California Research and Technology,<sup>20</sup> appears to be a useful means of performing deep penetration calculations with large-scale wave propagation codes with a reasonable degree of economy although it may be necessary to perform multiple calculations in layers that produce large velocity decreases. It also appears, however, that detailed analysis of the results of this and similar calculations should lead to the development of much less sophisticated methods which would also yield necessary information for depth prediction and projectile design.

During the deformable projectile calculation, the maximum radial displacement that was observed for the projectile surface was 30  $\mu\text{m}$ . Although this displacement was too small to alter the effective shape of the vehicle, fluctuations in displacement were sufficient to produce large changes in normal stress at the vehicle-soil interface, as shown in Figures B-37 through B-39. Thus, the dominant effect of the rigid-body approximation was to eliminate transient variations in the normal stress.

The agreement in predicted soil histories between the two calculations demonstrates that, for the particular material model used, these transients are damped out less than 20 mm from the vehicle and do not affect the predicted wave motion in the soil. However, the deformable body calculation predicts a deceleration about forty percent larger than that calculated for a rigid body. This comparison demonstrates that the deceleration is determined by the soil response in regions much closer to the vehicle than the locations at which stress measurements were made. The motion is similar to aerodynamic behavior, with the drag determined by the response in a narrow region, or boundary layer.

The differences between the results of the two calculations are related to their description of this boundary layer. The inclusion of the 45° nose tip results in a 5 MPa increase in stress, effective over a cross-sectional area of about  $4 \times 10^{-4} \text{ m}^2$ , accounting for a deceleration difference of about 1 g. Of greater significance is the procedure for obtaining the stress at the interface. In the calculations, stress histories are recorded only at zone centers and, therefore, not at the interface. For the rigid body calculation, the stress in the nearest soil zone was used to determine the decelerating force, as discussed in Section III. In the deformable body calculation, no interface stress or force was explicitly obtained; the sliding interface procedure results in an effective normal stress that is between the stress in the soil zone and the (usually higher) stress in the nearest vehicle zone.

While many questions remain to be investigated, this first attempt to predict projectile motion and target material response has been highly successful and most encouraging. Given data describing properties of each layer in the target medium, realistic soil response models were constructed and utilized in the finite difference code computations. Resulting predictions of projectile deceleration and of stress history at several points in the soil generally agreed well with measurements, lending credence to the method of analysis. Consequently greater confidence may now be placed in prediction of nonmeasurable quantities, such as normal stress distribution on projectile surface, which are necessary for design of earth penetrating projectiles.

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APPENDIX A

## List of Illustrations Appendix A

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- Figure A-24 Deviator Stress, J2, History (Pa) for Particle at Point 4,  
Z = 0.4 m, R = 0.15 m (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).
- Figure A-25 Radial Velocity (m/s) versus Time (s) for Particle at Point 5,  
Z = 0.1 m, R = 0.15 m.
- Figure A-26 Axial Velocity (m/s) versus Time (s) for Particle at Point 5,  
Z = 0.1 m, R = 0.15 m.
- Figure A-27 Radial Displacement (m) versus Time (s) for Particle at Point 5,  
Z = 0.1 m, R = 0.15 m.
- Figure A-28 Axial Displacement (m) versus Time (s) for Particle at Point 5,  
Z = 0.1 m, R = 0.15 m.
- Figure A-29 Pressure (Pa) versus Time (s) for Particle at Point 5, Z = 0.1 m,  
R = 0.15 m.
- Figure A-30 Deviator Stress, J2, History (Pa) for Particle at Point 5,  
Z = 0.1 m, R = 0.15 m (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).
- Figure A-31 Radial Velocity (m/s) versus Time (s) for Particle at Point 7,  
Z = 5.4 m, R = 0.45 m.

- Figure A-32 Axial Velocity (m/s) versus Time (s) for Particle at Point 7,  
Z = 5.4 m, R = 0.45 m.
- Figure A-33 Radial Displacement (m) versus Time (s) for Particle at Point 7,  
Z = 5.4 m, R = 0.45 m.
- Figure A-34 Axial Displacement (m) versus Time (s) for Particle at Point 7,  
Z = 5.4 m, R = 0.45 m.
- Figure A-35 Pressure (Pa) versus Time (s) for Particle at Point 7, Z = 5.4 m,  
R = 0.45 m.
- Figure A-36 Deviator Stress, J2, History (Pa) for Particle at Point 7,  
Z = 5.4 m, R = 0.45 m (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).
- Figure A-37 Radial Stress (Pa) History for Particle at Point 7, Z = 5.4 m,  
R = 0.45 m.
- Figure A-38 Radial Velocity (m/s) versus Time (s) for Particle at Point 8,  
Z = 3.6 m, R = 0.45 m.
- Figure A-39 Axial Velocity (m/s) versus Time (s) for Particle at Point 8,  
Z = 3.6 m, R = 0.45 m.
- Figure A-40 Radial Displacement (m) versus Time (s) for Particle at Point 8,  
Z = 3.6 m, R = 0.45 m.
- Figure A-41 Axial Displacement (m) versus Time (s) for Particle at Point 8,  
Z = 3.6 m, R = 0.45 m.
- Figure A-42 Pressure (Pa) versus Time (s) for Particle at Point 8, Z = 3.6 m,  
R = 0.45 m.
- Figure A-43 Deviator Stress, J2, History (Pa) for Particle at Point 8,  
Z = 3.6 m, R = 0.45 m (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).
- Figure A-44 Radial Stress (Pa) History for Particle at Point 8, Z = 3.6 m,  
R = 0.45 m.

- Figure A-45 Axial Stress (Pa) History for Particle at Point 8,  $Z = 3.6$  m,  
 $R = 0.45$  m.
- Figure A-46 Radial Velocity (m/s) versus Time (s) for Particle at Point 9,  
 $Z = 1.8$  m,  $R = 0.45$  m.
- Figure A-47 Axial Velocity (m/s) versus Time (s) for Particle at Point 9,  
 $Z = 1.8$  m,  $R = 0.45$  m.
- Figure A-48 Radial Displacement (m) versus Time (s) for Particle at Point 9,  
 $Z = 1.8$  m,  $R = 0.45$  m.
- Figure A-49 Axial Displacement (m) versus Time (s) for Particle at Point 9,  
 $Z = 1.8$  m,  $R = 0.45$  m.
- Figure A-50 Pressure (Pa) versus Time (s) for Particle at Point 9,  $Z = 1.8$  m,  
 $R = 0.45$  m.
- Figure A-51 Deviator Stress,  $J_2$ , History (Pa) for Particle at Point 9,  
 $Z = 1.8$  m,  $R = 0.45$  m (Octahedral Shear Stress  $=\sqrt{2/3}(J_2)$ ).
- Figure A-52 Radial Stress (Pa) History for Particle at Point 9,  $Z = 1.8$  m,  
 $R = 0.45$  m.
- Figure A-53 Radial Velocity (m/s) versus Time (s) for Particle at Point 10,  
 $Z = 0.4$  m,  $R = 0.45$  m.
- Figure A-54 Axial Velocity (m/s) versus Time (s) for Particle at Point 10,  
 $Z = 0.4$  m,  $R = 0.45$  m.
- Figure A-55 Radial Displacement (m) versus Time (s) for Particle at Point 10,  
 $Z = 0.4$  m,  $R = 0.45$  m.
- Figure A-56 Axial Displacement (m) versus Time (s) for Particle at Point 10,  
 $Z = 0.4$  m,  $R = 0.45$  m.
- Figure A-57 Pressure (Pa) versus Time (s) for Particle at Point 10,  
 $Z = 0.4$  m,  $R = 0.45$  m.

- Figure A-58 Deviator Stress,  $J_2$ , History (Pa) for Particle at Point 10,  $Z = 0.4$  m,  $R = 0.45$  m (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).
- Figure A-59 Radial Velocity (m/s) versus Time (s) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m.
- Figure A-60 Axial Velocity (m/s) versus Time (s) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m.
- Figure A-61 Radial Displacement (m) versus Time (s) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m.
- Figure A-62 Axial Displacement (m) versus Time (s) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m.
- Figure A-63 Pressure (Pa) versus Time (s) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m.
- Figure A-64 Deviator Stress,  $J_2$ , History (Pa) for Particle at Point 11,  $Z = 0.1$  m,  $R = 0.45$  m (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).
- Figure A-65 Radial Velocity (m/s) versus Time (s) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m.
- Figure A-66 Axial Velocity (m/s) versus Time (s) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m.
- Figure A-67 Radial Displacement (m) versus Time (s) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m.
- Figure A-68 Axial Displacement (m) versus Time (s) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m.
- Figure A-69 Pressure (Pa) versus Time (s) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m.
- Figure A-70 Deviator Stress,  $J_2$ , History (Pa) for Particle at Point 12,  $Z = 3.6$  m,  $R = 0.9$  m (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).

- Figure A-71 Radial Stress (Pa) History for Particle at Point 12,  $Z = 3.6$  m,  
 $R = 0.9$  m.
- Figure A-72 Axial Stress (Pa) History for Particle at Point 12,  $Z = 3.6$  m,  
 $R = 0.9$  m.
- Figure A-73 Pressure (Pa) versus Time (s) for Particle at Point 13,  
 $Z = 5.4$  m,  $R = 1.5$  m.
- Figure A-74 Radial Stress (Pa) History for Particle at Point 13,  $Z = 5.4$  m,  
 $R = 1.5$  m.
- Figure A-75 Pressure (Pa) versus Time (s) for Particle at Point 14,  $Z = 3.6$  m,  
 $R = 1.5$  m.
- Figure A-76 Radial Stress (Pa) History for Particle at Point 14,  $Z = 3.6$  m,  
 $R = 1.5$  m.
- Figure A-77 Pressure (Pa) versus Time (s) for Particle at Point 15,  $Z = 1.8$  m,  
 $R = 1.5$  m.
- Figure A-78 Radial Stress (Pa) History for Particle at Point 15,  $Z = 1.8$  m,  
 $R = 1.5$  m.
- Figure A-79 Lagrangian coordinates when projectile has penetrated to depth  
of 0.1 m.
- Figure A-80 Normal stress (Pa) along surface of projectile when projectile  
is at 0.1 m depth.
- Figure A-81 Tangential stress (Pa) along surface of projectile when projectile  
is at 0.1 m depth.
- Figure A-82 Contours of Axial Stress in Target. Projectile at 0.1 m Depth.
- Figure A-83 Contours of Radial Stress in Target. Projectile at 0.1 m Depth.
- Figure A-84 Contours of Hoop Stress in Target. Projectile at 0.1 m Depth.

- Figure A-85 Contours of Radial-Vertical Shear Stress in Target. Projectile at 0.1 m Depth
- Figure A-86 Contours of Vertical Velocity in Target. Projectile at 0.1 m Depth.
- Figure A-87 Contours of Radial Velocity in Target. Projectile at 0.1 m Depth.
- Figure A-88 Lagrangian Coordinates When Projectile has Penetrated to Depth of 0.4 m.
- Figure A-89 Normal Stress (Pa) Along Surface of Projectile When Projectile is at 0.4 m Depth.
- Figure A-90 Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 0.4 m Depth.
- Figure A-91 Contours of Axial Stress in Target. Projectile at 0.4 m Depth.
- Figure A-92 Contours of Radial Stress in Target. Projectile at 0.4 m Depth.
- Figure A-93 Contours of Hoop Stress in Target. Projectile at 0.4 m Depth.
- Figure A-94 Contours of Radial-Vertical Shear Stress in Target. Projectile at 0.4 m Depth.
- Figure A-95 Contours of Vertical Velocity in Target. Projectile at 0.4 m Depth.
- Figure A-96 Contours of Radial Velocity in Target. Projectile at 0.4 m Depth.
- Figure A-97 Lagrangian Coordinates When Projectile has Penetrated to Depth of 2.0 m. Radial Dimensions Doubled for Clarity.
- Figure A-98 Normal Stress (Pa) along Surface of Projectile When Projectile is at 2.0 m Depth.
- Figure A-99 Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 2.0 m Depth.
- Figure A-100 Contours of Axial Stress in Target. Projectile at 2.0 m Depth.
- Figure A-101 Contours of Radial Stress in Target. Projectile at 2.0 m Depth.
- Figure A-102 Contours of Hoop Stress in Target. Projectile at 2.0 m Depth.

- Figure A-103 Contours of Radial Vertical Shear Stress in Target. Projectile at 2.0 m Depth.
- Figure A-104 Contours of Vertical Velocity in Target. Projectile at 2.0 m Depth.
- Figure A-105 Contours of Radial Velocity in Target. Projectile at 2.0 m Depth.
- Figure A-106 Lagrangian Coordinates When Projectile has Penetrated to Depth of 2.8 m. Radial Dimensions Doubled for Clarity.
- Figure A-107 Normal Stress (Pa) Along Surface of Projectile When Projectile is at 2.8 m Depth.
- Figure A-108 Tangential Stress (Pa) Along Surface of Projectile when Projectile is at 2.8 m Depth.
- Figure A-109 Contours of Axial Stress in Target. Projectile at 2.8 m Depth.
- Figure A-110 Contours of Radial Stress in Target. Projectile at 2.8 m Depth.
- Figure A-111 Contours of Hoop Stress in Target. Projectile at 2.8 m Depth.
- Figure A-112 Contours of Radial Vertical Shear Stress in Target. Projectile at 2.8 m Depth.
- Figure A-113 Contours of Vertical Velocity in Target. Projectile at 2.8 m Depth.
- Figure A-114 Contours of Radial Velocity in Target. Projectile at 2.8 m Depth.
- Figure A-115 Lagrangian Coordinates When Projectile has Penetrated to Depth of 4.4 m. Radial Dimensions Doubled for Clarity.
- Figure A-116 Normal Stress (Pa) Along Surface of Projectile When Projectile is at 4.4 m Depth.
- Figure A-117 Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 4.4 m Depth.
- Figure A-118 Contours of Axial Stress in Target. Projectile at 4.4 m Depth.
- Figure A-119 Contours of Radial Stress in Target. Projectile at 4.4 m Depth.
- Figure A-120 Contours of Hoop Stress in Target. Projectile at 4.4 m Depth.

- Figure A-121 Contours of Radial-Vertical Shear Stress in Target. Projectile at 4.4 m Depth.
- Figure A-122 Contours of Vertical Velocity in Target. Projectile at 4.4 m Depth.
- Figure A-123 Contours of Radial Velocity in Target. Projectile at 4.4 m Depth.
- Figure A-124 Lagrangian Coordinates When Projectile has Penetrated to Depth of 5.2 m. Radial Dimensions Doubled for Clarity.
- Figure A-125 Normal Stress (Pa) Along Surface of Projectile When Projectile is at 5.2 m Depth.
- Figure A-126 Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 5.2 m Depth.
- Figure A-127 Contours of Axial Stress in Target. Projectile at 5.2 m Depth.
- Figure A-128 Contours of Radial Stress in Target. Projectile at 5.2 m Depth.
- Figure A-129 Contours of Hoop Stress in Target. Projectile at 5.2 m Depth.
- Figure A-130 Contours of Radial-Vertical Shear Stress in Target. Projectile at 5.2 m Depth.
- Figure A-131 Contours of Vertical Velocity in Target. Projectile at 5.2 m Depth.
- Figure A-132 Contours of Radial Velocity in Target. Projectile at 5.2 m Depth.
- Figure A-133 Lagrangian Coordinates When Projectile has Penetrated to Depth of 6.8 m. Radial Dimensions Doubled for Clarity.
- Figure A-134 Normal Stress (Pa) Along Surface of Projectile When Projectile is at 6.8 m Depth.
- Figure A-135 Tangential Stress (Pa) Along Surface of Projectile when Projectile is at 6.8 m Depth.
- Figure A-136 Contours of Axial Stress in Target. Projectile at 6.8 m Depth.
- Figure A-137 Contours of Radial Stress in Target. Projectile at 6.8 m Depth.
- Figure A-138 Contours of Hoop Stress in Target. Projectile at 6.8 m Depth.

Figure A-139 Contours of Radial-Vertical Shear Stress in Target. Projectile  
at 6.8 m Depth.

Figure A-140 Contours of Vertical Velocity in Target. Projectile at 6.8 m Depth.

Figure A-141 Contours of Radial Velocity in Target. Projectile at 6.8 m Depth.

TABLE A-1

TABLE OF HISTORY PLOTS

| Point | Radius (m) | Depth (m) | Radial Velocity | Axial Velocity | Radial Displacement | Axial Displacement | Pressure | Deviator Stress | Radial Stress | Axial Stress |
|-------|------------|-----------|-----------------|----------------|---------------------|--------------------|----------|-----------------|---------------|--------------|
|       | X          | Z         | UX              | UZ             | DX                  | DZ                 | P        | J2              | TRX           | TRZ          |
| 3     | 0.15       | 3.6       | A-11            | A-12           | A-13                | A-14               | A-15     | A-16            | A-17          | A-18         |
| 4     | 0.15       | 0.4       | A-19            | A-20           | A-21                | A-22               | A-23     | A-24            |               |              |
| 5     | 0.15       | 0.1       | A-25            | A-26           | A-27                | A-28               | A-29     | A-30            |               |              |
| 7     | 0.45       | 5.4       | A-31            | A-32           | A-33                | A-34               | A-35     | A-36            | A-37          |              |
| 8     | 0.45       | 3.6       | A-38            | A-39           | A-40                | A-41               | A-42     | A-43            | A-44          | A-45         |
| 9     | 0.45       | 1.8       | A-46            | A-47           | A-48                | A-49               | A-50     | A-51            | A-52          |              |
| 10    | 0.45       | 0.4       | A-53            | A-54           | A-55                | A-56               | A-57     | A-58            |               |              |
| 11    | 0.45       | 0.1       | A-59            | A-60           | A-61                | A-62               | A-63     | A-64            |               |              |
| 12    | 0.9        | 3.6       | A-65            | A-66           | A-67                | A-68               | A-69     | A-70            | A-71          | A-72         |
| 13    | 1.5        | 5.4       |                 |                |                     |                    | A-73     |                 | A-74          |              |
| 14    | 1.5        | 3.6       |                 |                |                     |                    | A-75     |                 | A-76          |              |
| 15    | 1.5        | 1.8       |                 |                |                     |                    | A-77     |                 | A-78          |              |

Table A-2  
 Table of Figure Numbers for Contour Plots, Lagrangian  
 Grid Plots and Plots of Normal and Tangential  
 Stress Along Projectile Surface

| Projectile<br>Depth (m)<br>(Layer) | Time After<br>Impact<br>(ms) | Grid  | Normal<br>Stress | Tangential<br>Stress | Axial Stress<br>Contours | Radial Stress<br>Contours | Hoop Stress<br>Contours | Shear Stress<br>Contours | Axial Velocity<br>Contours | Radial Velocity<br>Contours |
|------------------------------------|------------------------------|-------|------------------|----------------------|--------------------------|---------------------------|-------------------------|--------------------------|----------------------------|-----------------------------|
| 0.1<br>(1)                         | 0.657                        | A-79  | A-80             | A-81                 | A-82                     | A-83                      | A-84                    | A-85                     | A-86                       | A-87                        |
| 0.4<br>(1)                         | 2.63                         | A-88  | A-89             | A-90                 | A-91                     | A-92                      | A-93                    | A-94                     | A-95                       | A-96                        |
| 2.0<br>(1)                         | 13.4                         | A-97  | A-98             | A-99                 | A-100                    | A-101                     | A-102                   | A-103                    | A-104                      | A-105                       |
| 2.8<br>(2)                         | 18.9                         | A-106 | A-107            | A-108                | A-109                    | A-110                     | A-111                   | A-112                    | A-113                      | A-114                       |
| 4.4<br>(2)                         | 30.3                         | A-115 | A-116            | A-117                | A-118                    | A-119                     | A-120                   | A-121                    | A-122                      | A-123                       |
| 5.2<br>(3)                         | 36.2                         | A-124 | A-125            | A-126                | A-127                    | A-128                     | A-129                   | A-130                    | A-131                      | A-132                       |
| 6.8<br>(3)                         | 48.4                         | A-133 | A-134            | A-135                | A-136                    | A-137                     | A-138                   | A-139                    | A-140                      | A-141                       |

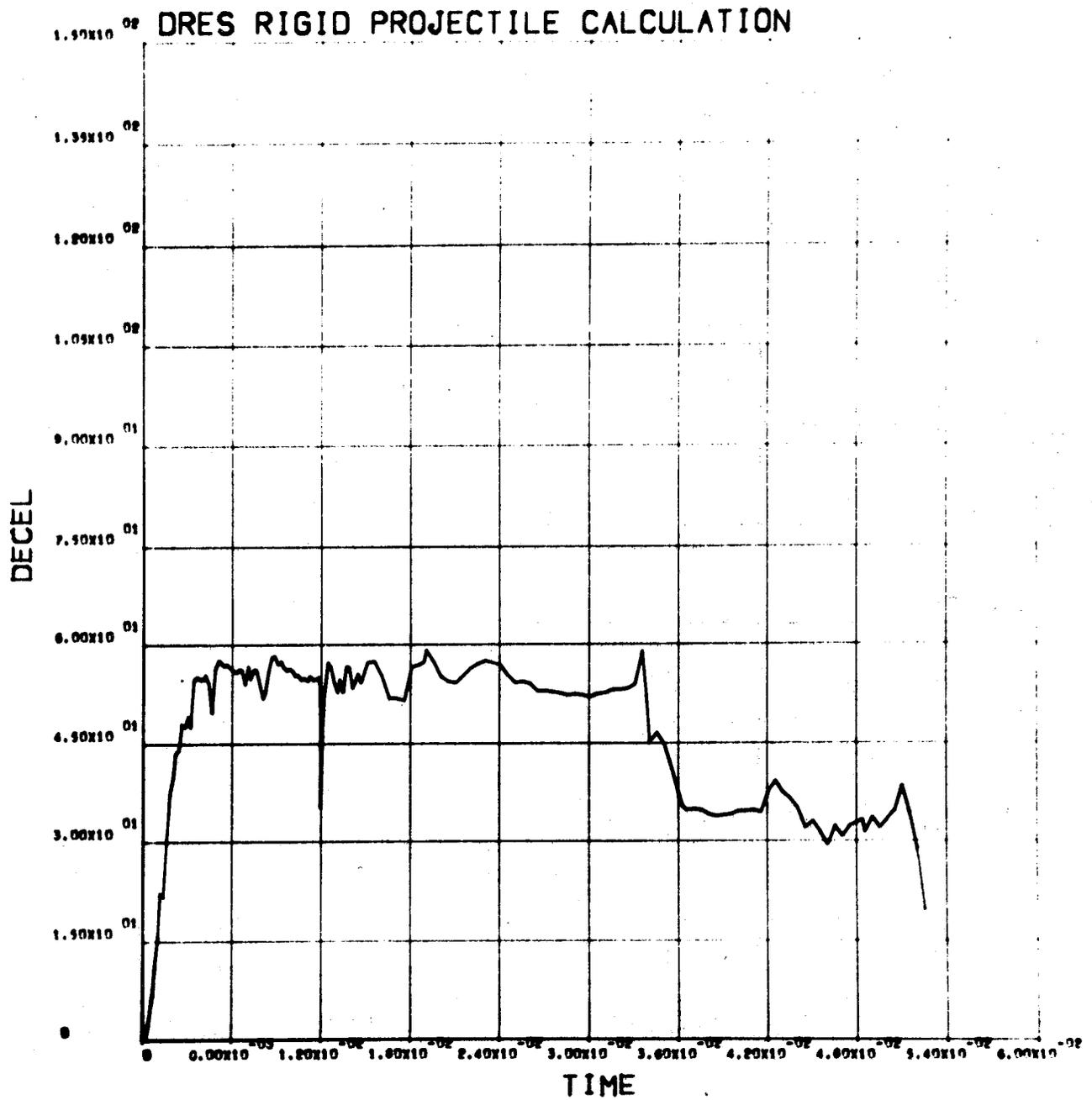


Figure A-1  
Projectile Deceleration vs. Time.

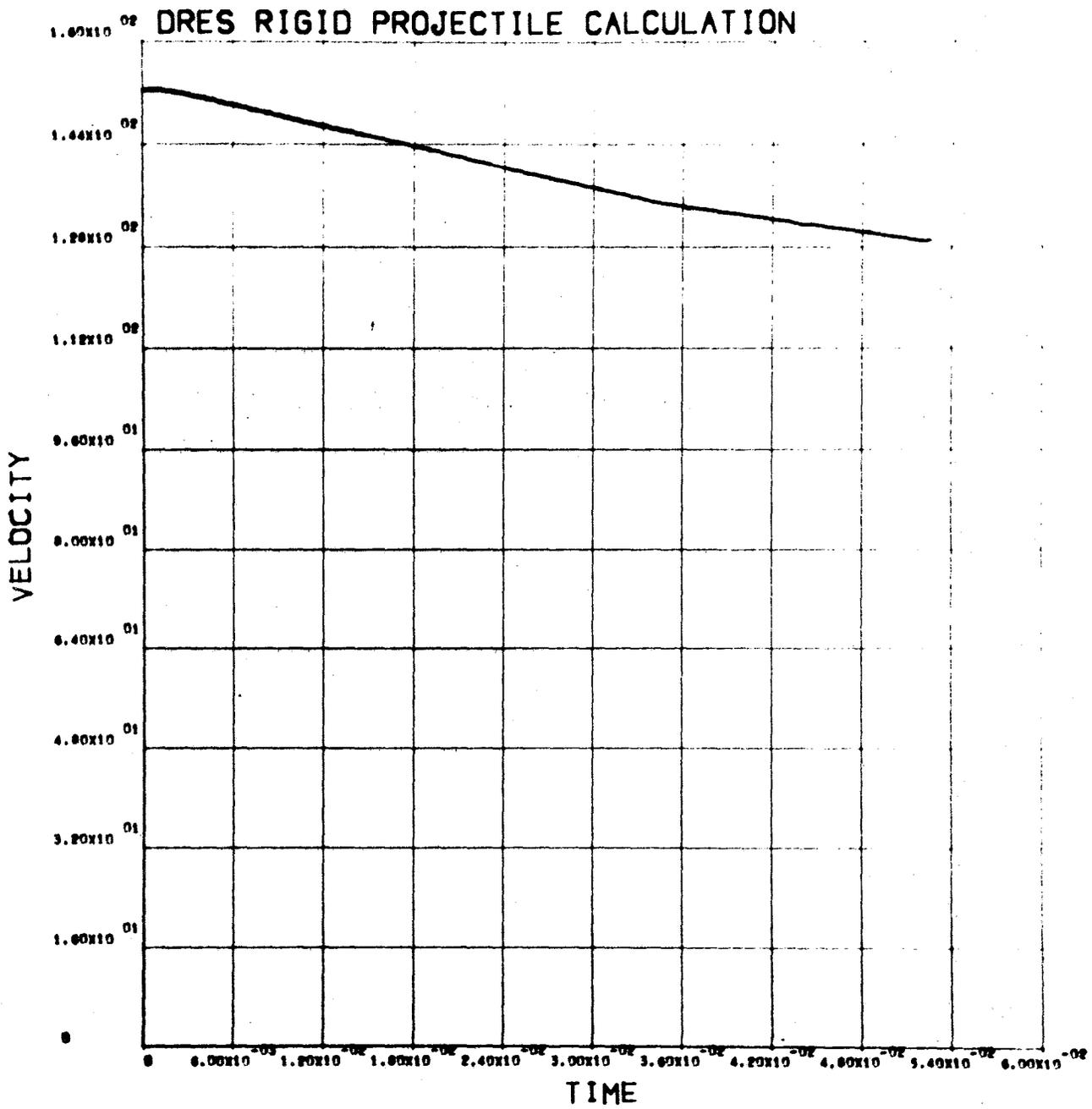


Figure A-2  
Projectile Velocity vs. Time.

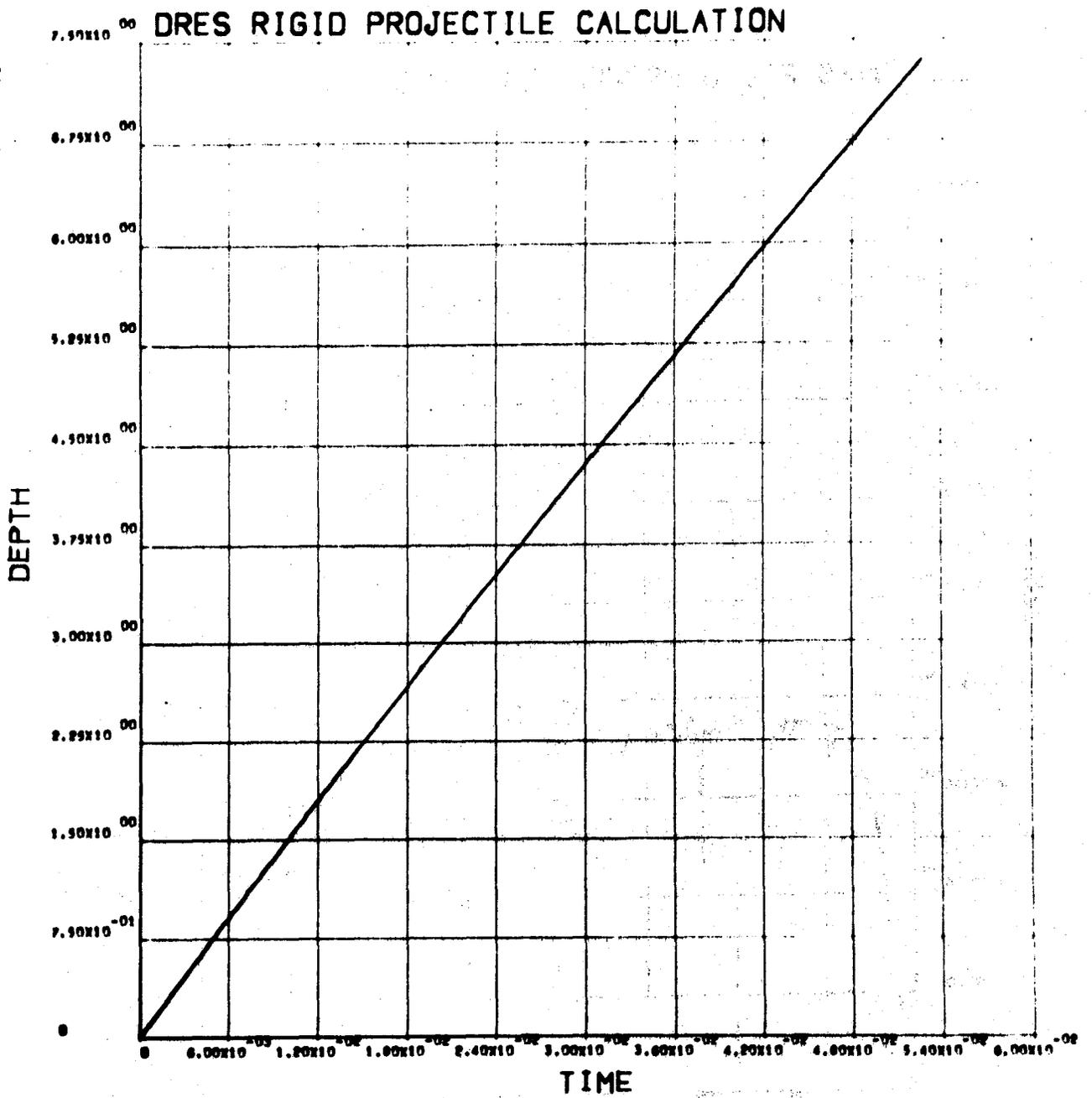


Figure A-3  
Projectile Depth vs. Time.

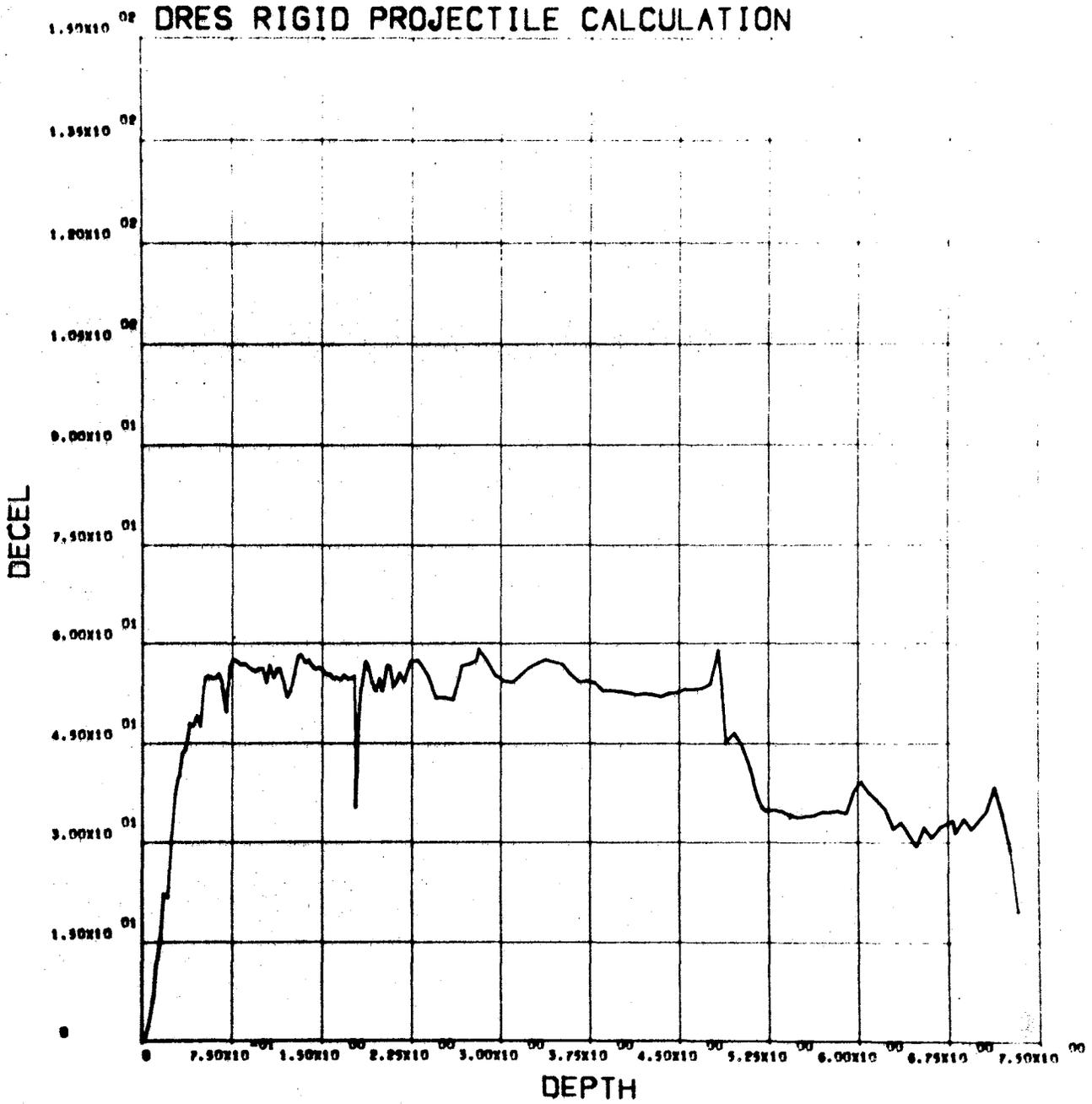


Figure A-4  
Projectile Deceleration vs. Depth.

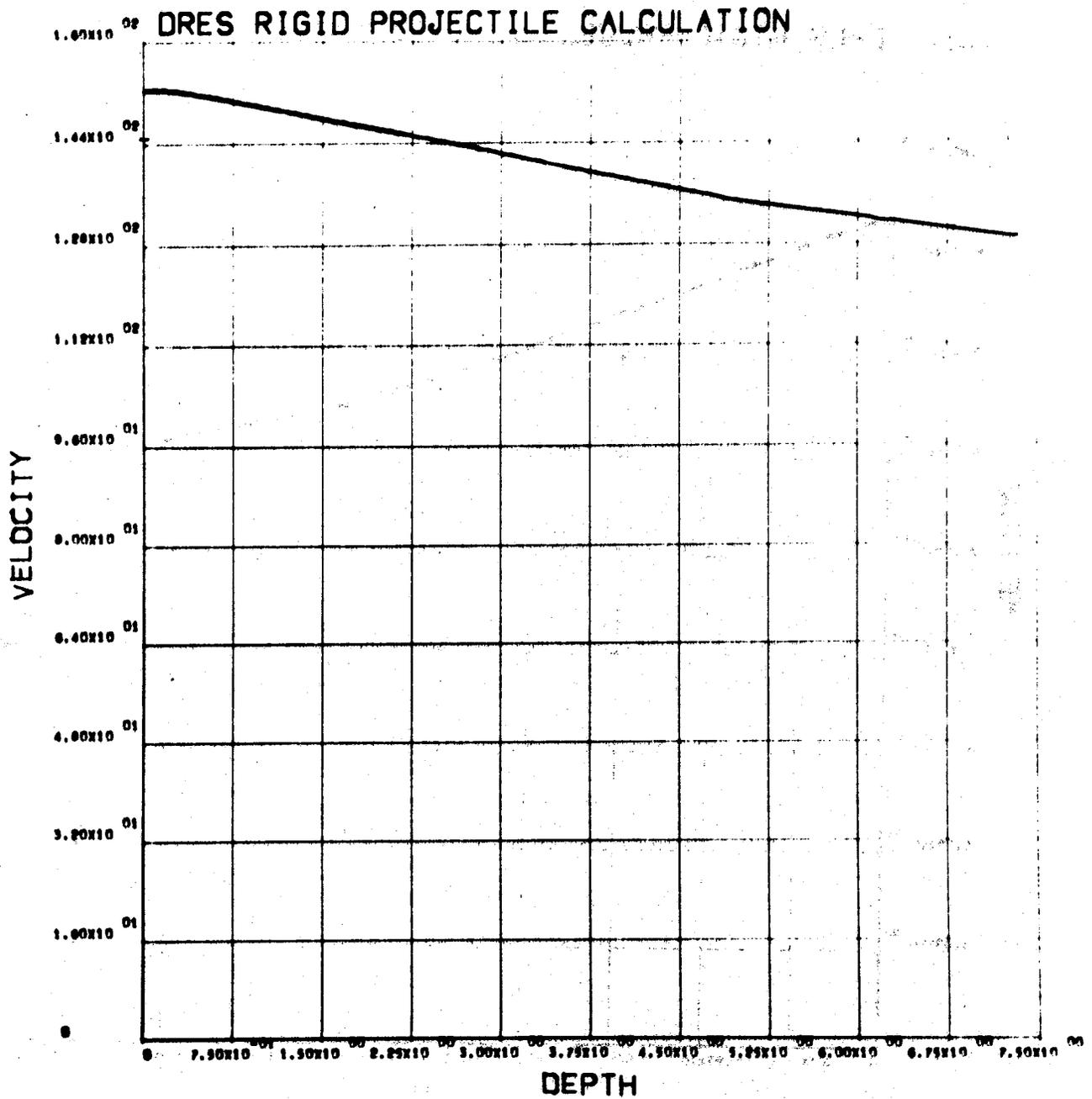


Figure A-5  
Projectile Velocity vs. Depth.

# 4.00x10<sup>05</sup> DRES RIGID PROJECTILE CALCULATION

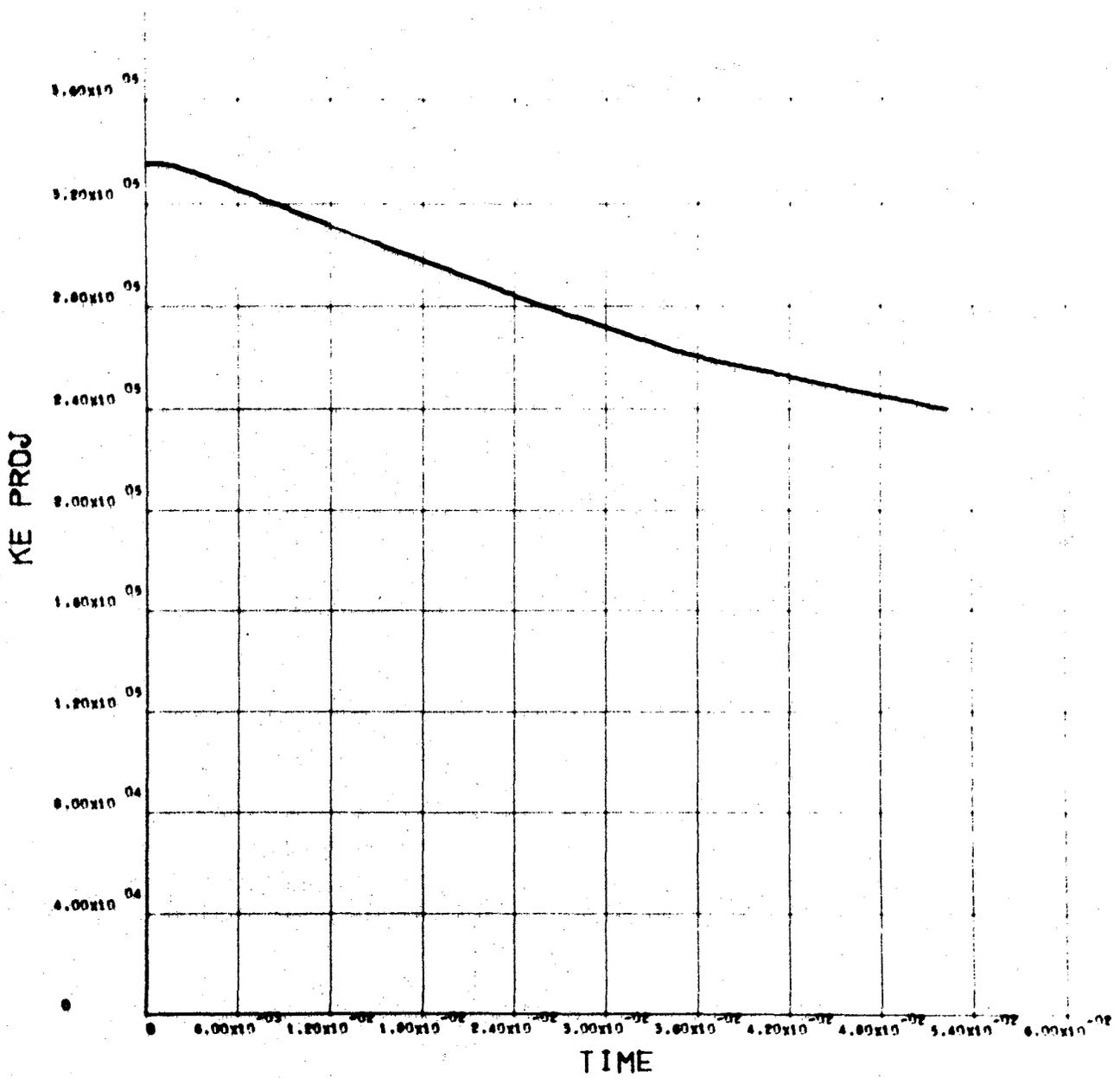


Figure A-6  
Projectile Kinetic Energy/Radian vs. Time.

# DRES RIGID PROJECTILE CALCULATION

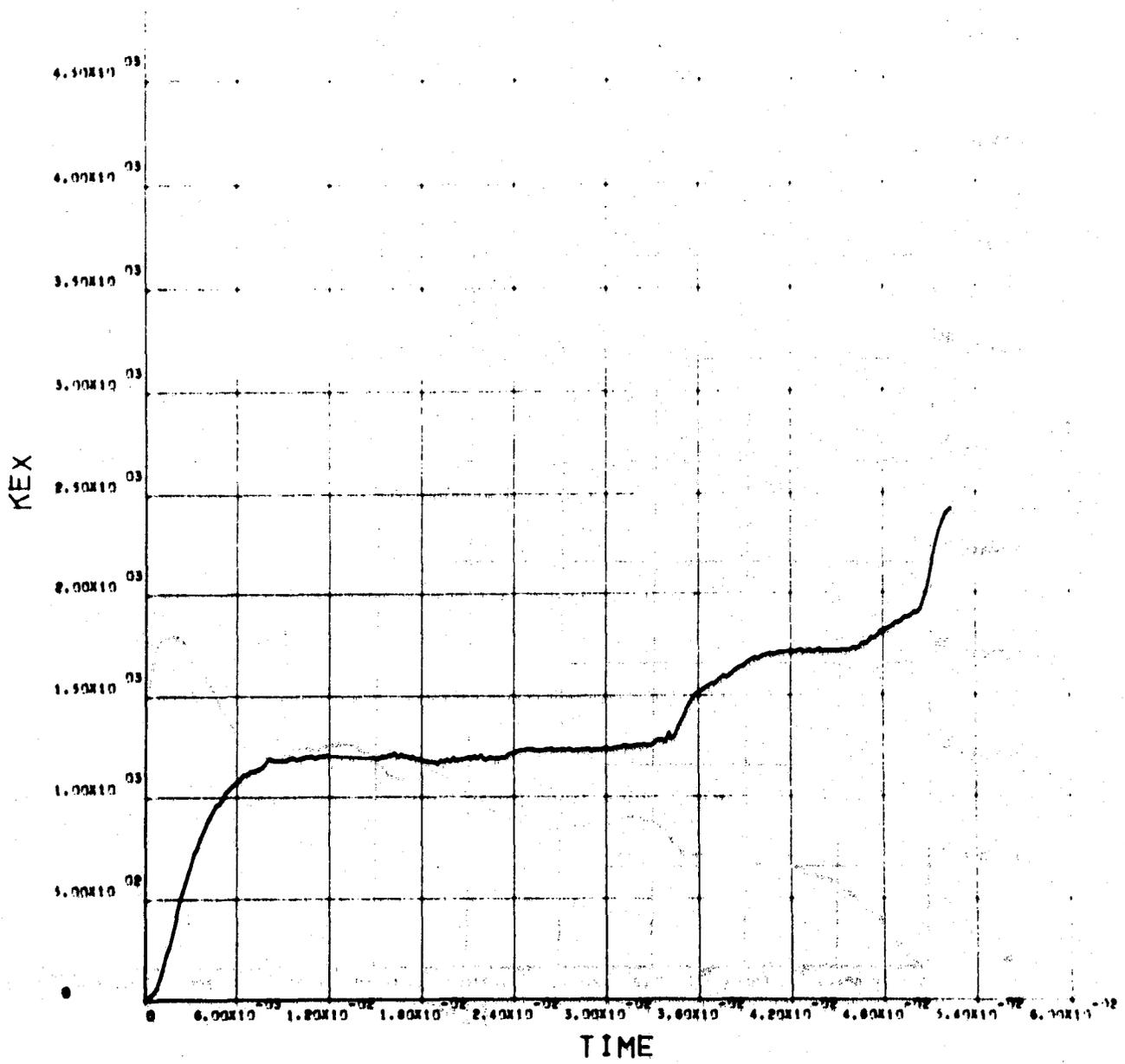


Figure A-7  
Soil Kinetic Energy/Radian, Due to Radial Velocity, vs. Time.

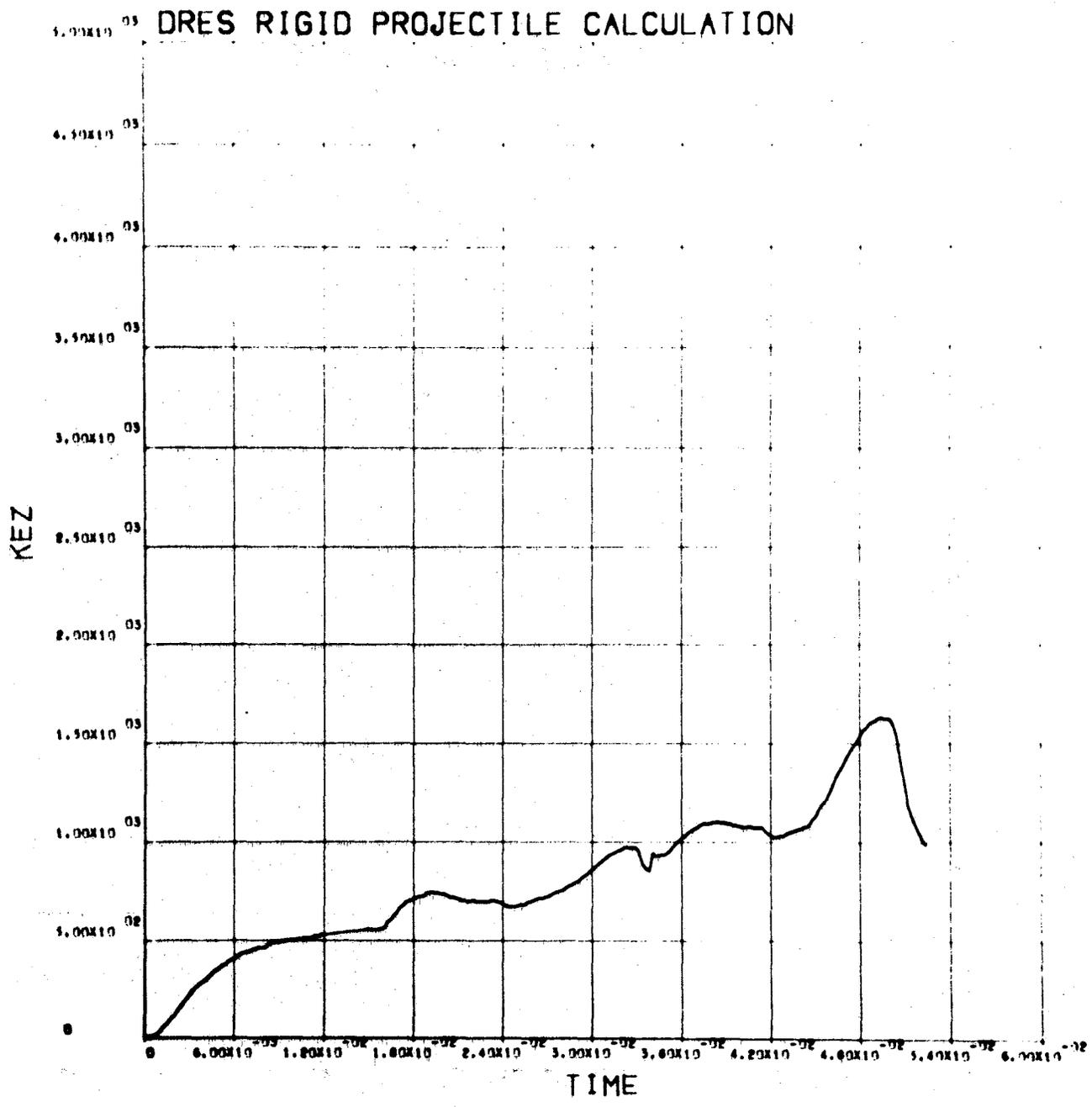


Figure A-8

Soil Kinetic Energy/Radian, Due to Axial Velocity, vs. Time.

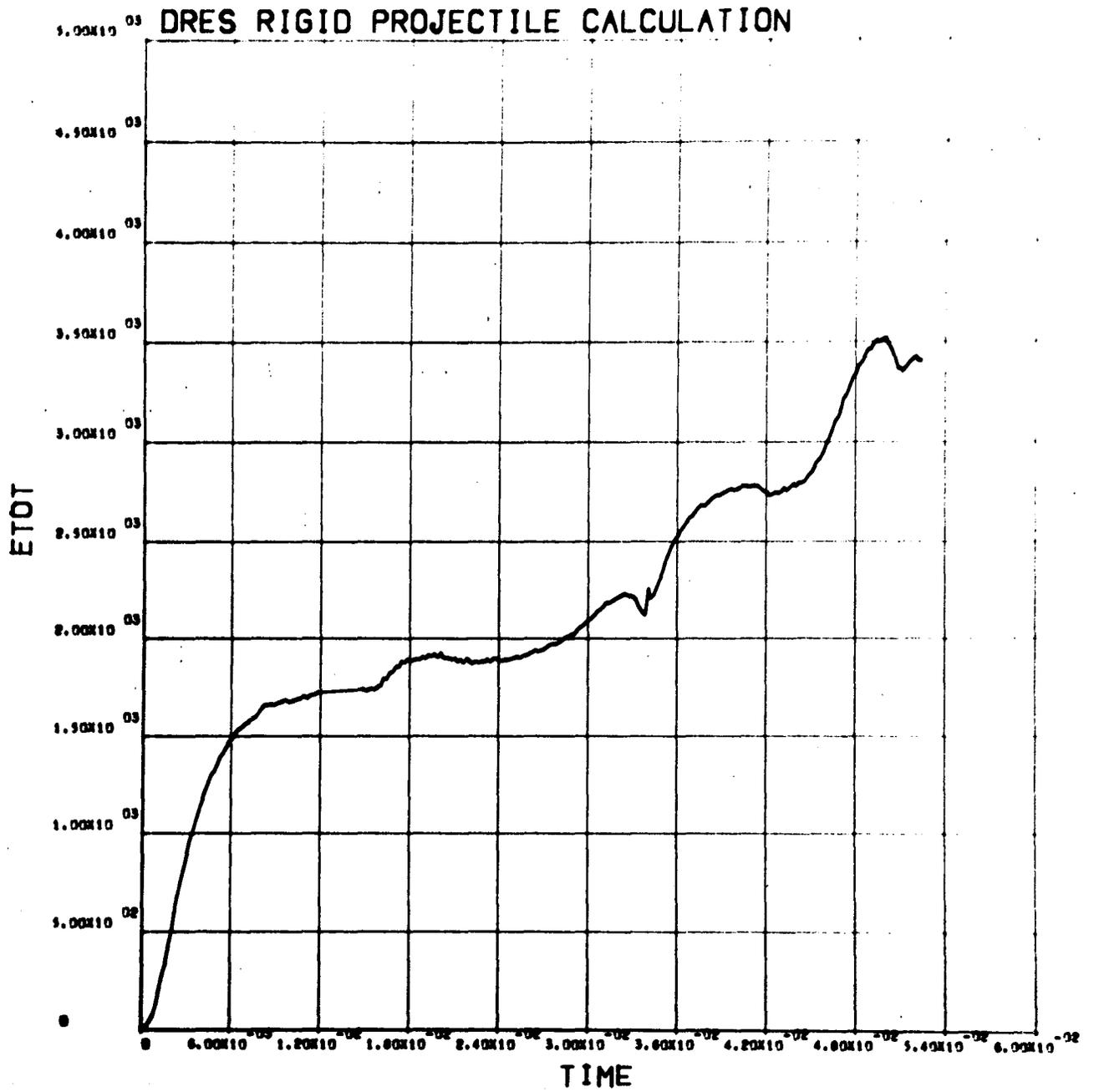


Figure A-9  
Total Soil Kinetic Energy/Radian vs. Time.

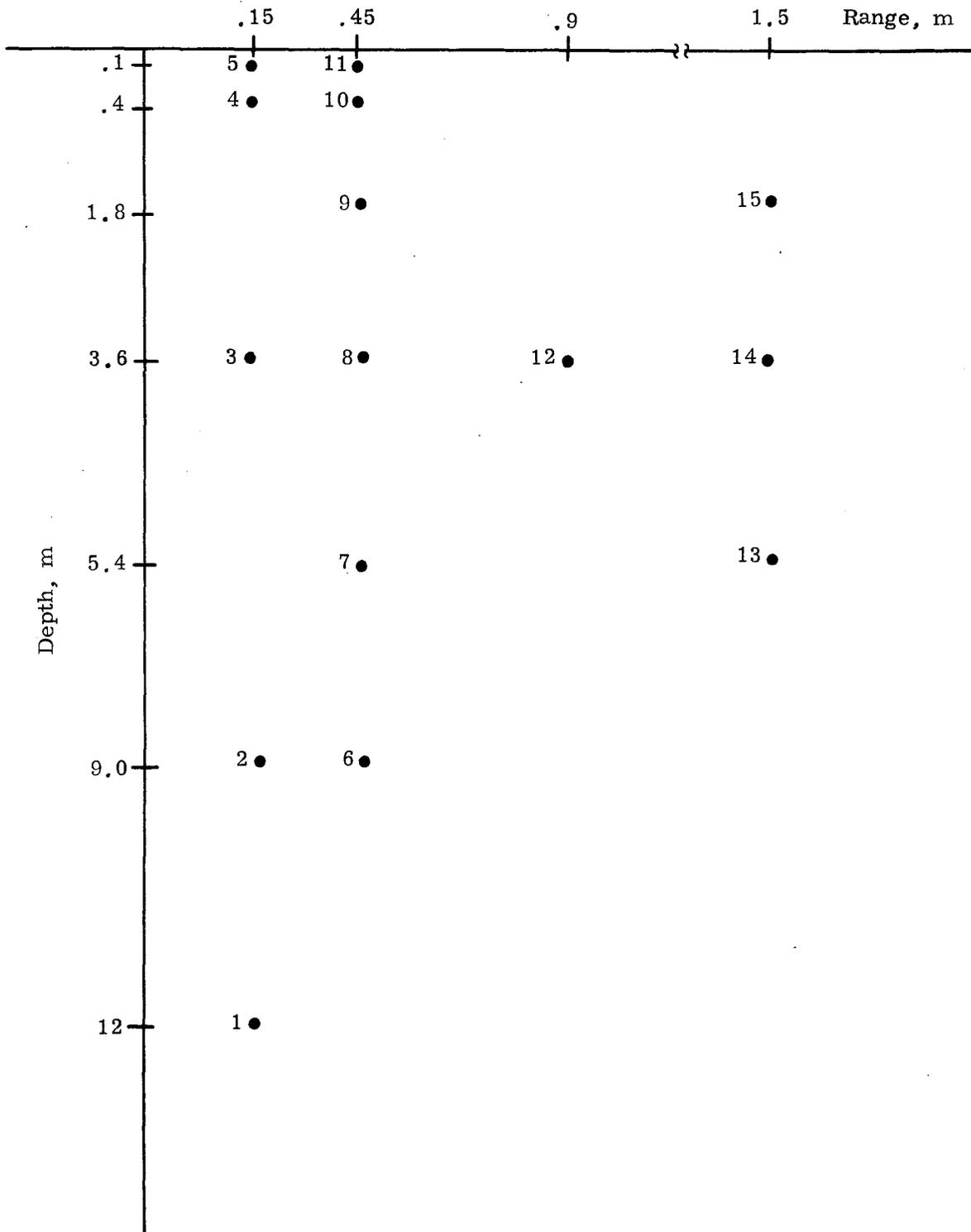


Figure A-10

Legend for Point History Plots from Rigid Projectile Calculation.

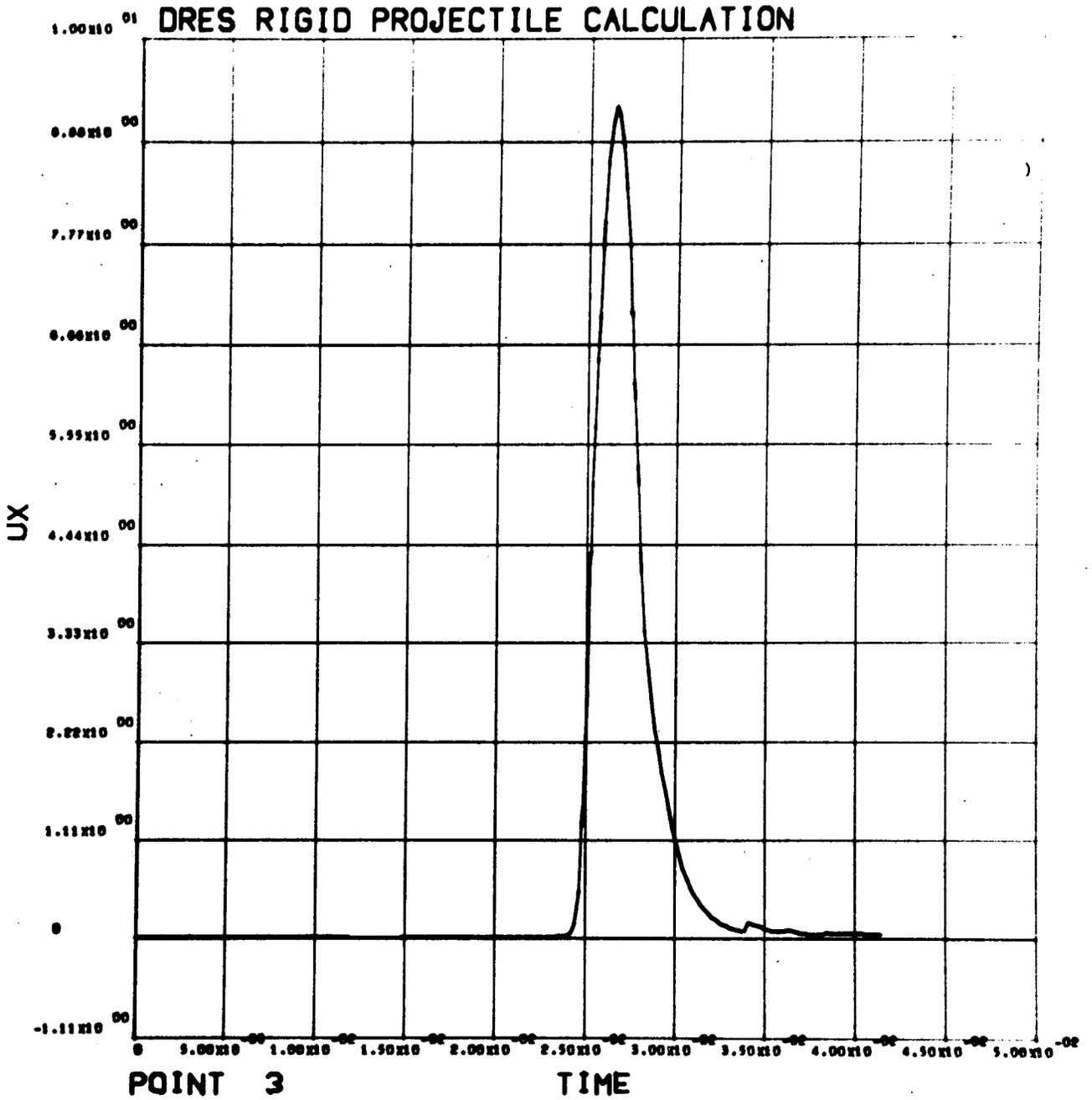


Figure A-11

Radial Velocity (m/s) versus Time (s) for Particle at Point 3,

Z = 3.6 m, R = 0.15 m.

# DRES RIGID PROJECTILE CALCULATION

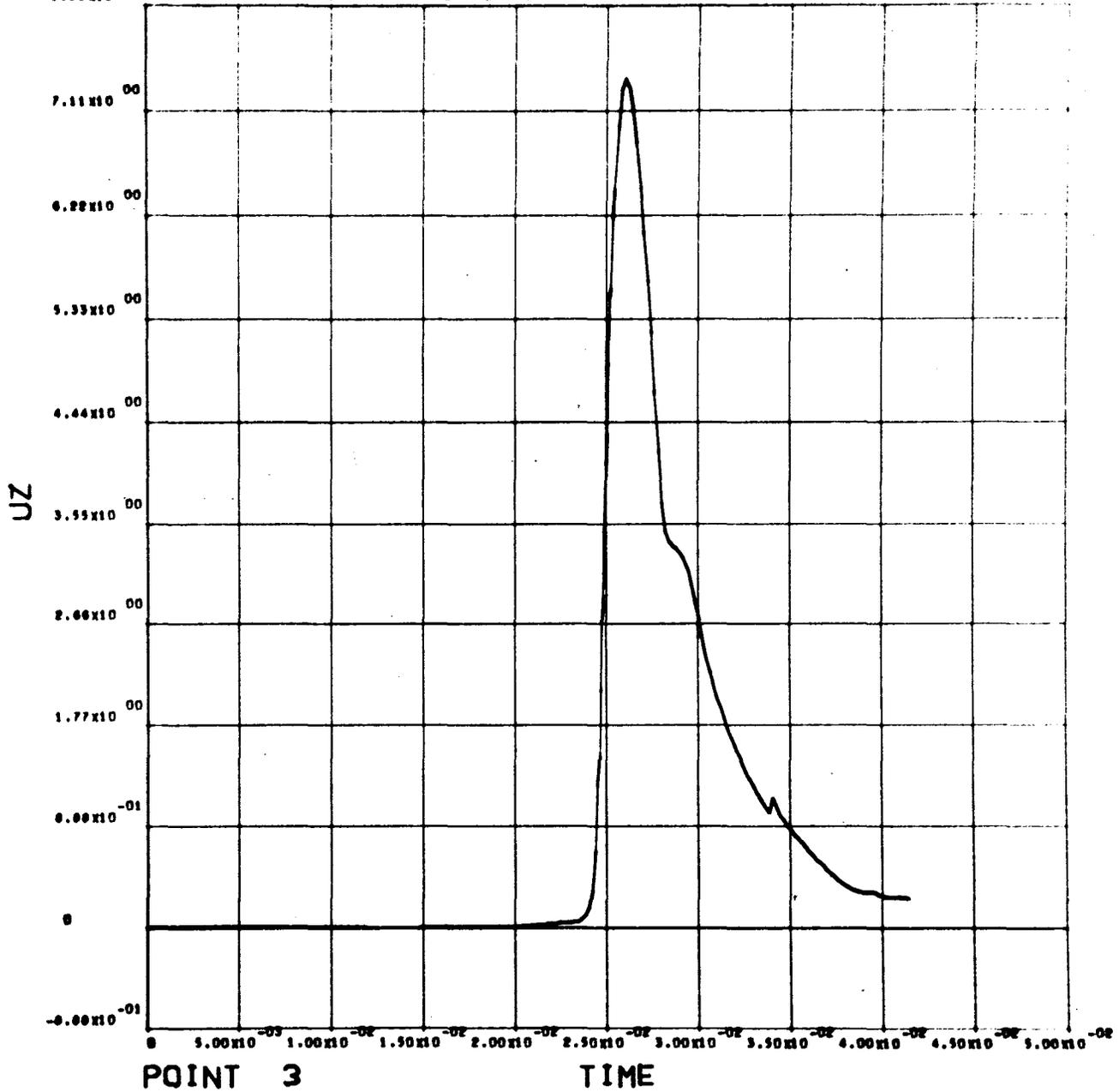


Figure A-12

Axial Velocity (m/s) versus Time (s) for Particle at Point 3,  
Z = 3.6 m, R = 0.15 m.

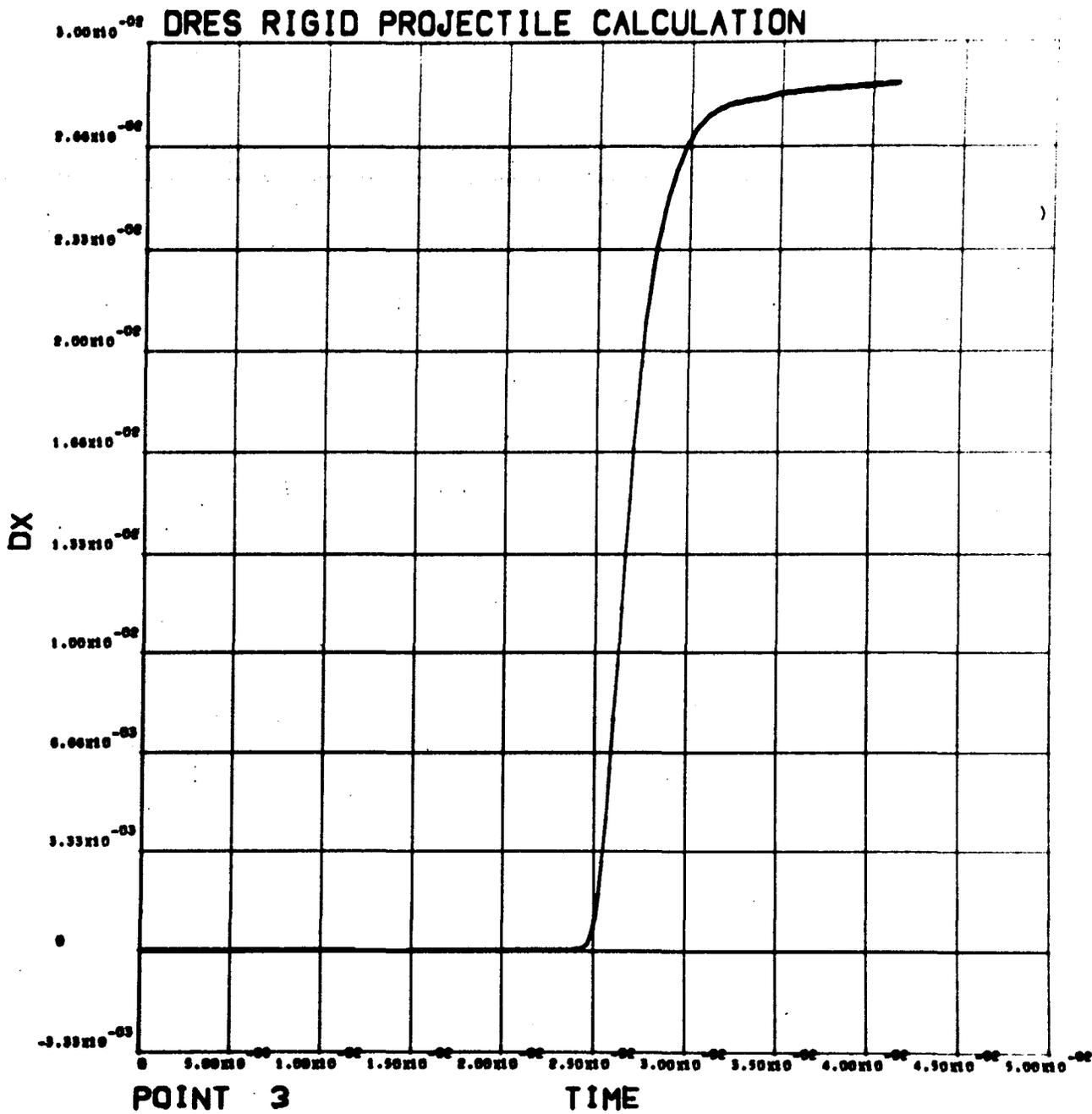


Figure A-13

Radial Displacement (m) versus Time (s) for Particle at Point 3,  
 $Z = 3.6 \text{ m}$ ,  $R = 0.15 \text{ m}$ .

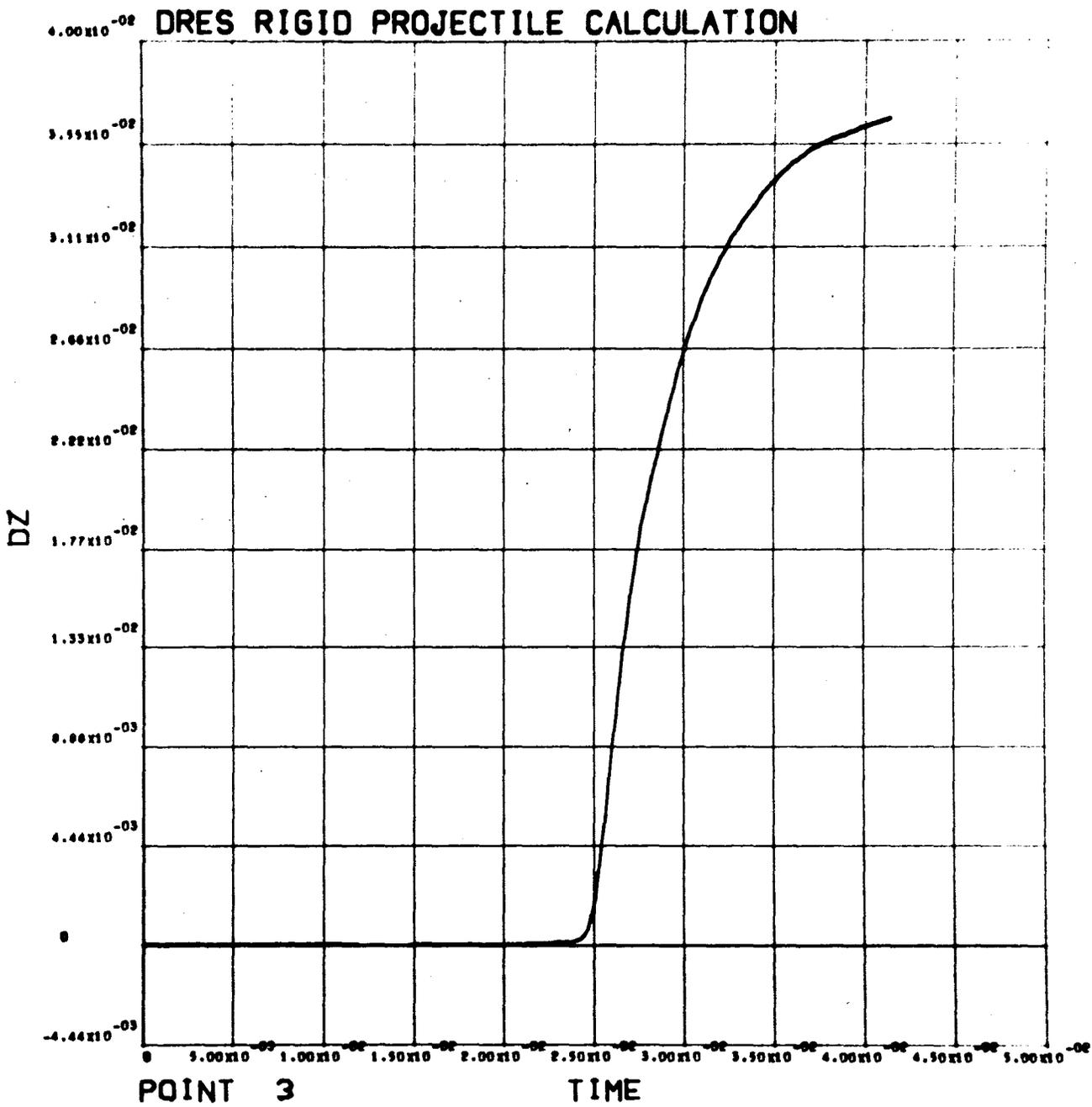


Figure A-14

Axial Displacement (m) versus Time (s) for particle at Point 3,  
 $Z = 3.6$  m,  $R = 0.15$  m.



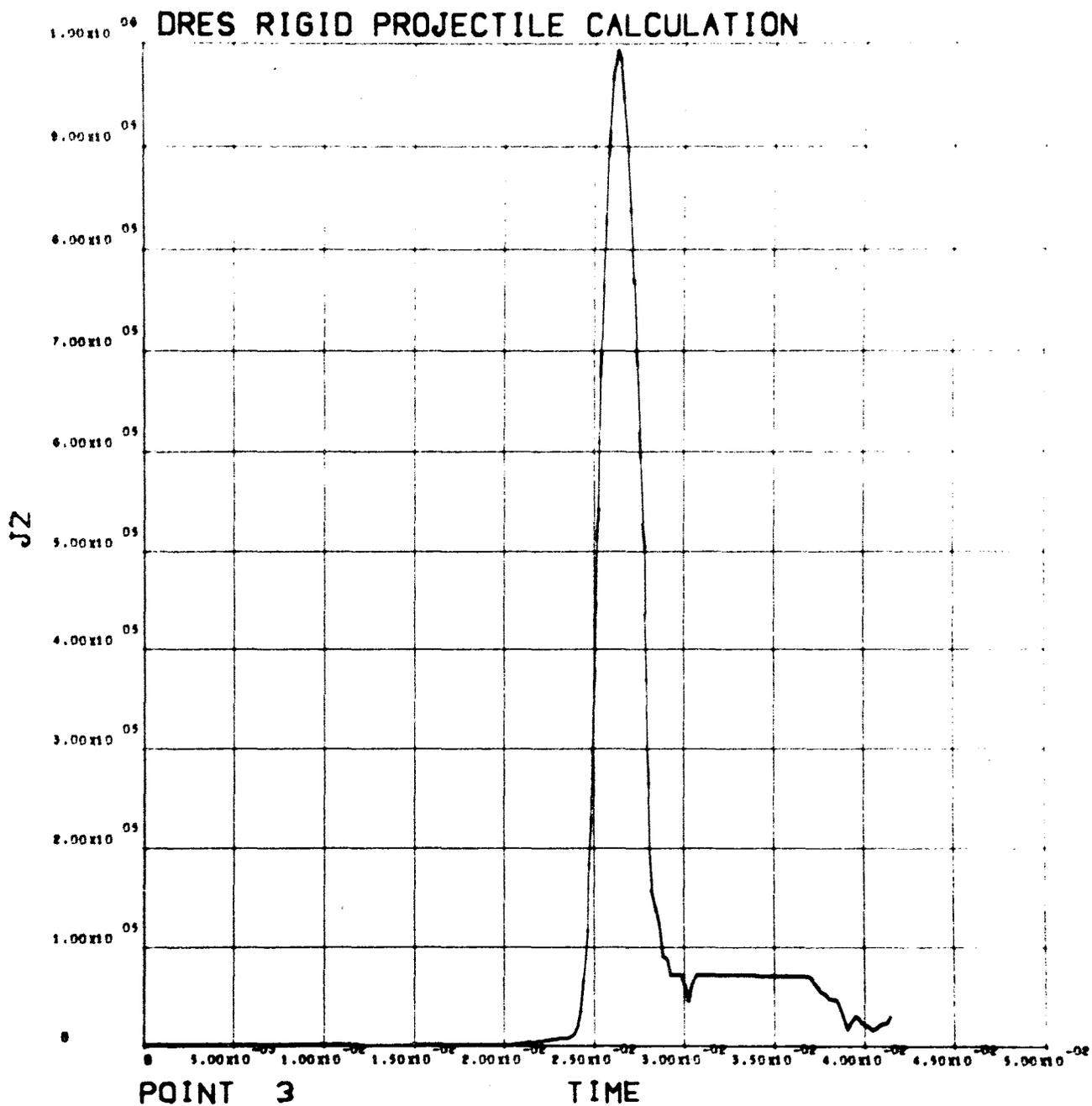


Figure A-16

Deviator Stress  $J_2$ , History (Pa) for Particle at Point 3,  $Z = 3.6$  m,  $R = 0.15$  m.  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).

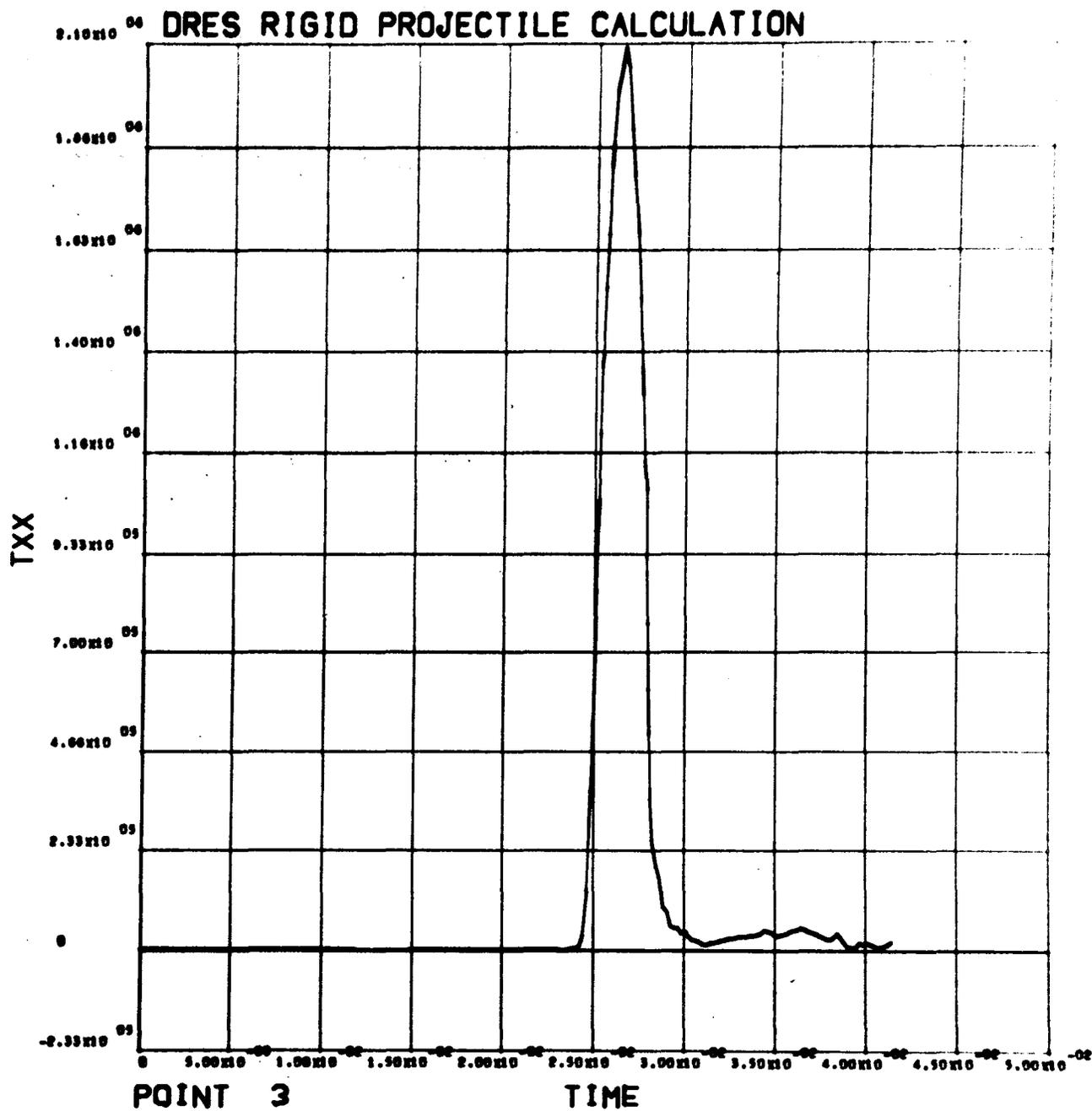


Figure A-17  
 Radial Stress (Pa) History for Particle at Point 3, Z = 3.6 m, R = 0.15 m.

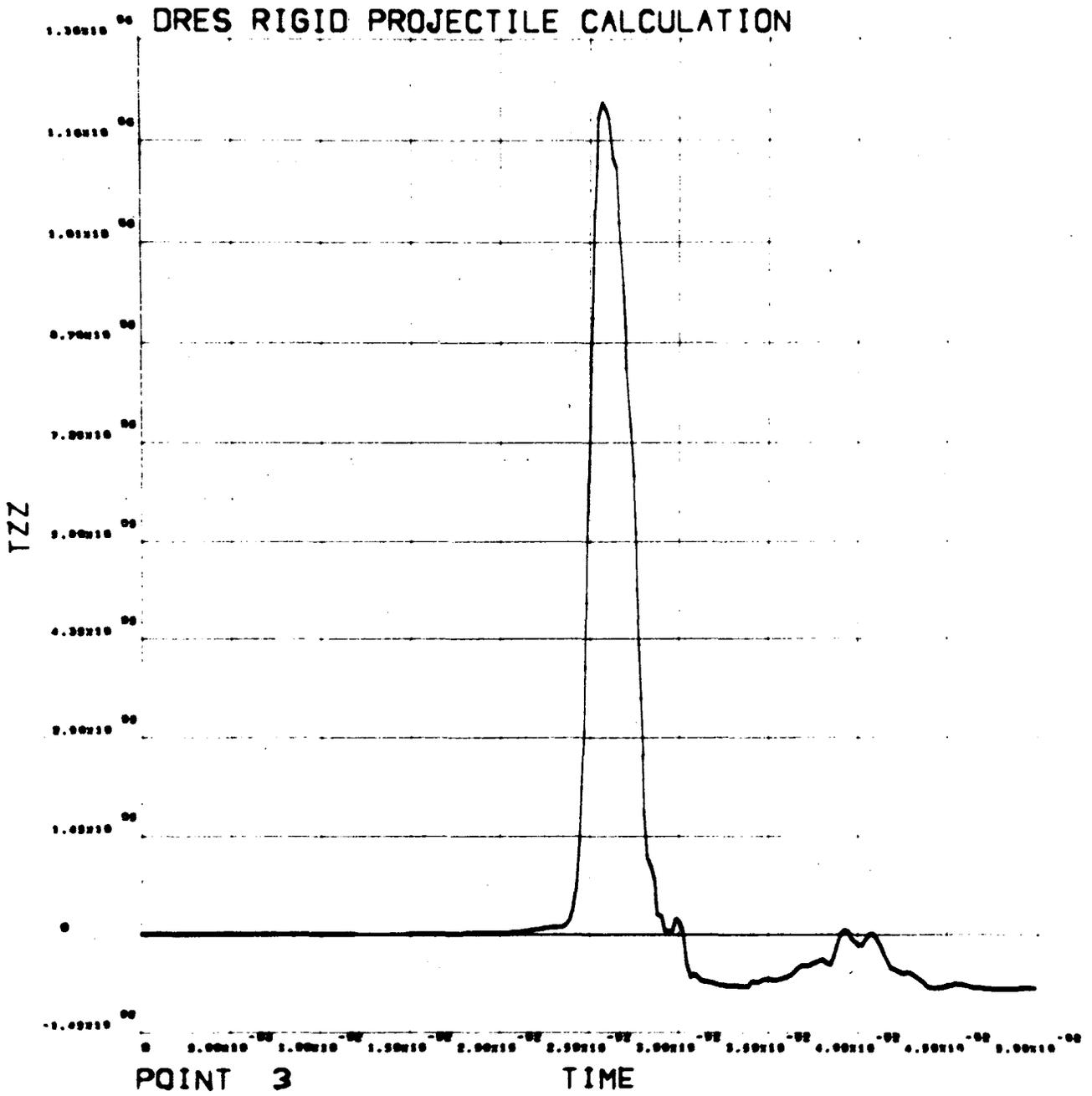


Figure A-18

Axial Stress (Pa) History for Particle at Point 3, Z = 3.6 m, R = 0.15 m.



# DRES RIGID PROJECTILE CALCULATION

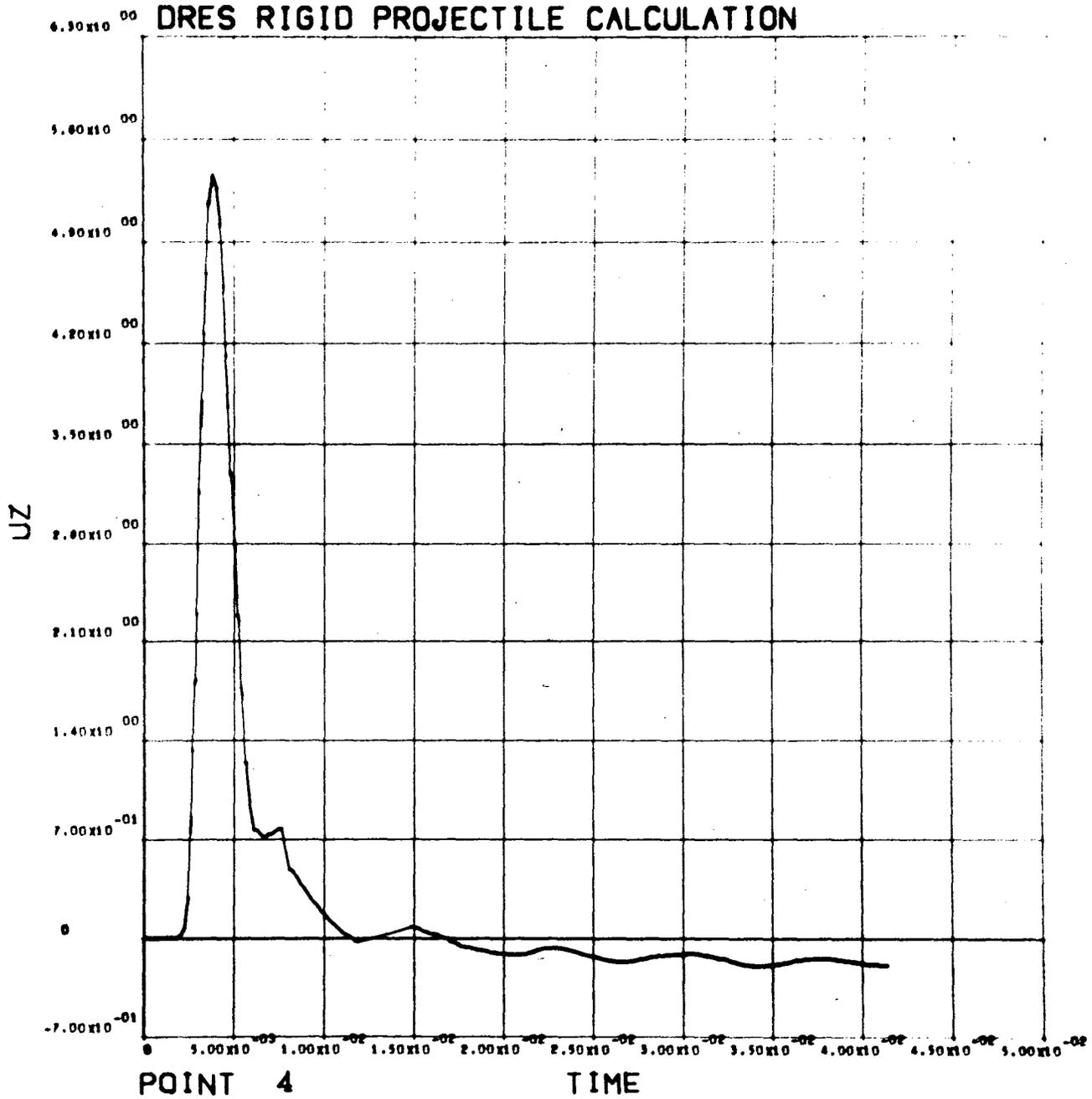


Figure A-20

Axial Velocity (m/s) versus Time (s) for Particle at Point 4,  
Z = 0.4 m, R = 0.15 m.



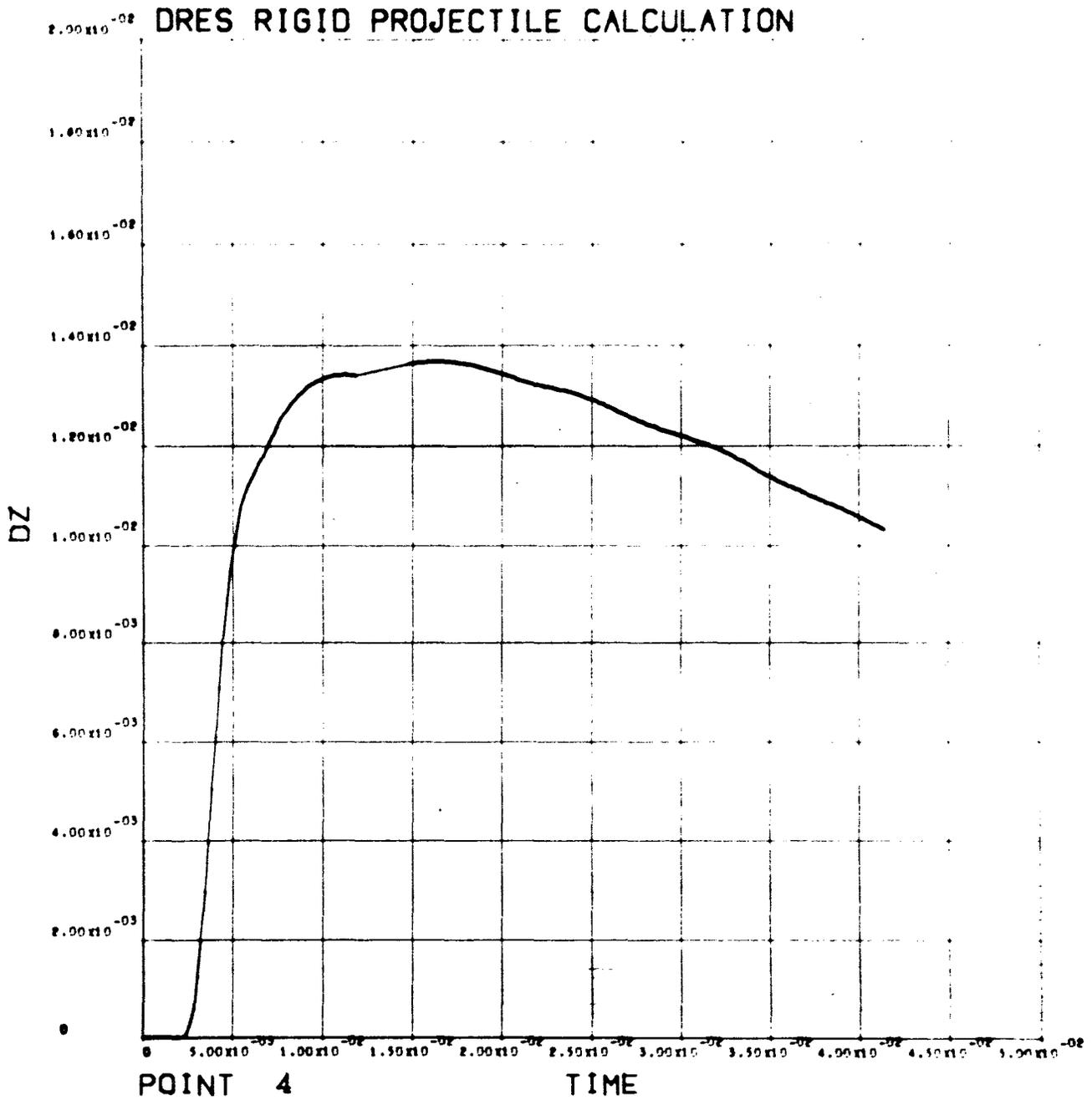


Figure A-22

Axial Displacement (m) versus Time (s) for Particle at Point 4,  
 $D = 1.4$  m,  $R = 0.15$  m.

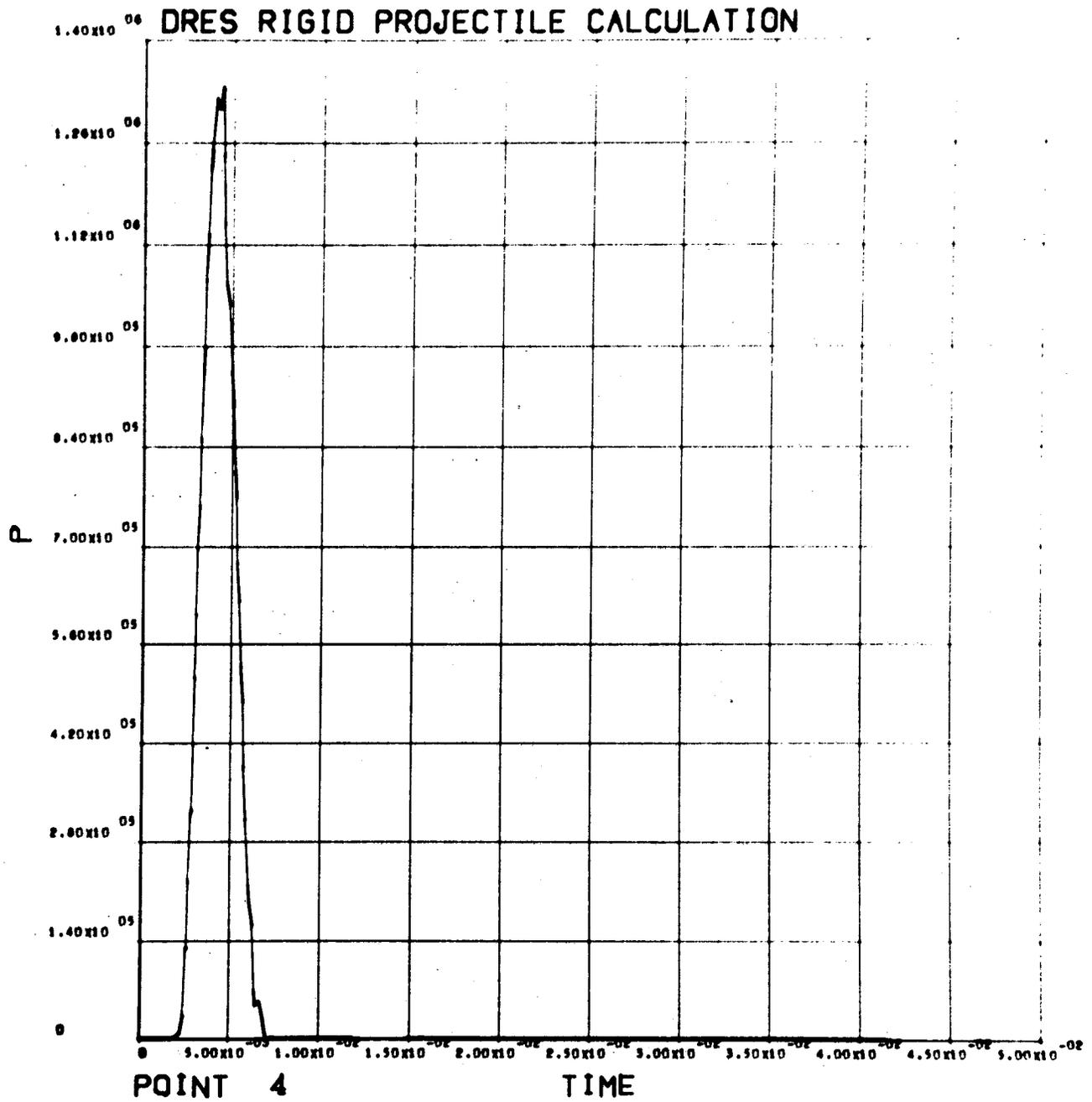


Figure A-23

Pressure (Pa) versus Time (s) for Particle at Point 4, Z = 0.4 m, R = 0.15 m.

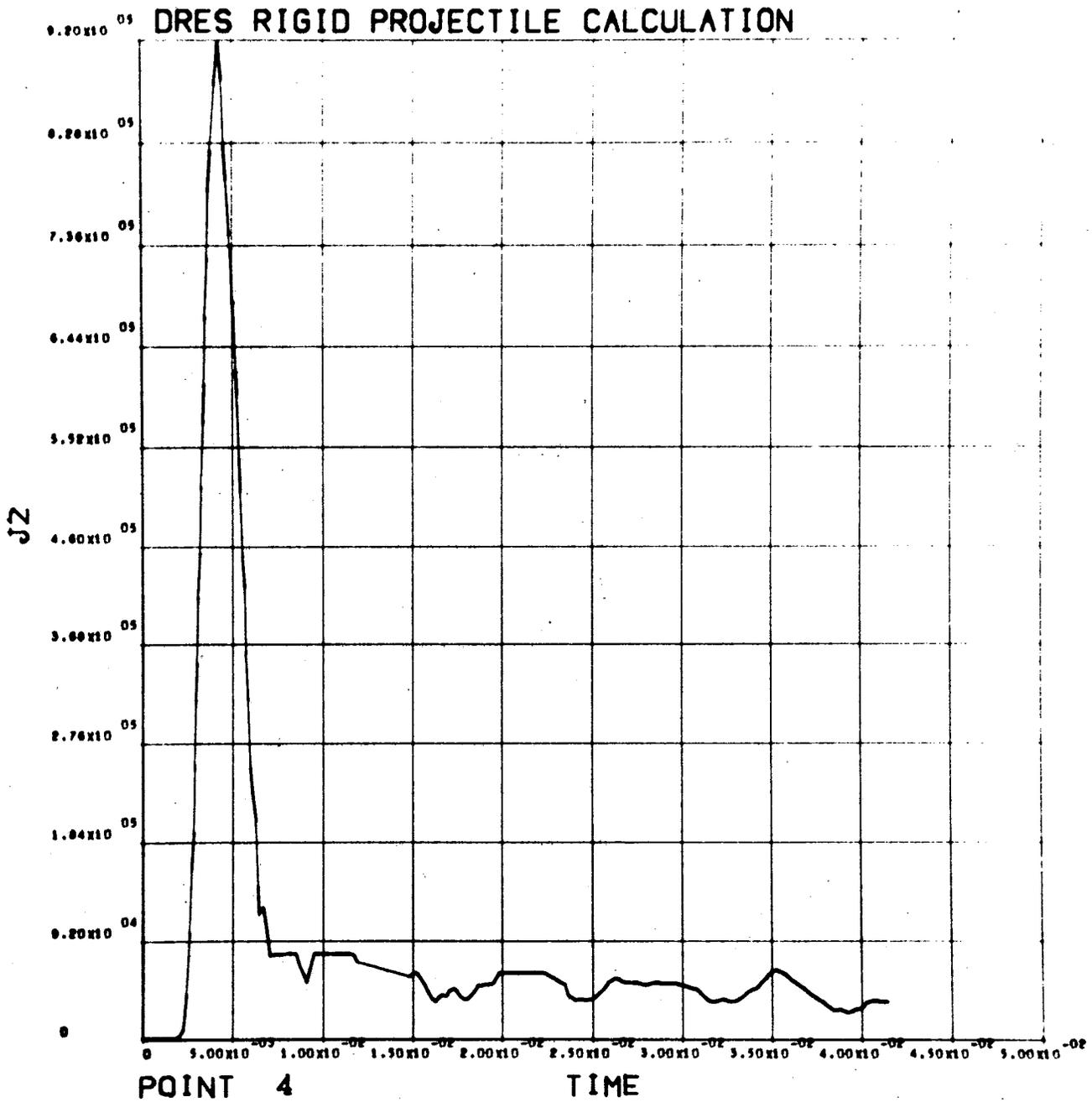


Figure A-24

Deviator Stress  $J_2$ , History (Pa) for Particle at Point 4,  $Z = 0.4$  m,  $R = 0.15$  m,  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).

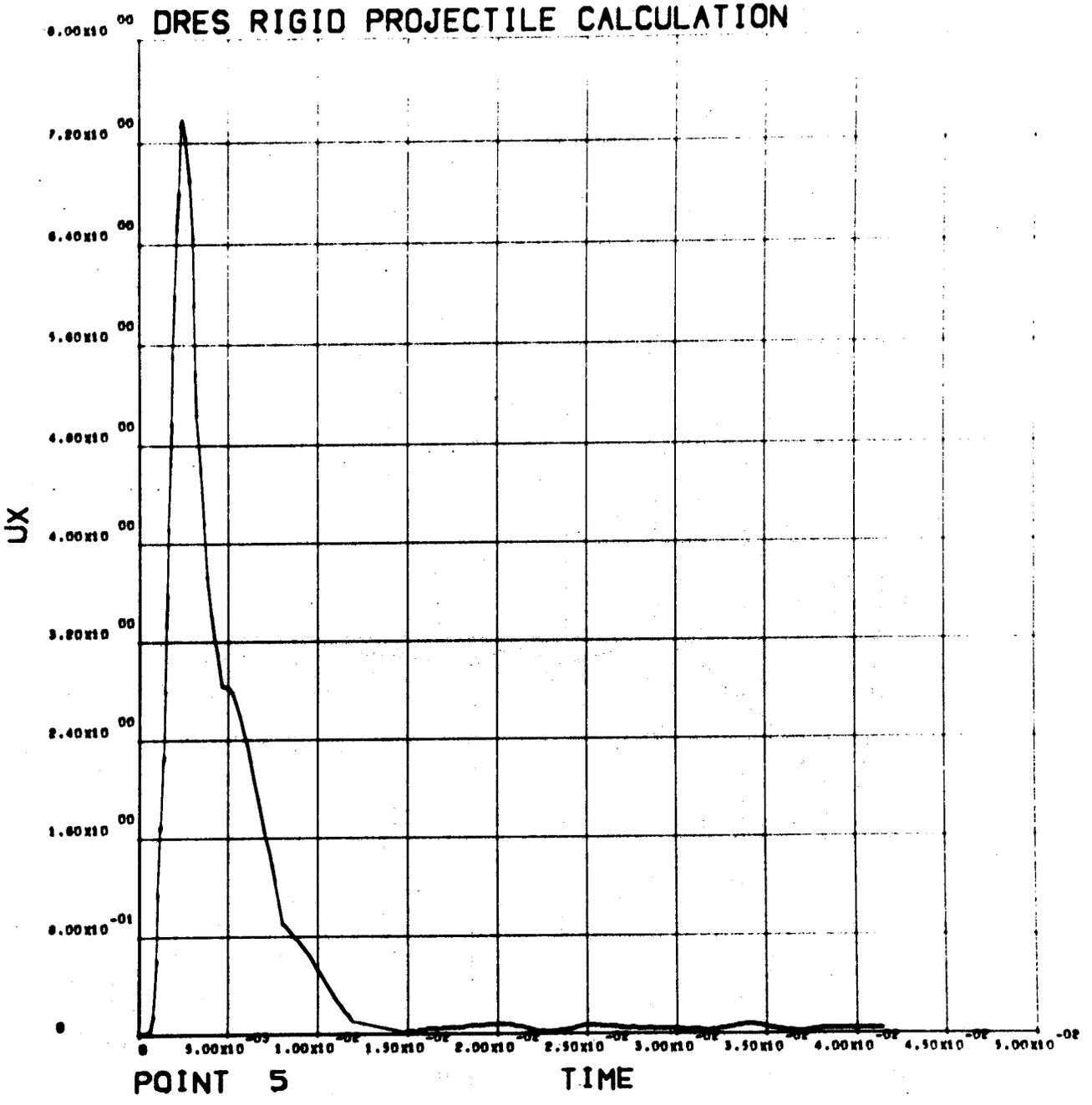


Figure A-25

Radial Velocity (m/s) versus Time (s) for Particle at Point 5, Z = 0.1 m, R = 0.15 m.

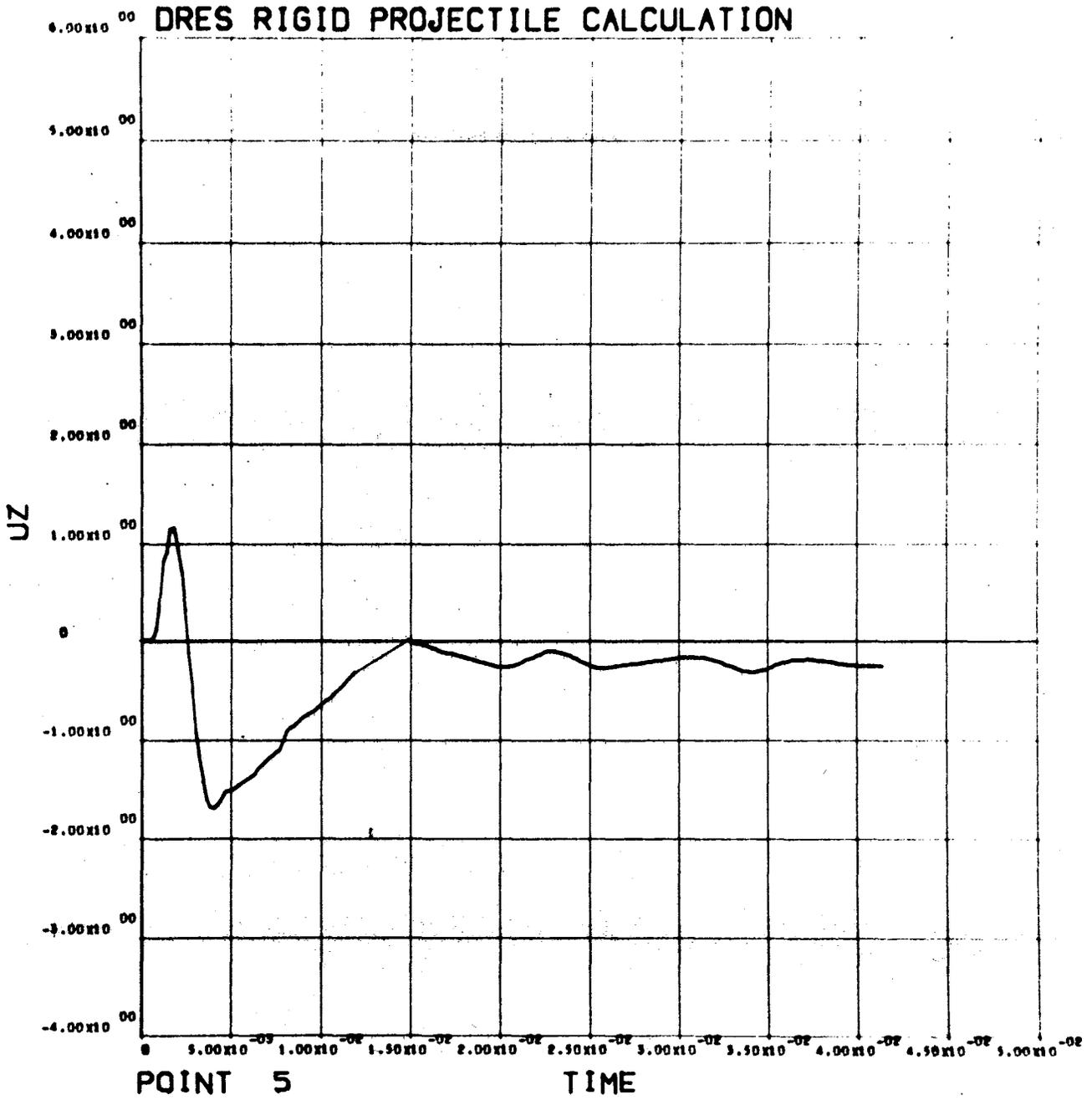


Figure A-26

Axial Velocity (m/s) versus Time (s) for Particle at Point 5, Z = 0.1 m, R = 0.15 m.

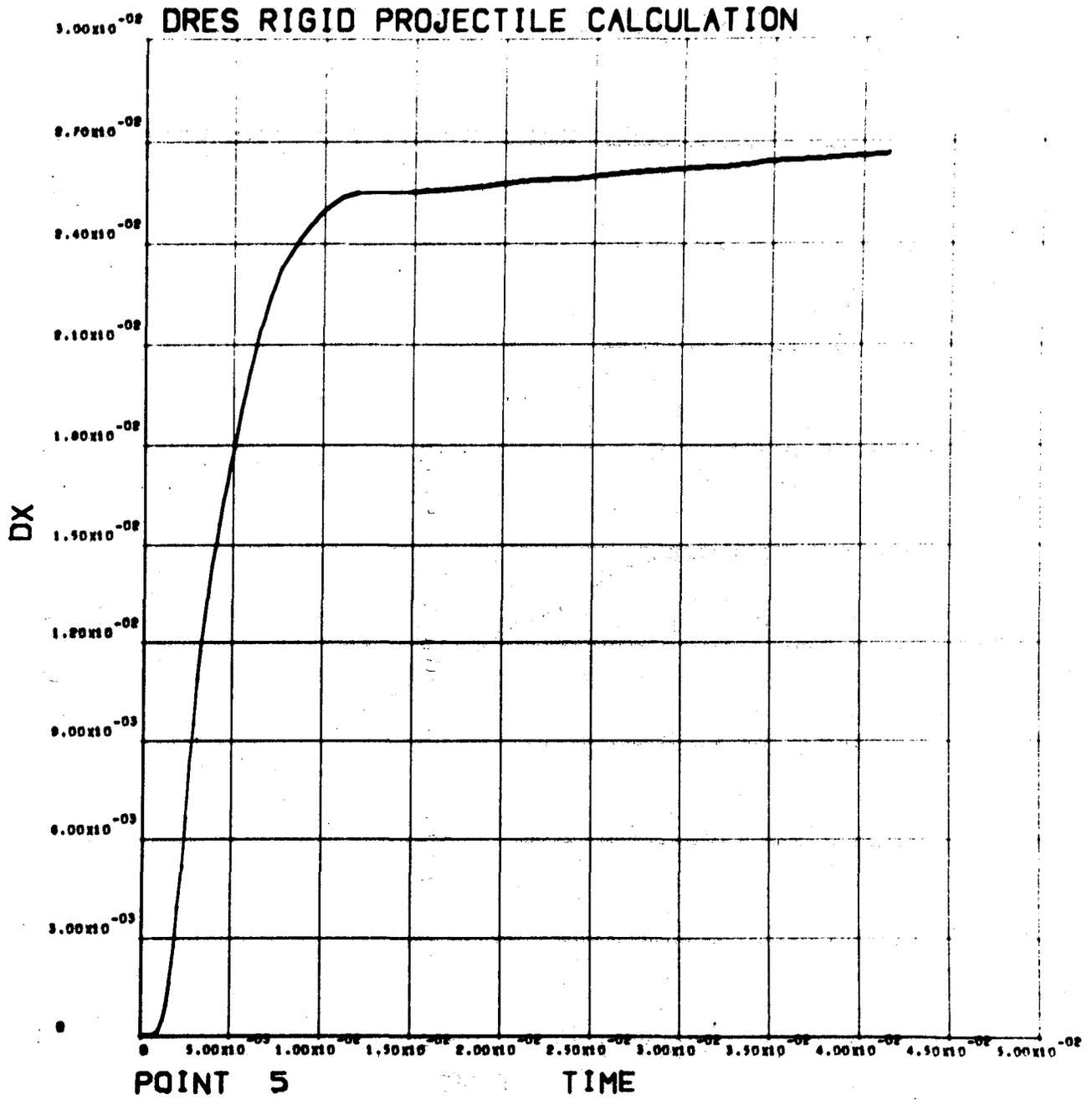


Figure A-27

Radial Displacement (m) versus Time (s) for Particle at Point 5, Z = 0.1 m, R = 0.15 m.

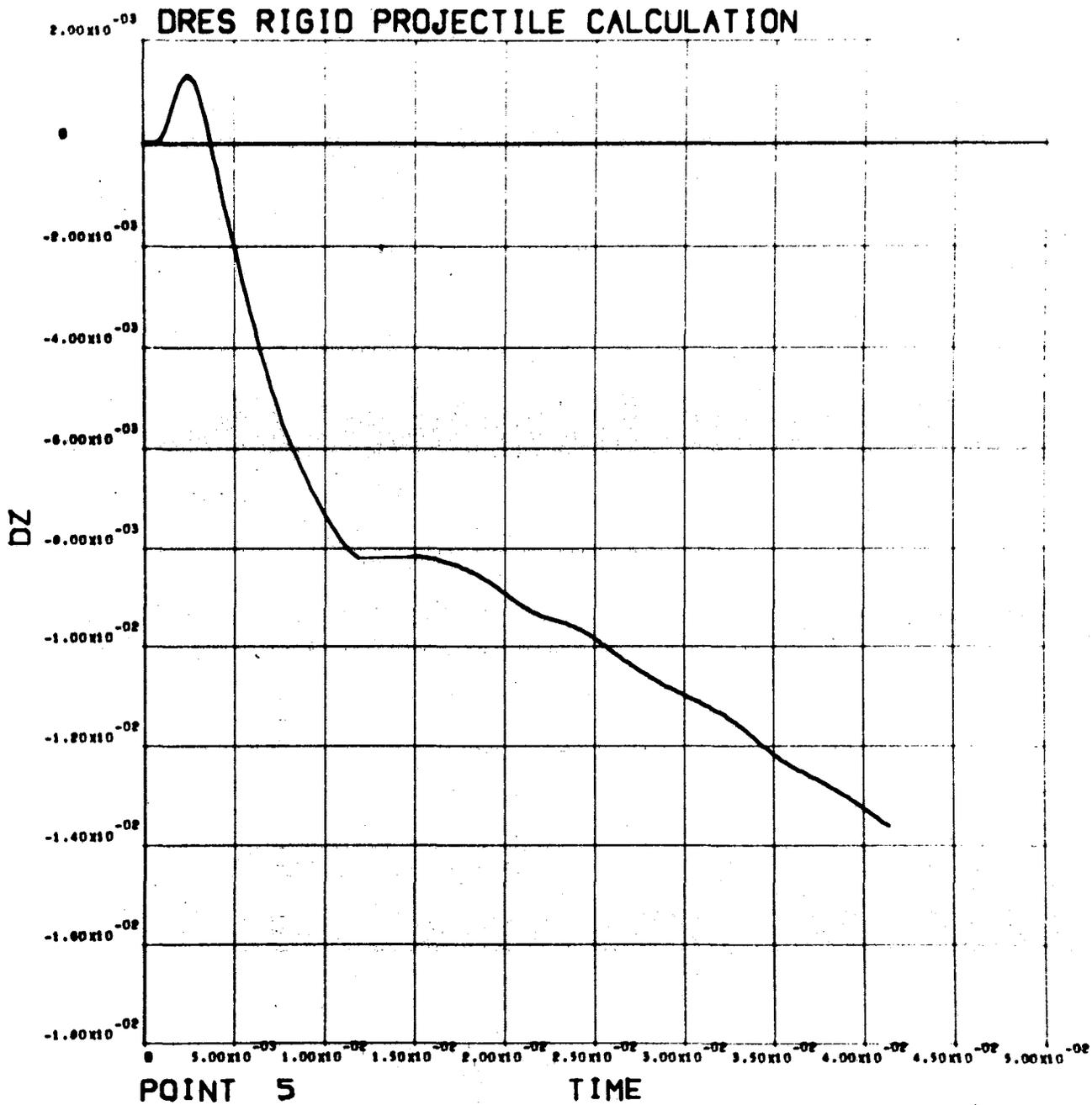


Figure A-28

Axial Displacement (m) versus Time (s) for Particle at Point 5, Z = 0.1 m, R = 0.15 m.

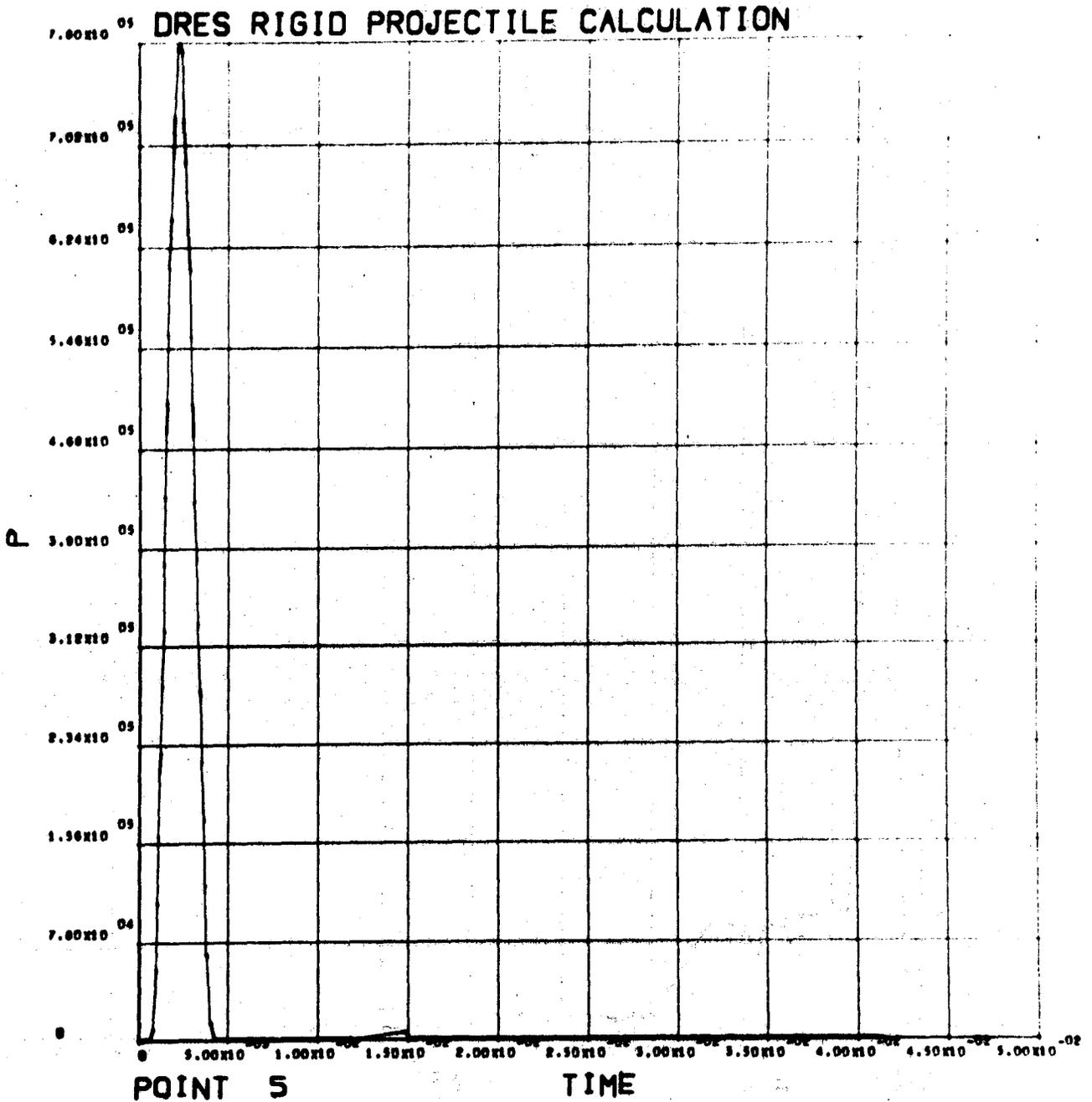


Figure A-29

Pressure (Pa) versus Time (s) for Particle at Point 5, Z = 0.1 m, R = 0.15 m.

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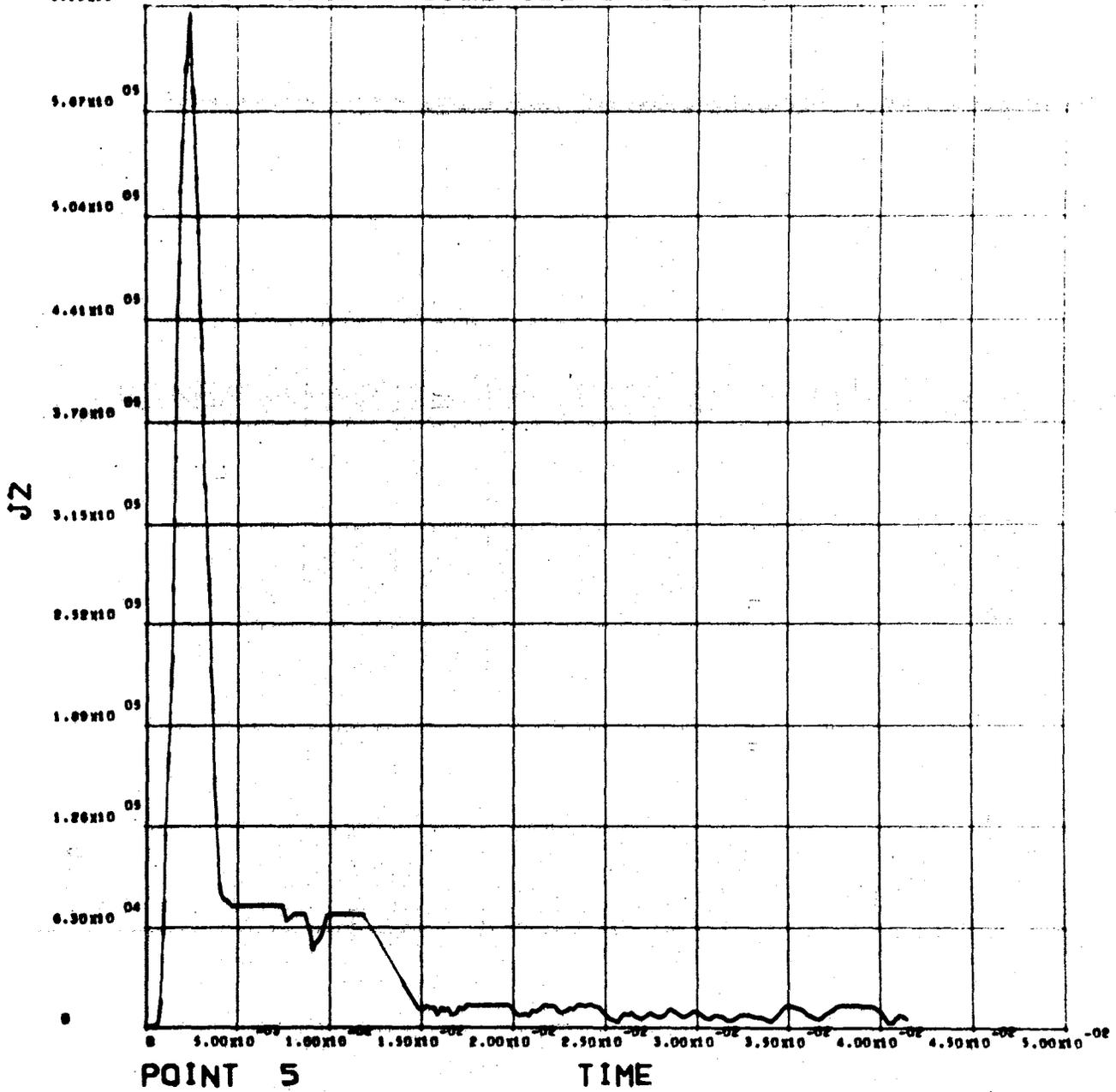


Figure A-30

Deviator Stress J2, History (Pa) for Particle at Point 5, Z = 0.1 m, R = 0.15 m, (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

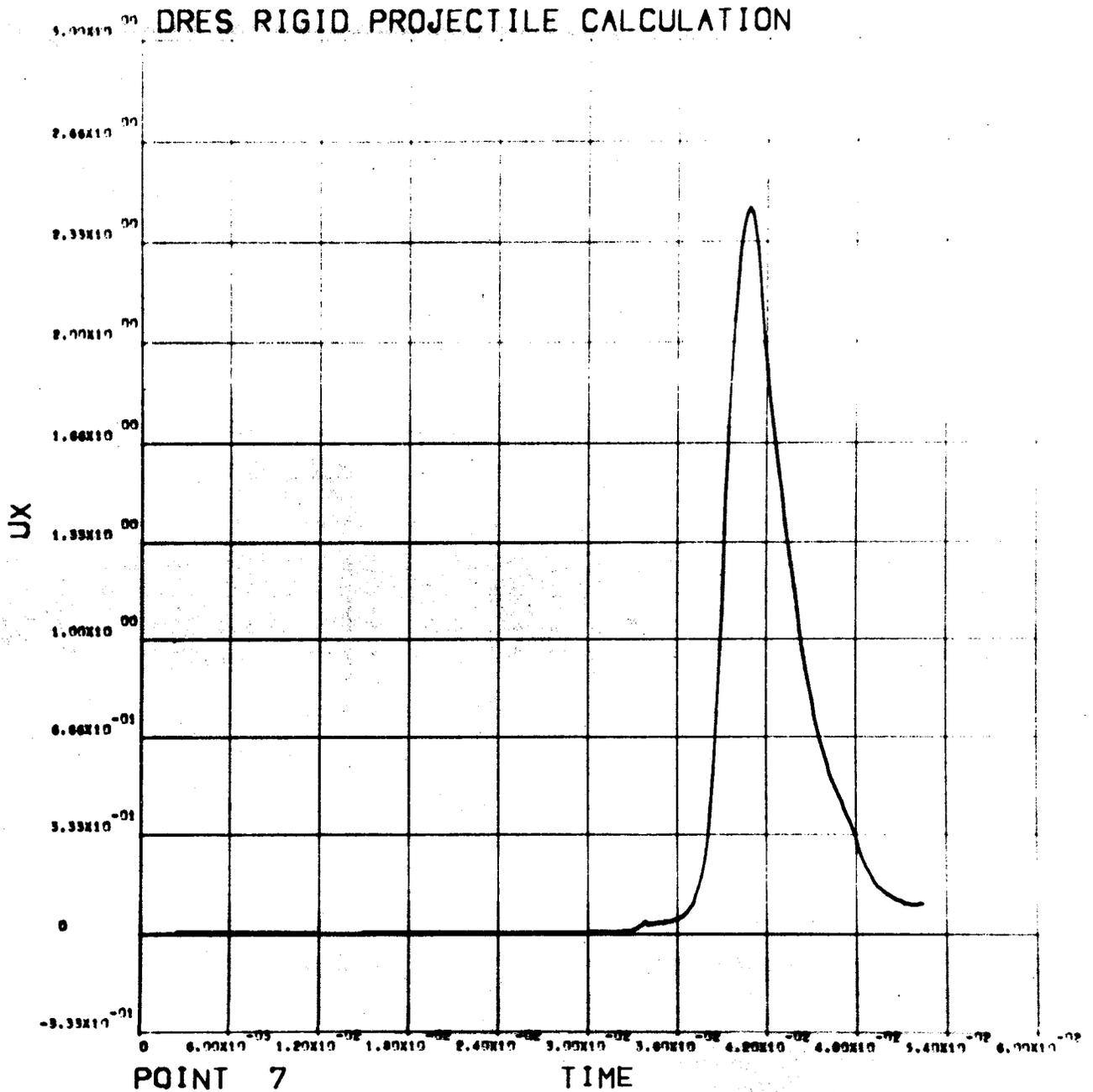


Figure A-31

Radial Velocity (m/s) versus Time (s) for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

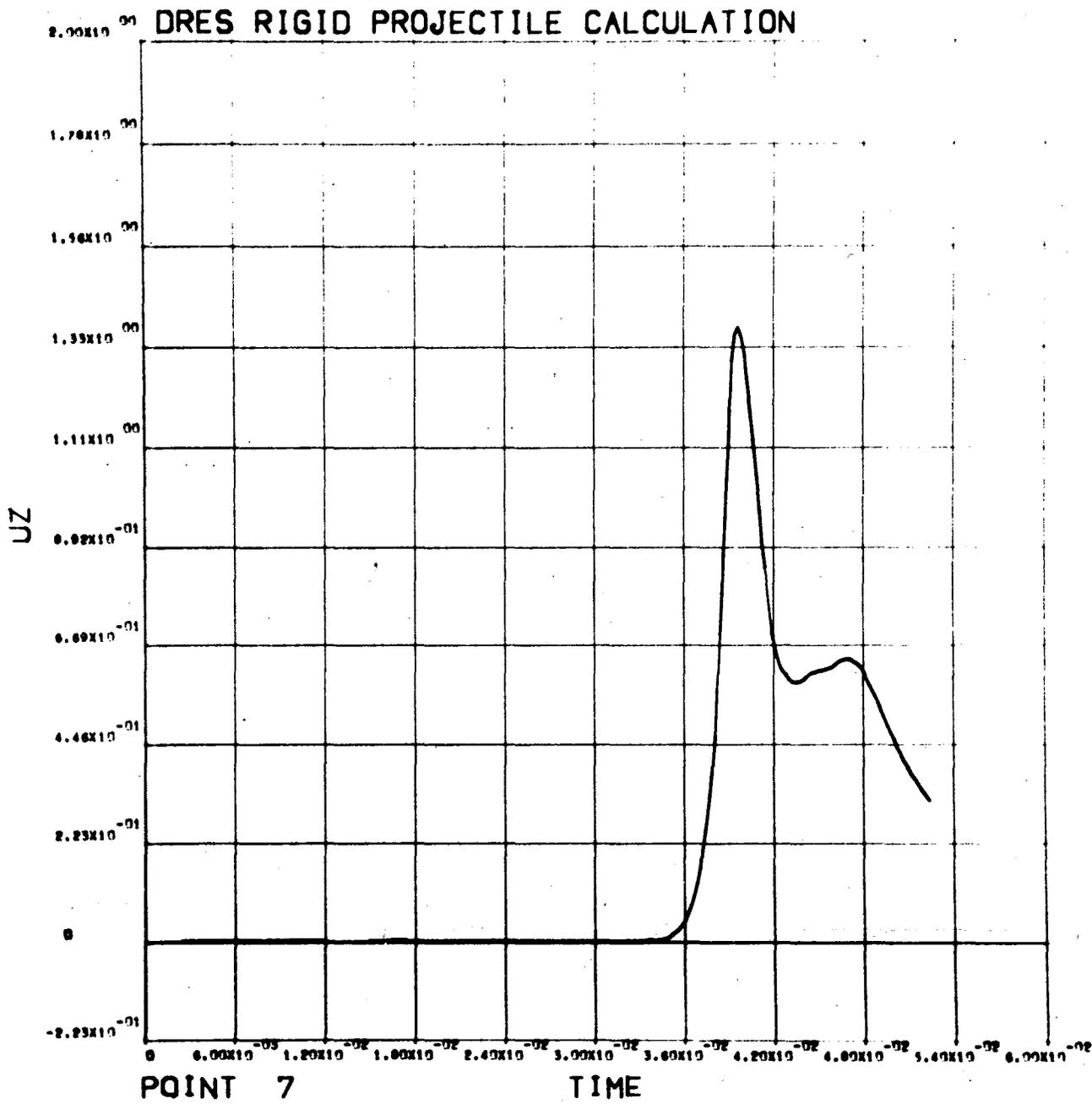


Figure A-32

Axial Velocity (m/s) versus Time (s) for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

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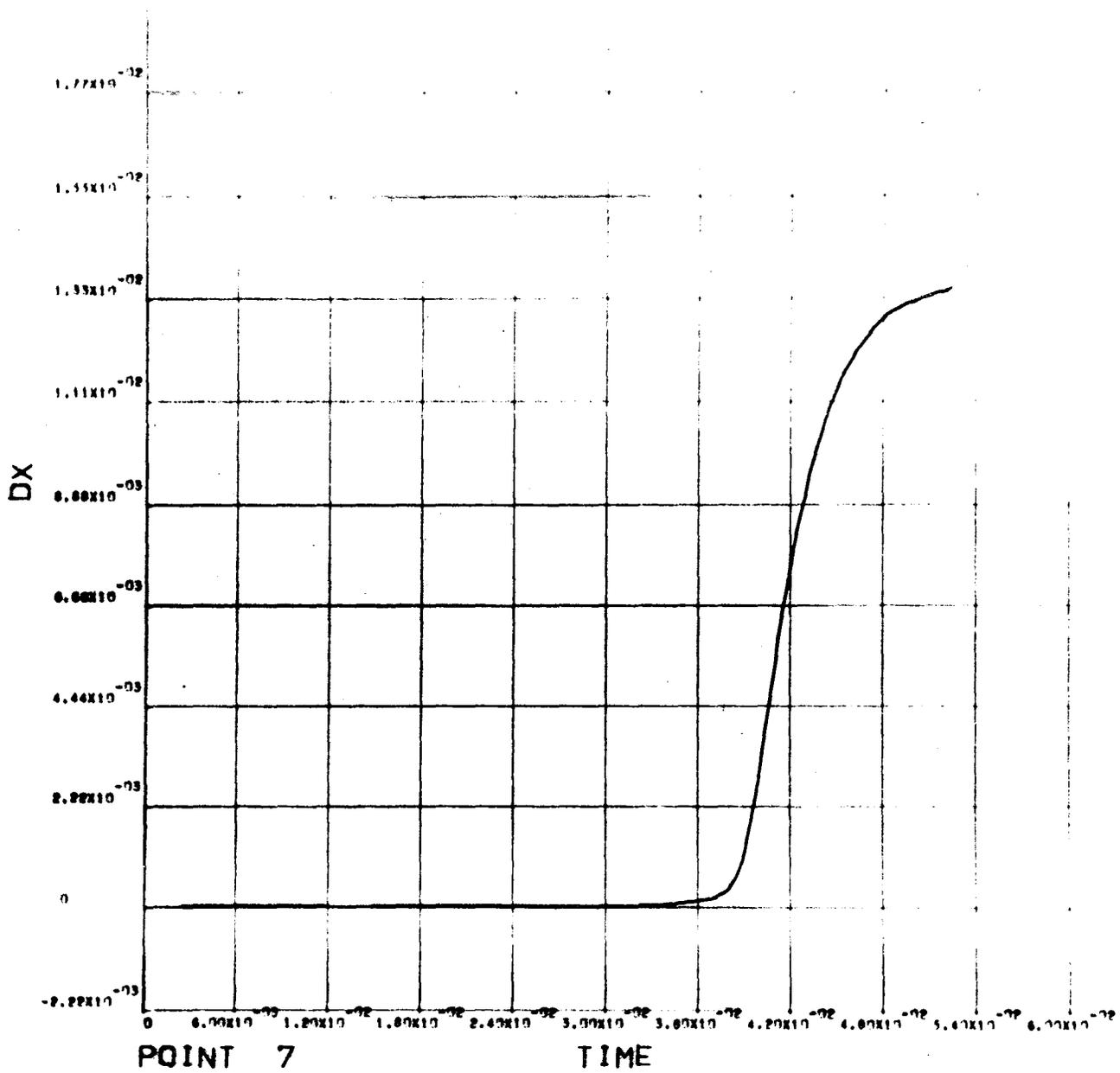


Figure A-33

Radial Displacement (m) versus Time (s) for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

2.10X10<sup>-02</sup> DRES RIGID PROJECTILE CALCULATION

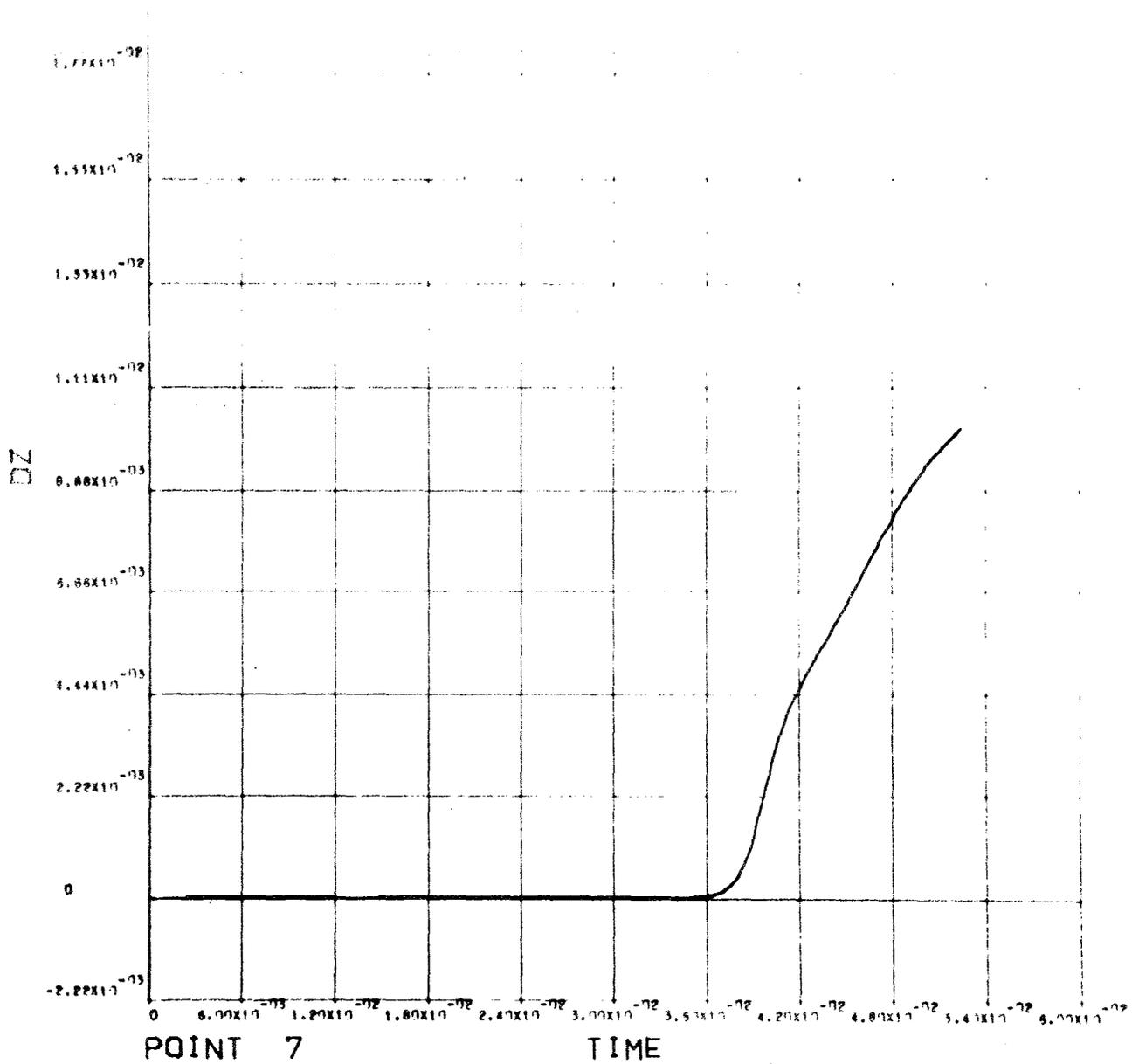


Figure A-34

Axial Displacement (m) versus Time (s) for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

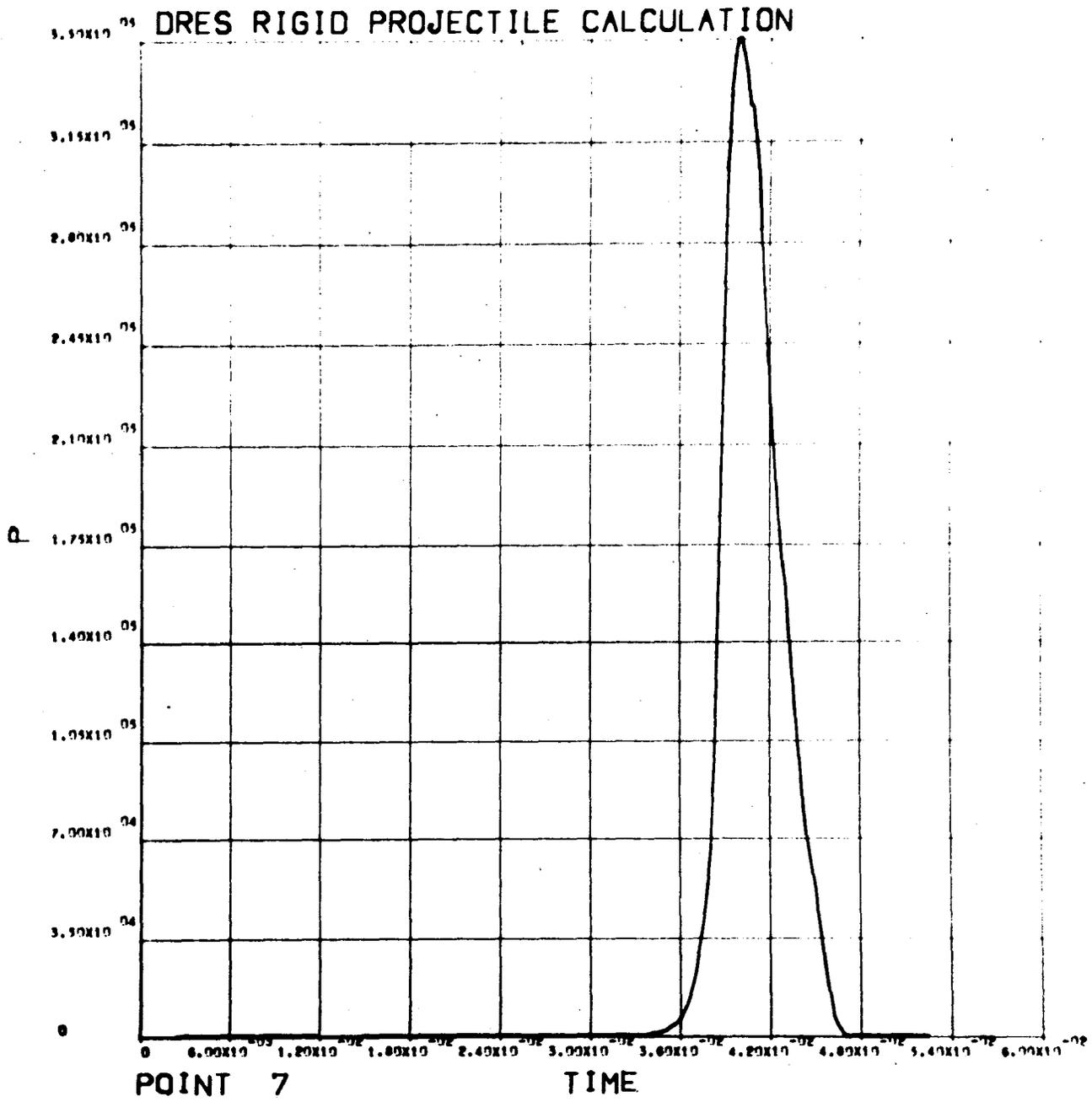


Figure A-35

Pressure (Pa) versus Time (s) for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

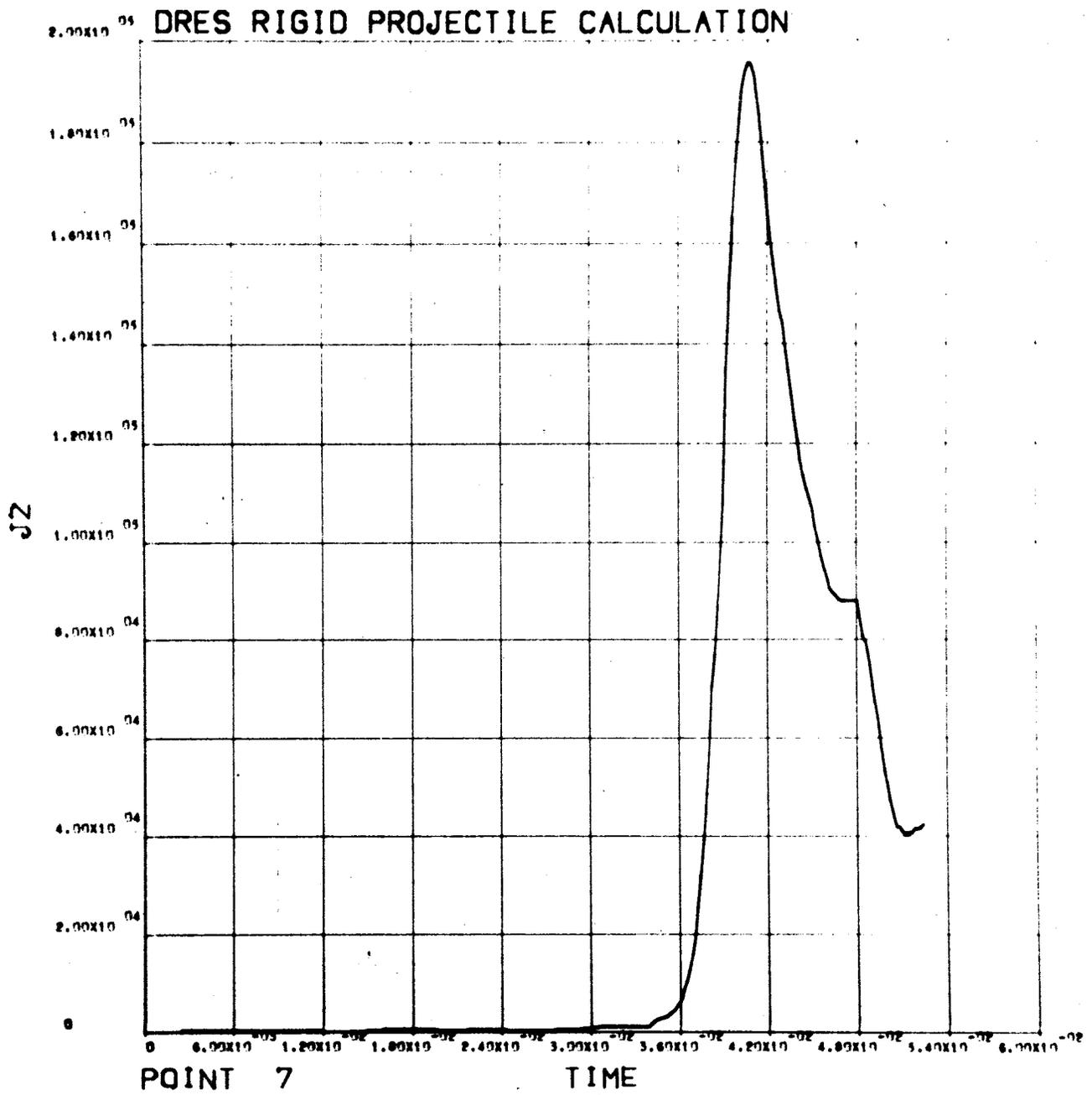


Figure A-36

Deviator Stress, J2, History (Pa) for Particle at Point 7, Z = 5.4 m, R = 0.45 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

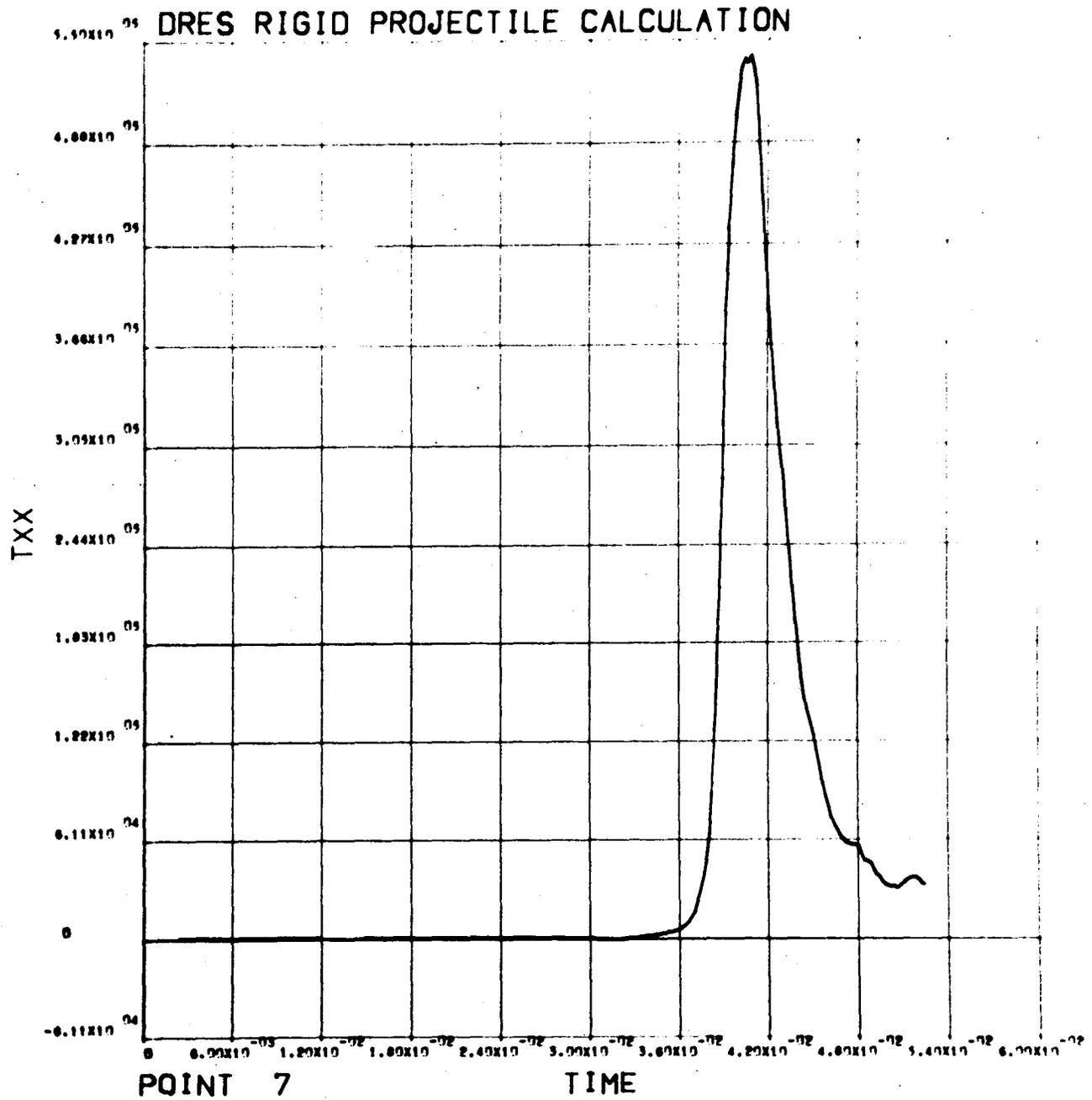


Figure A-37

Radial Stress (Pa) History for Particle at Point 7, Z = 5.4 m, R = 0.45 m.

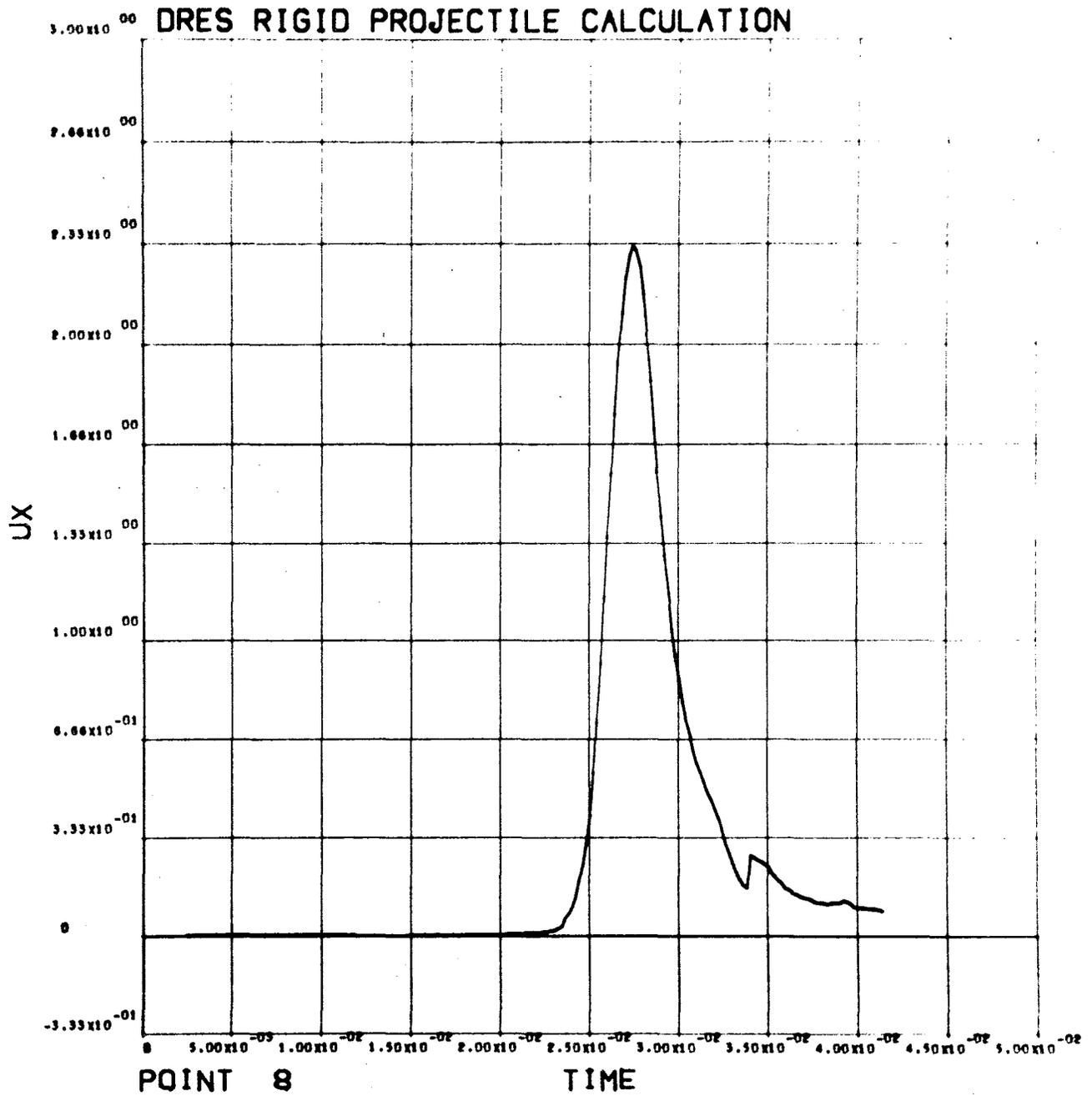


Figure A-38

Radial Velocity (m/s) versus Time (s) for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

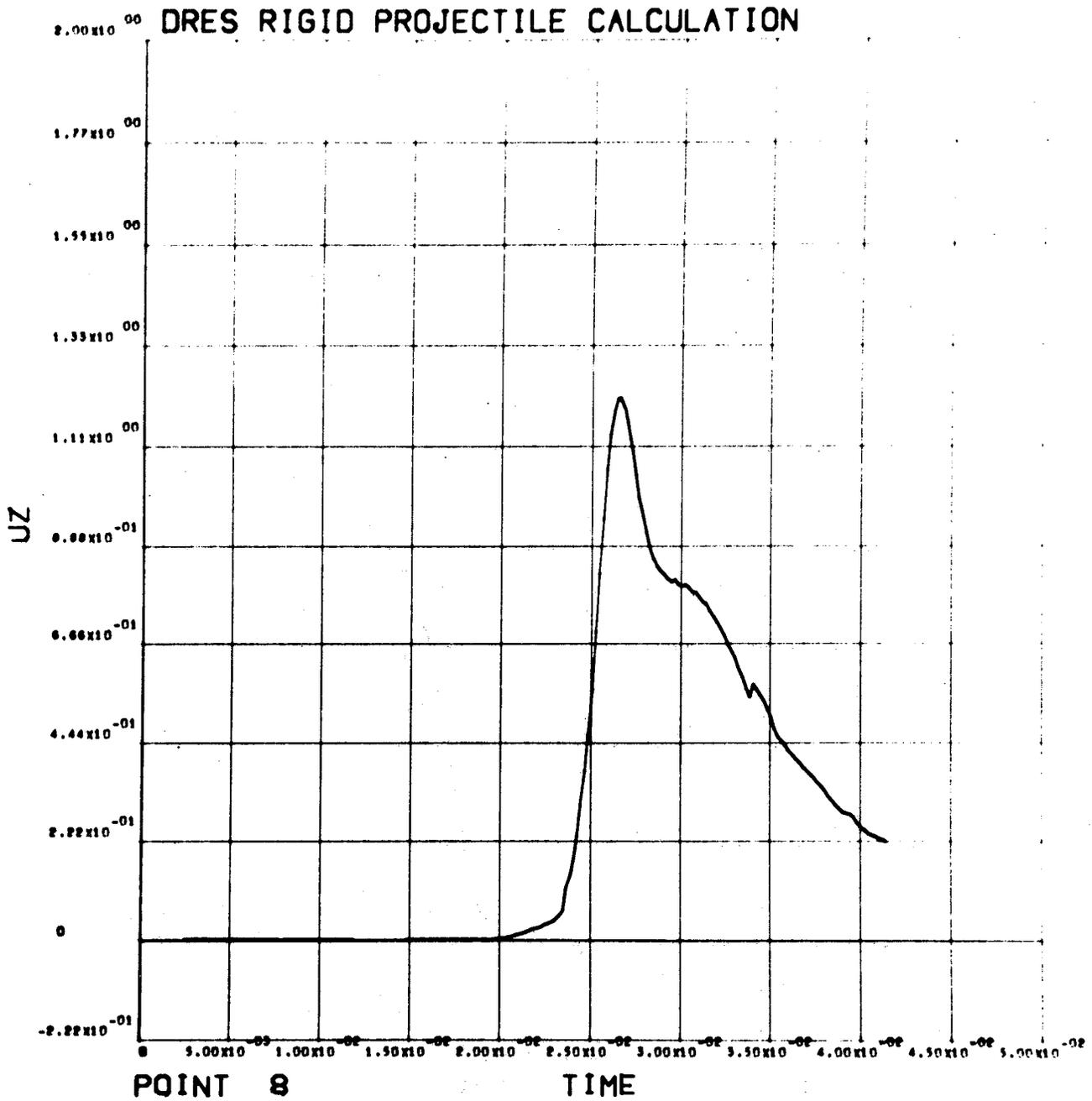


Figure A-39

Axial Velocity (m/s) versus Time (s) for Particle at Point 8; Z = 3.6 m, R = 0.45 m.

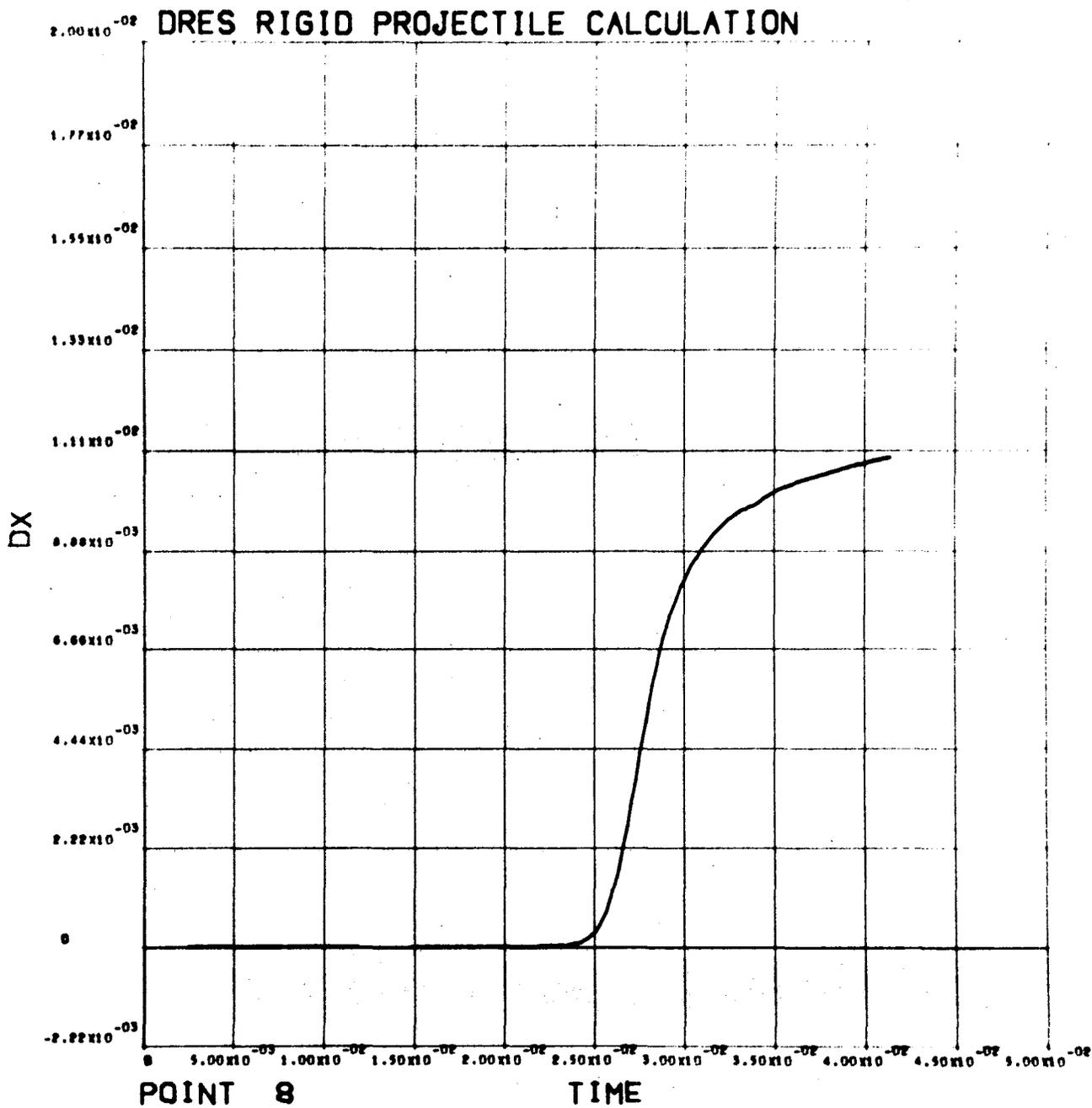


Figure A-40

Radial Displacement (m) versus Time (s) for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

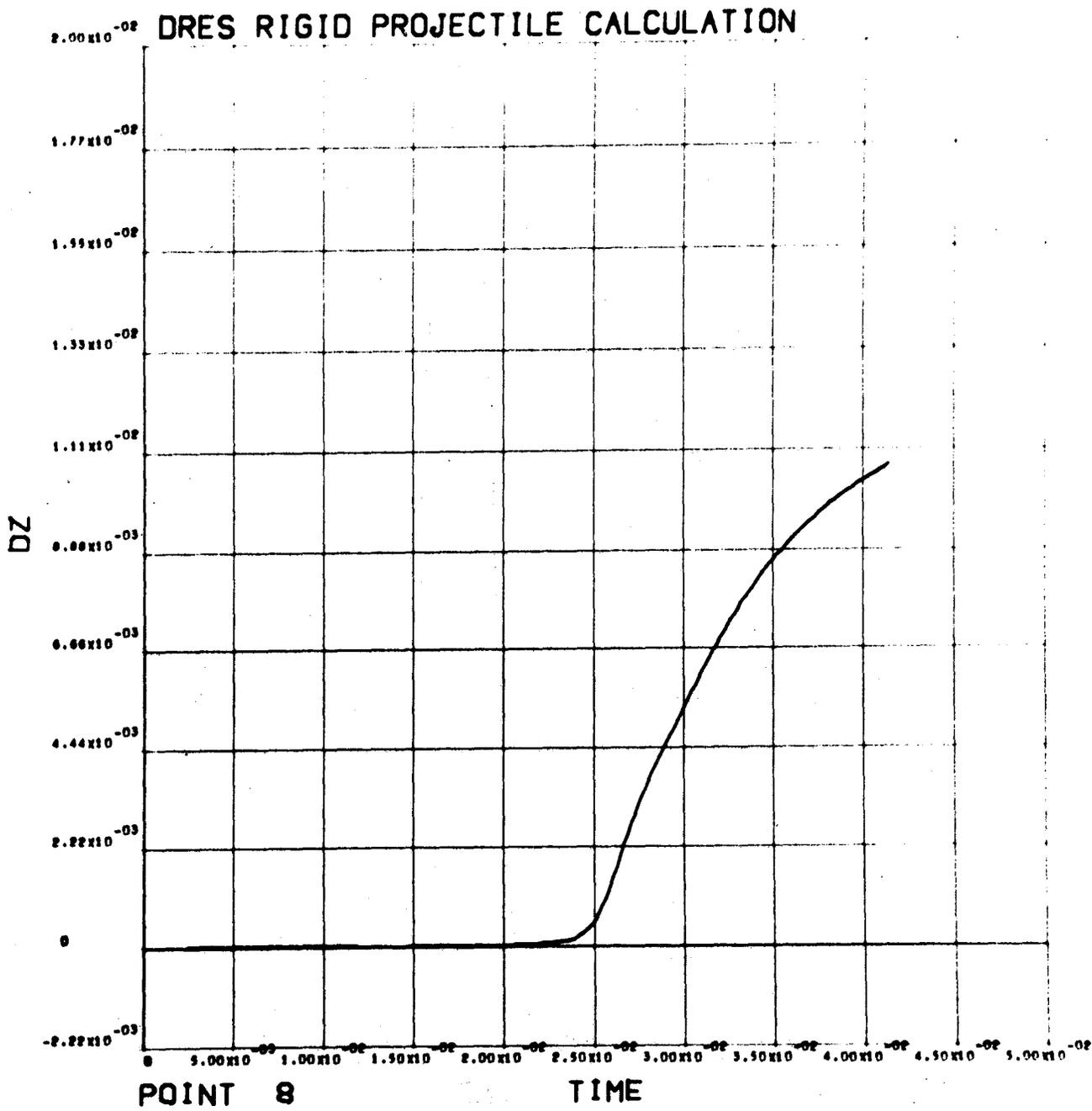


Figure A-41

Axial Displacement (m) versus Time (s) for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

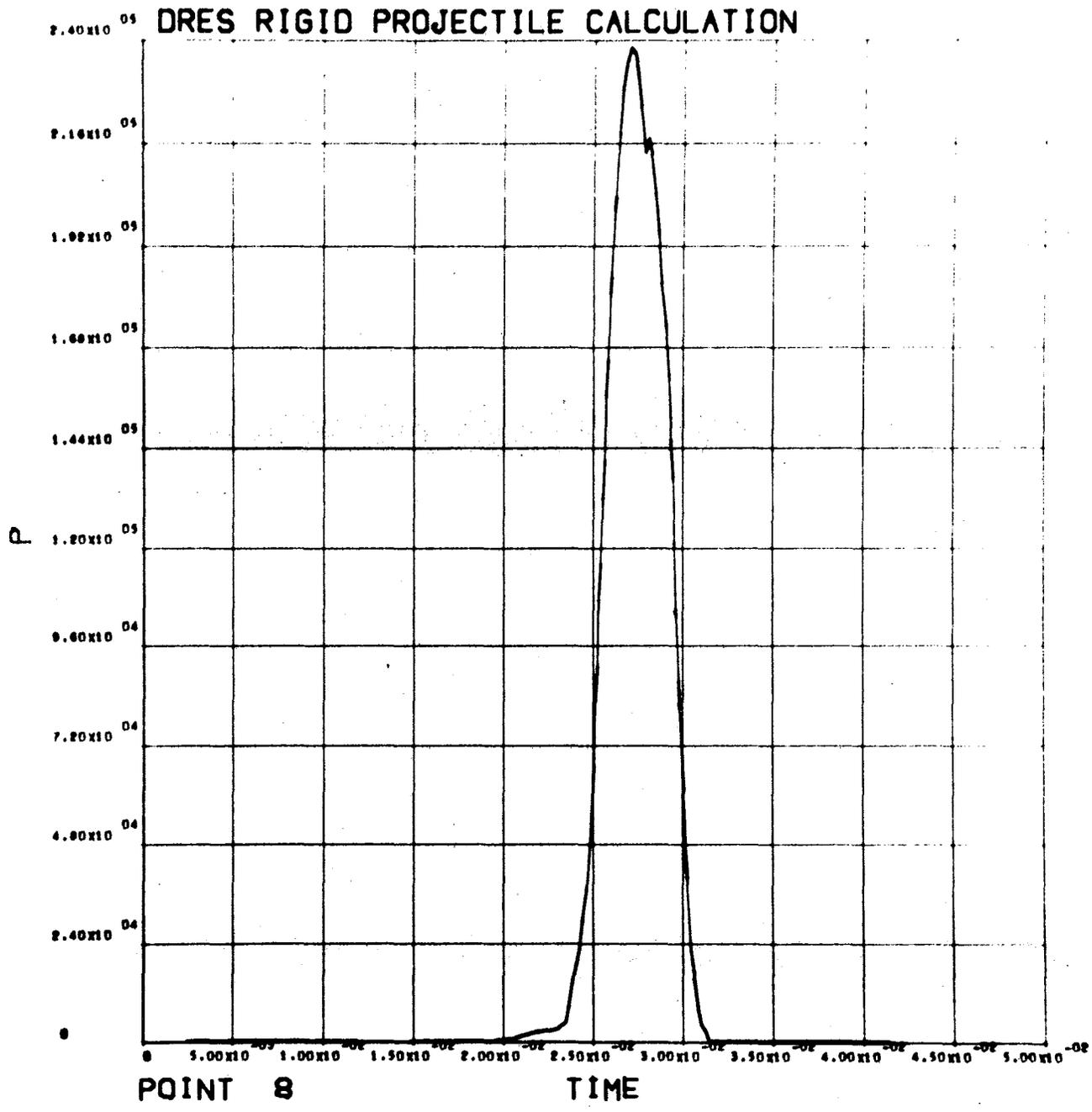


Figure A-42

Pressure (Pa) versus Time (s) for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

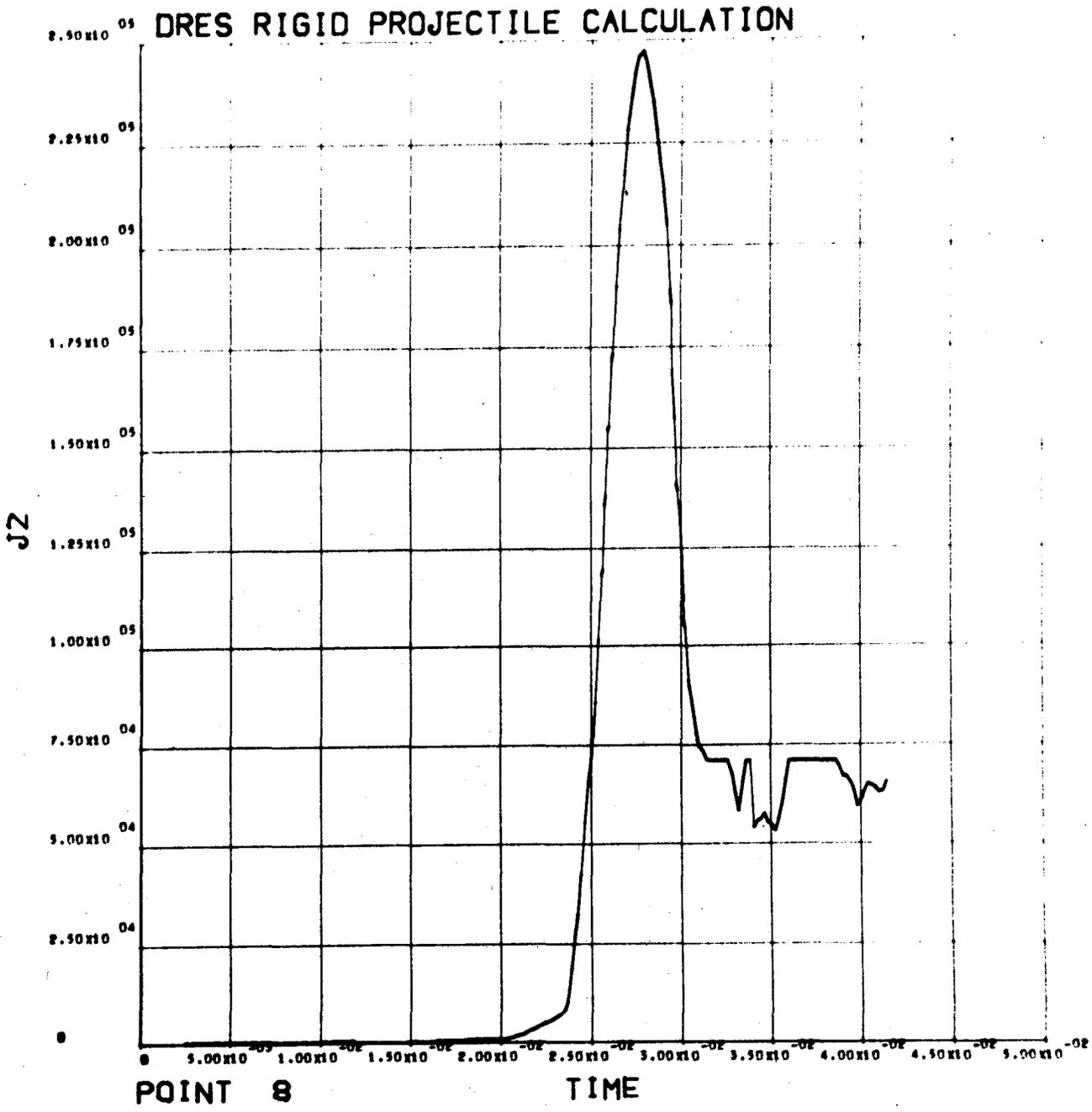


Figure A-43

Deviator Stress, J2, History (Pa) for Particle at Point 8, Z = 3.6 m, R = 0.45 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

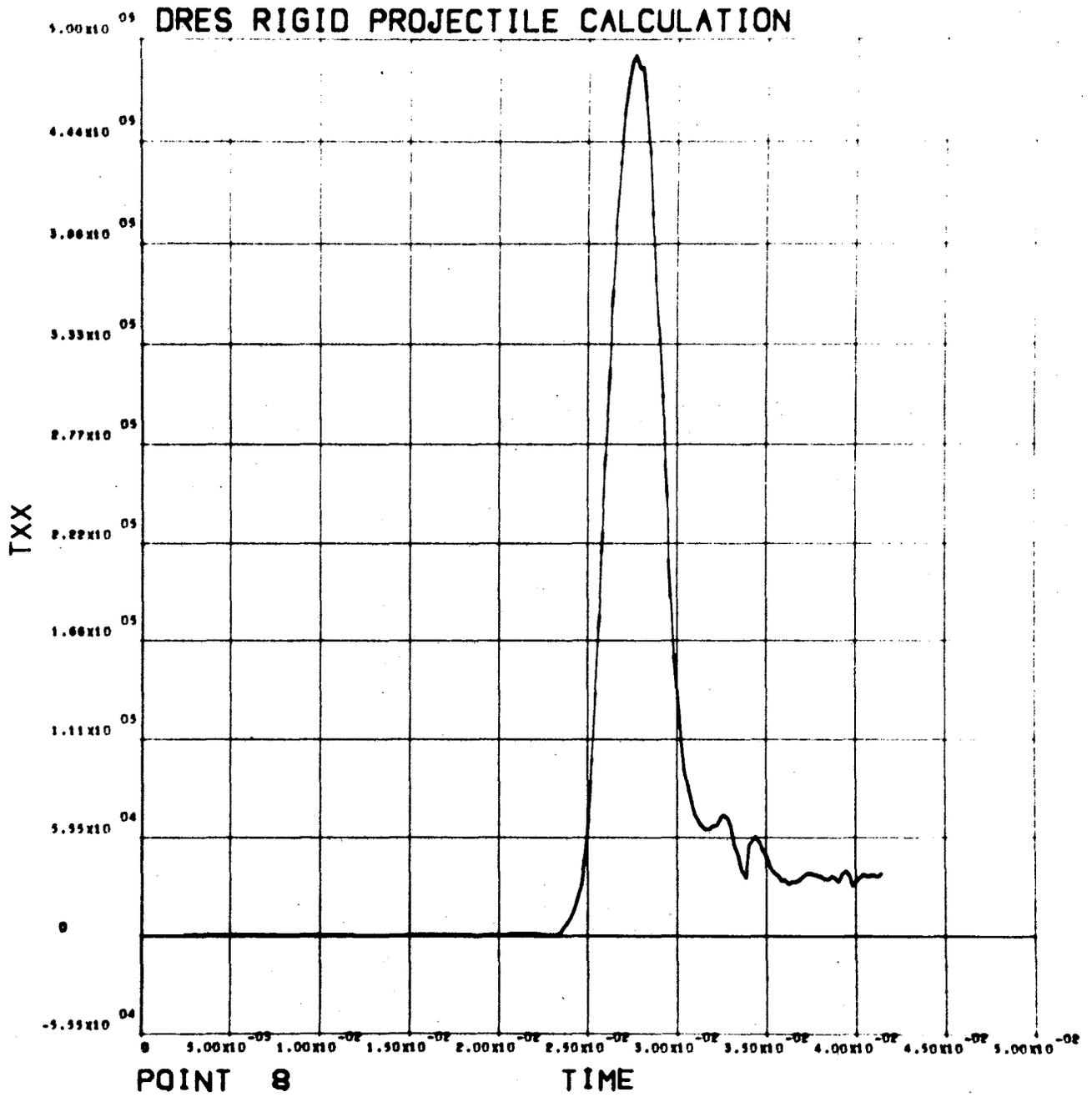


Figure A-44

Radial Stress (Pa) History for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

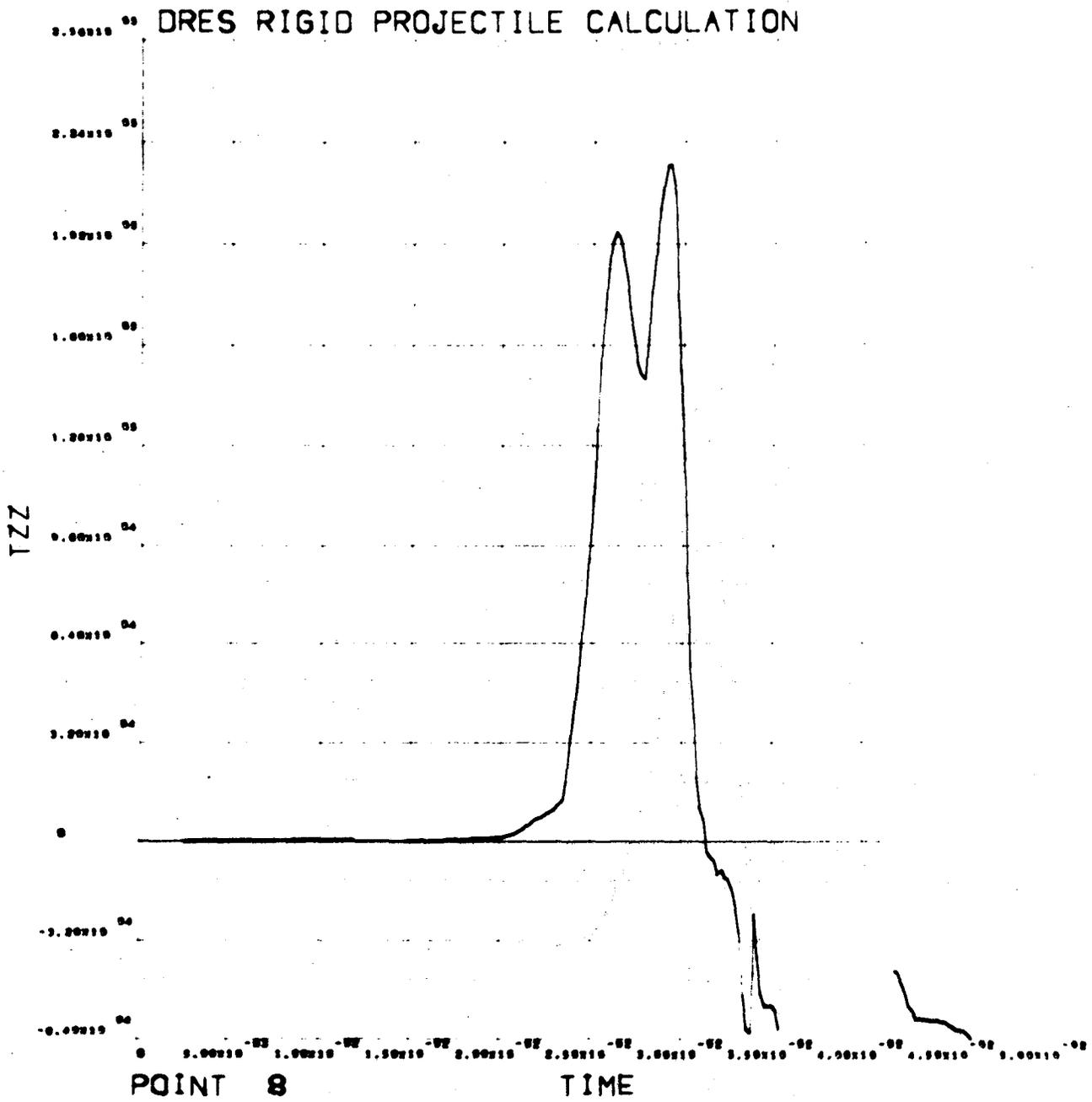


Figure A-45

Axial Stress (Pa) History for Particle at Point 8, Z = 3.6 m, R = 0.45 m.

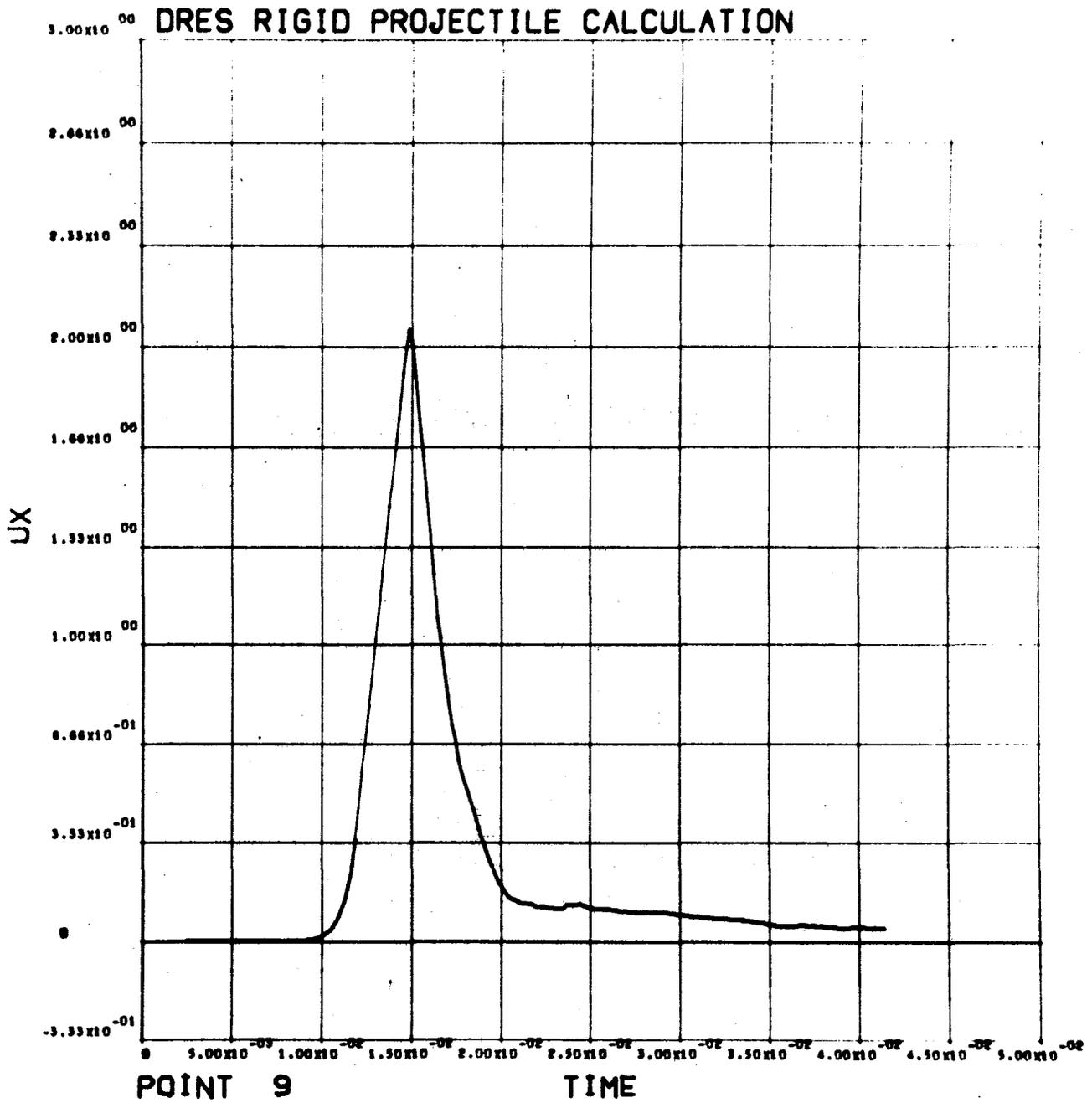


Figure A-46

Radial Velocity (m/s) versus Time (s) for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

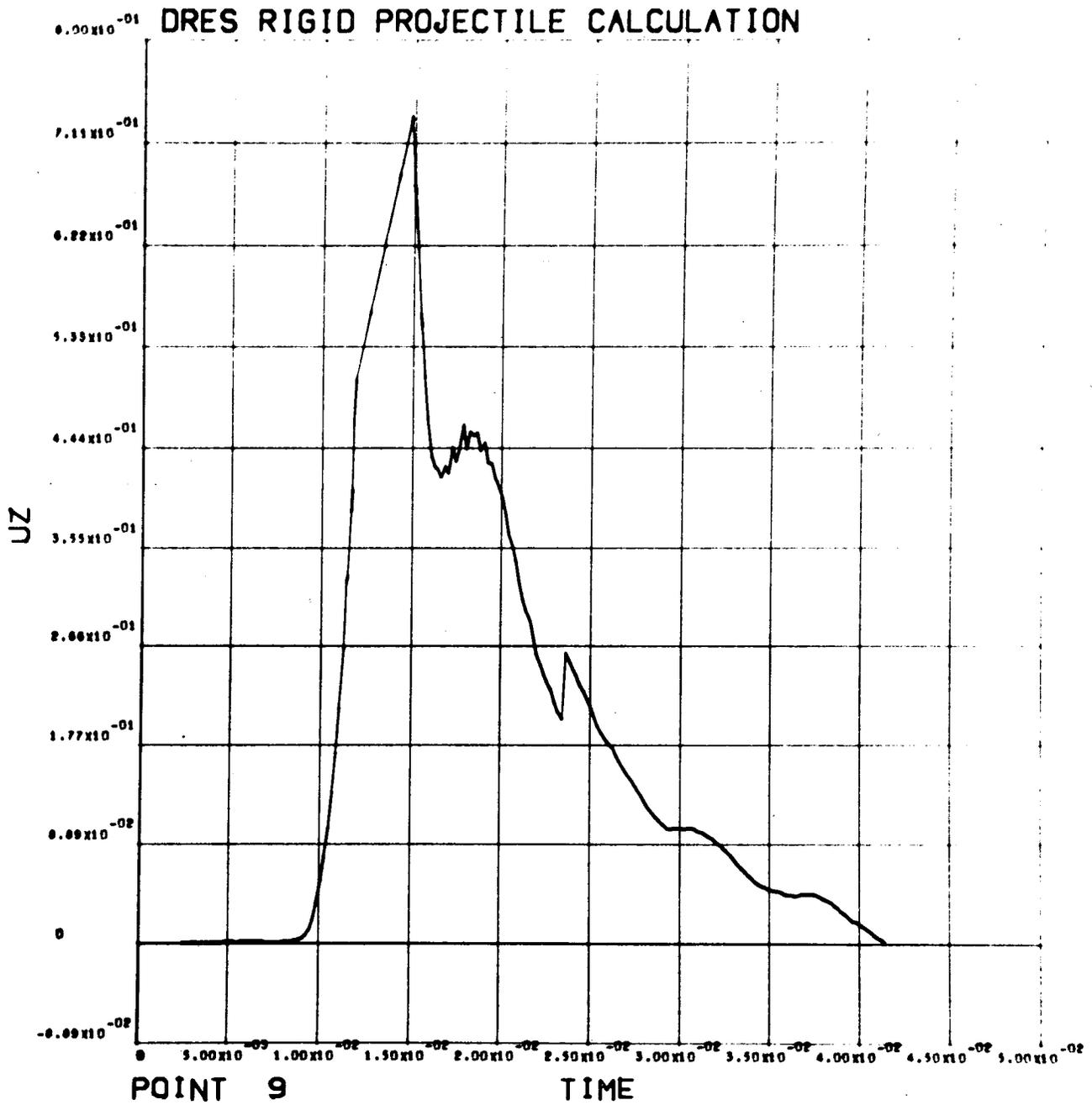


Figure A-47

Axial Velocity (m/s) versus Time (s) for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

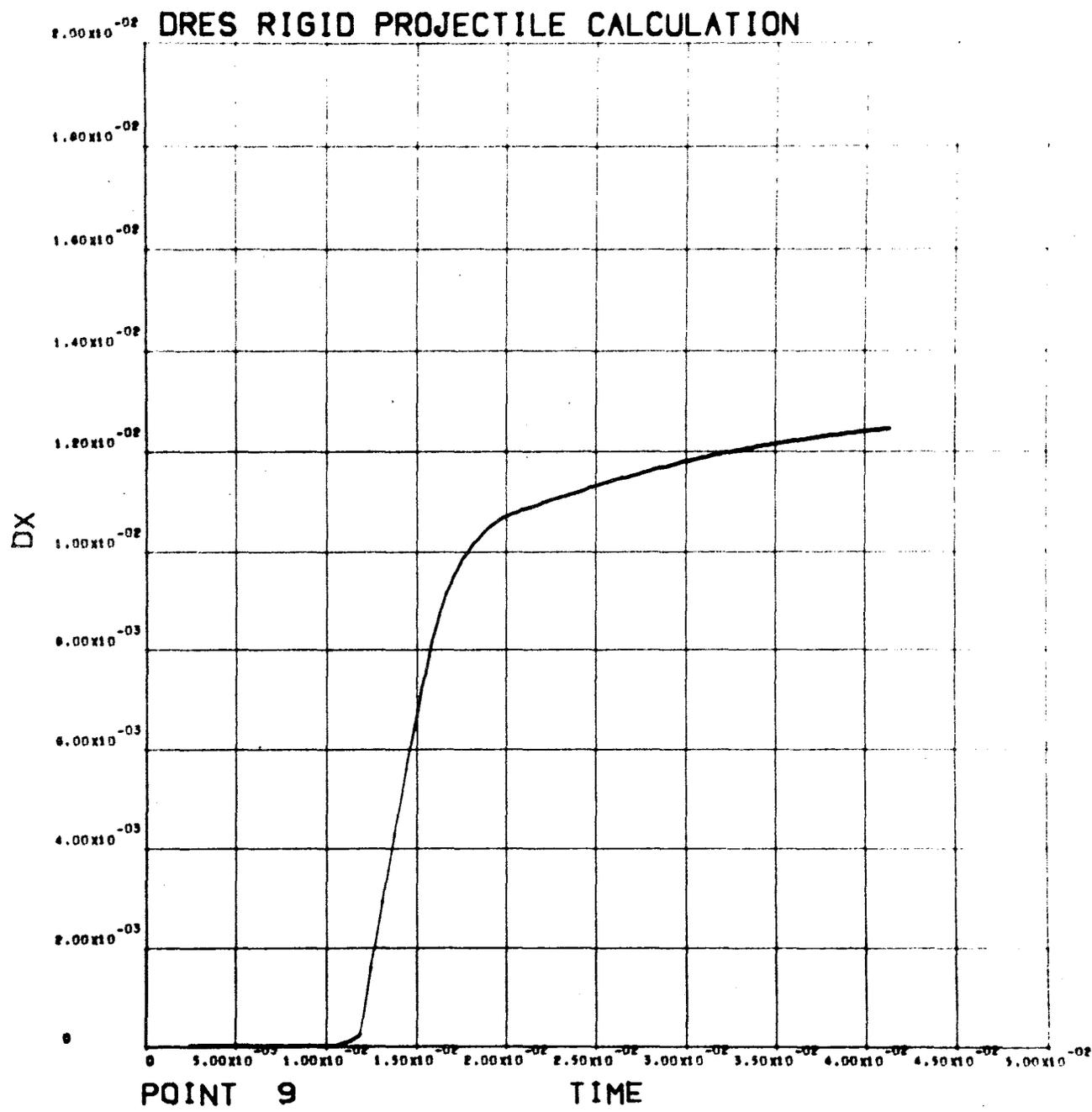


Figure A-48

Radial Displacement (m) versus Time (s) for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

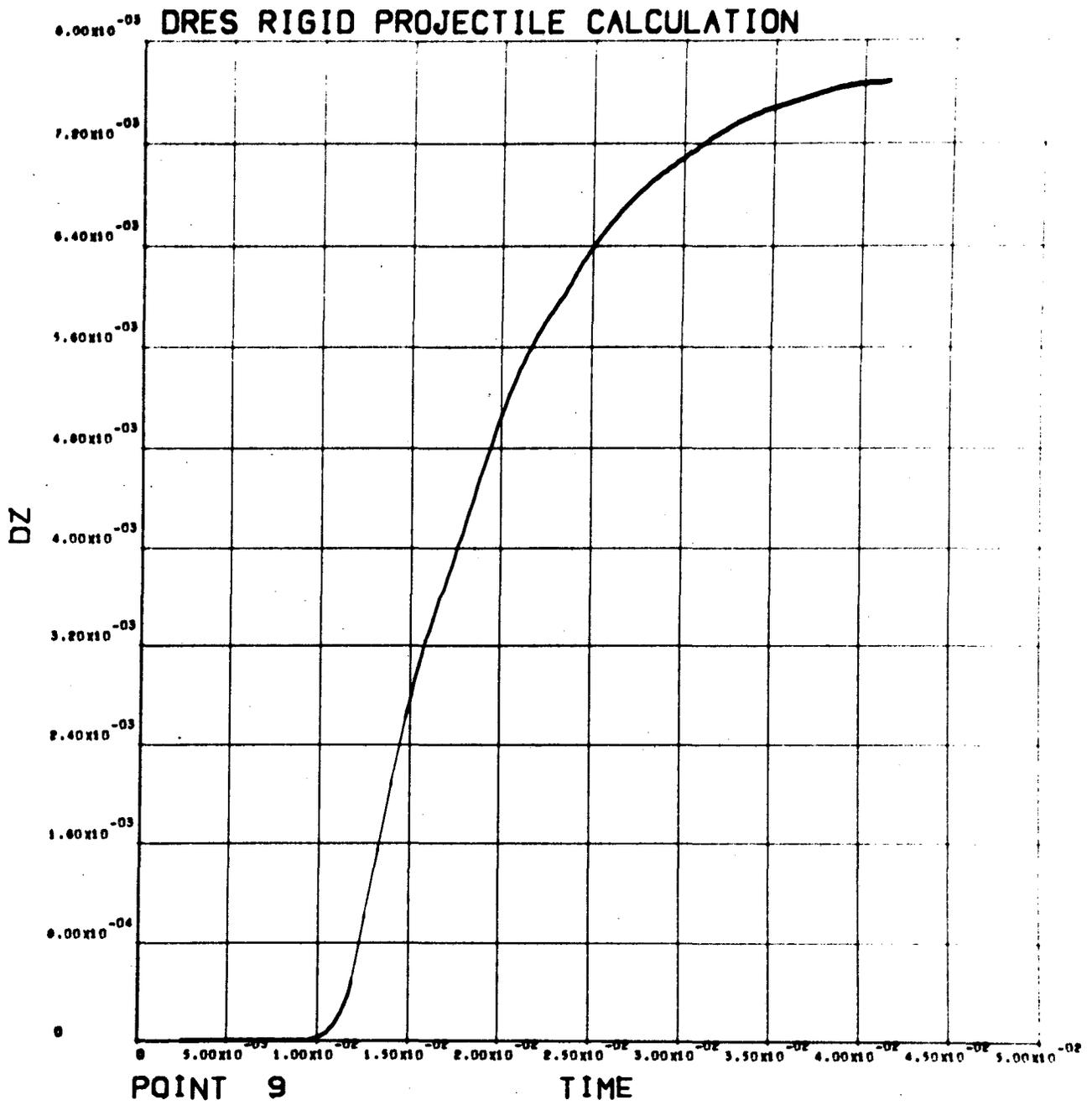


Figure A-49

Axial Displacement (m) versus Time (s) for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

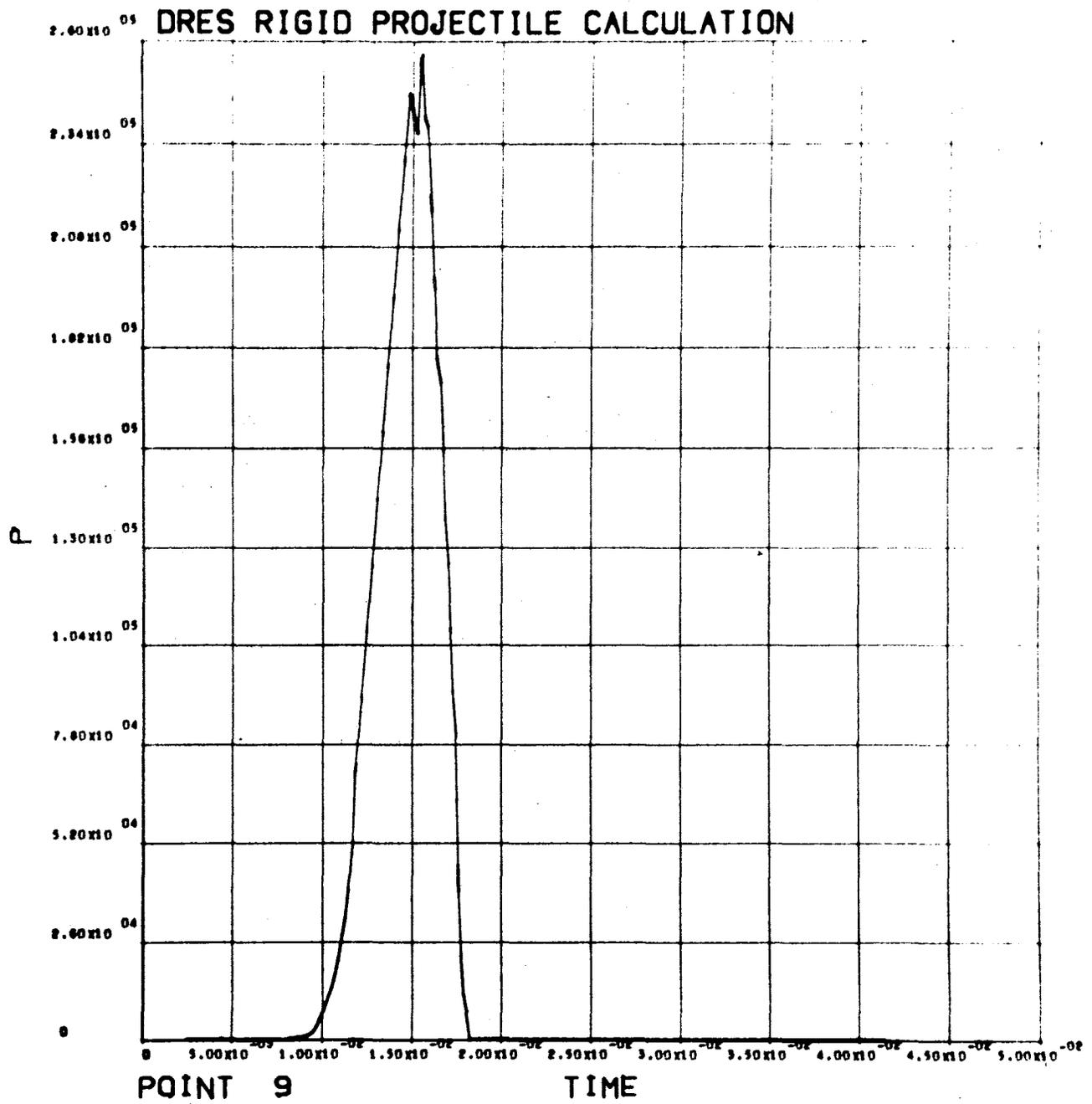


Figure A-50

Pressure (Pa) versus Time (s) for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

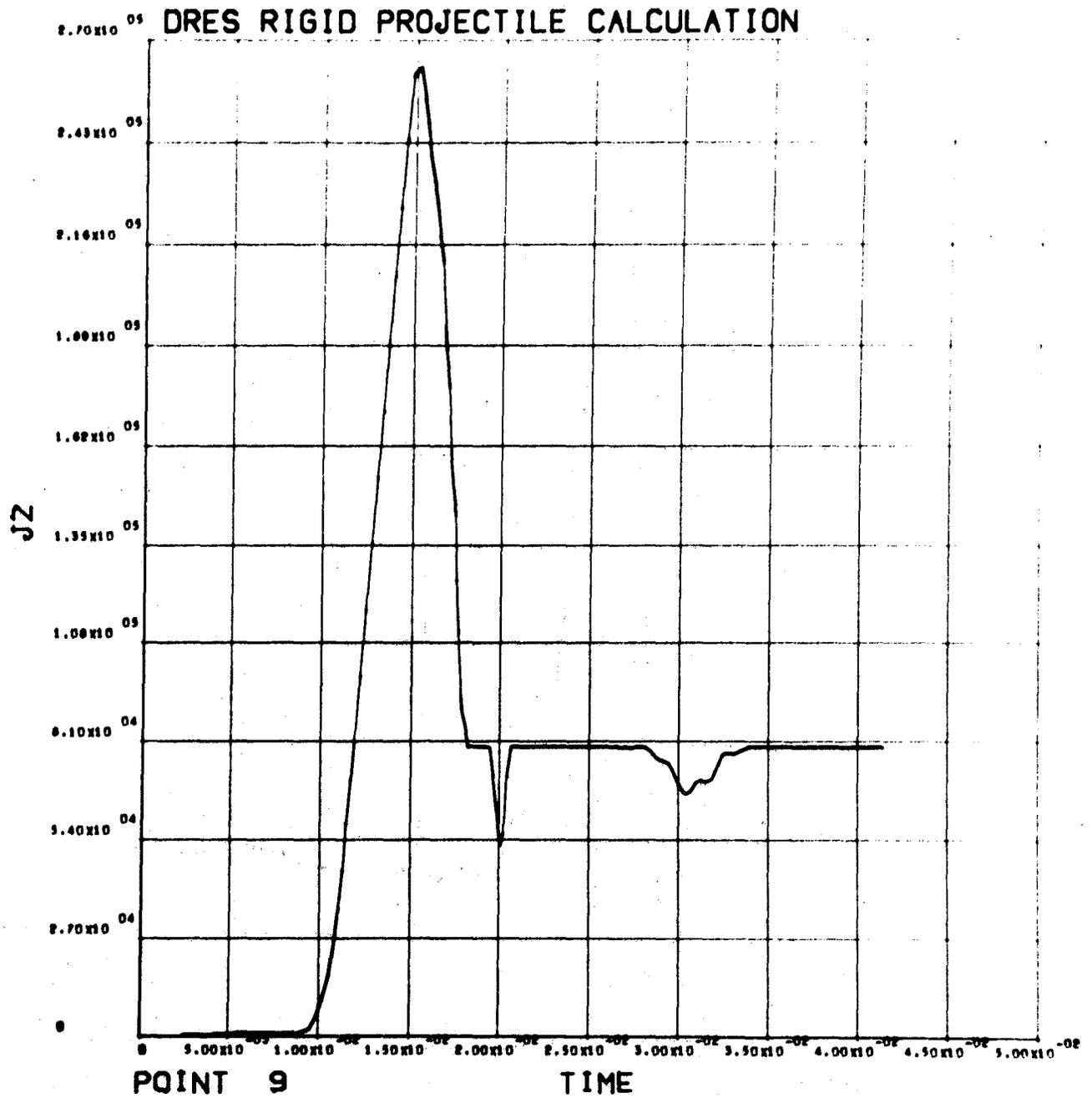


Figure A-51

Deviator Stress, J2, History (Pa) for Particle at Point 9, Z = 1.8 m, R = 0.45 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

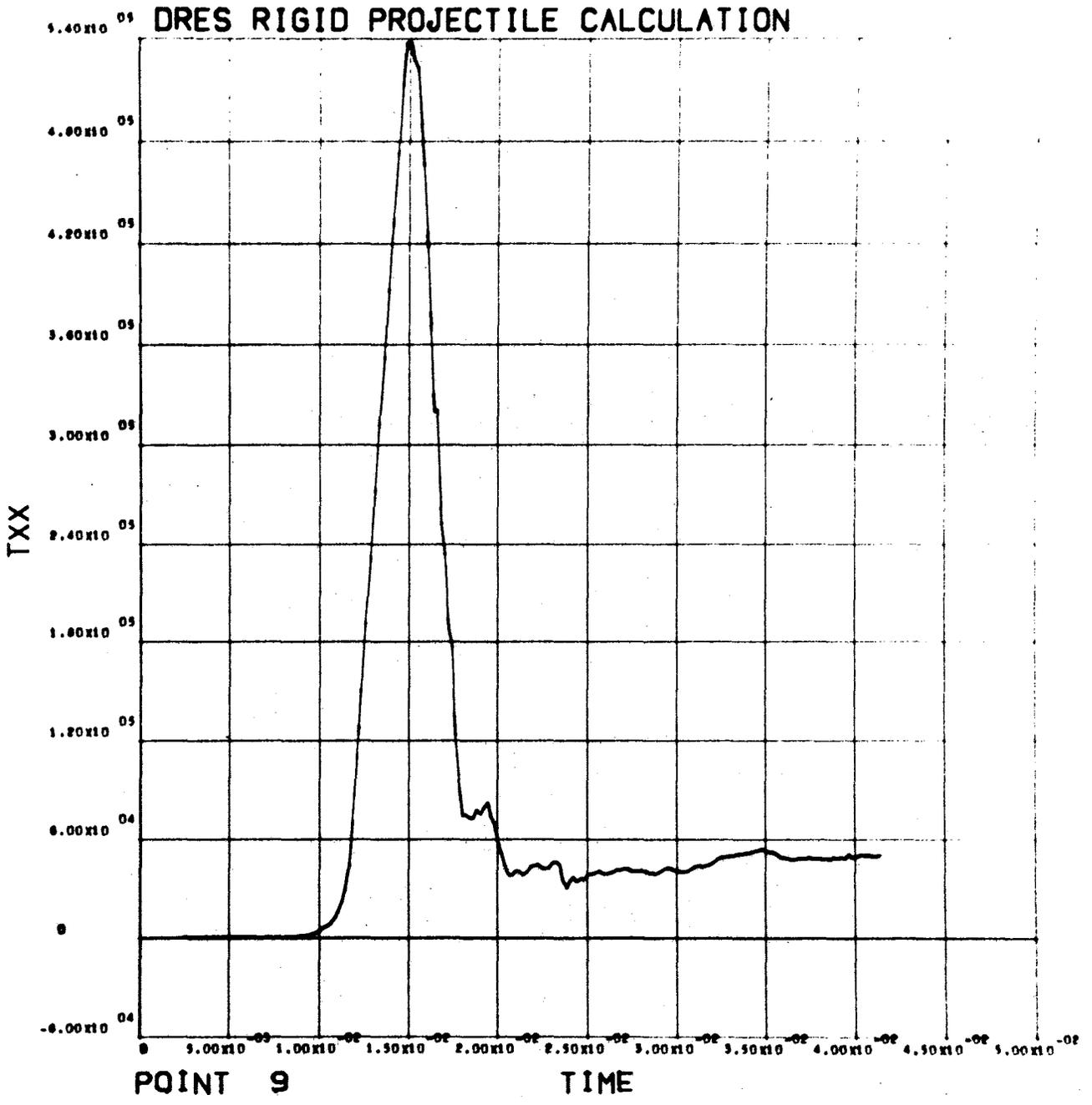


Figure A-52

Radial Stress (Pa) History for Particle at Point 9, Z = 1.8 m, R = 0.45 m.

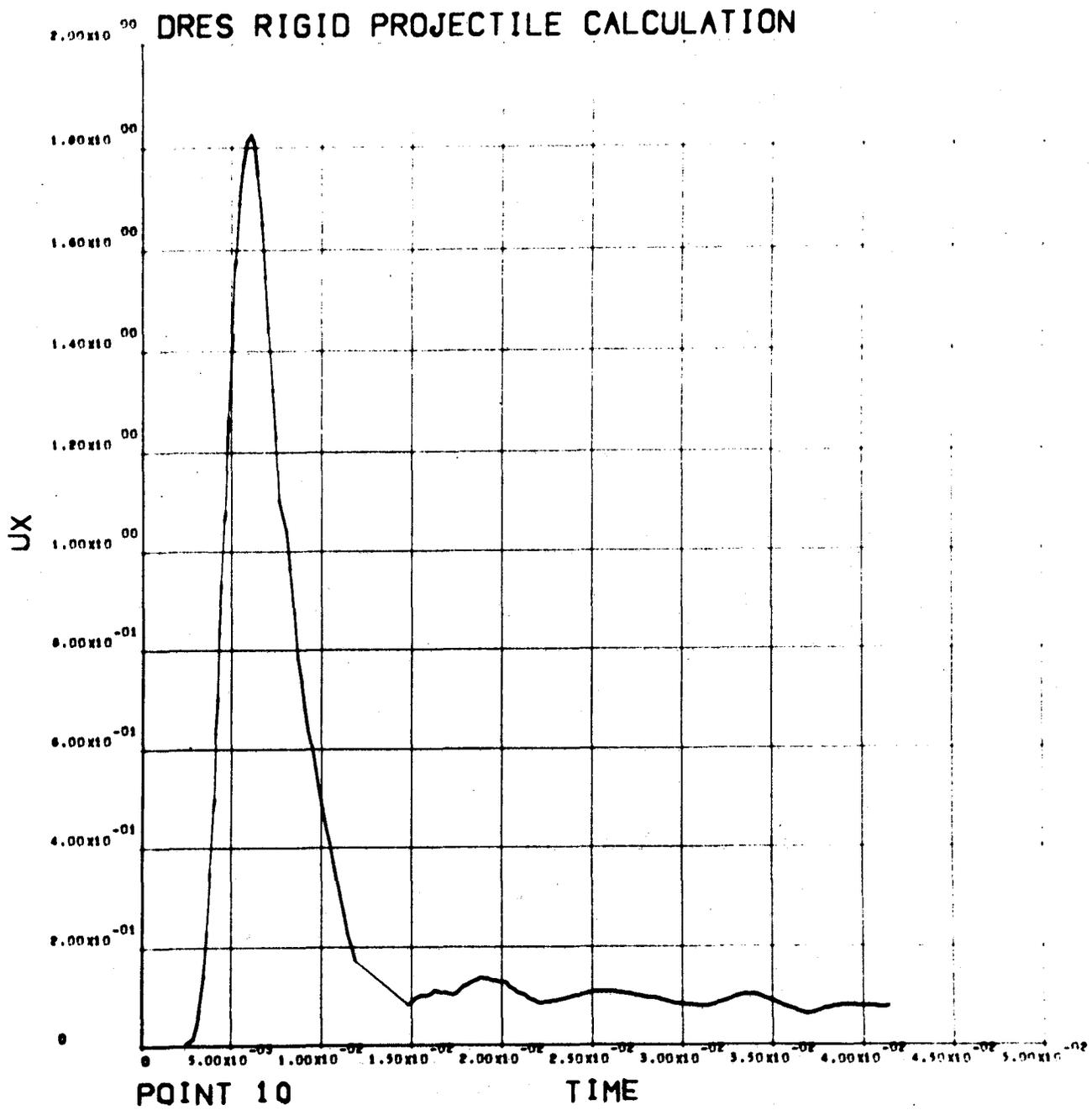


Figure A-53

Radial Velocity (m/s) versus Time (s) for Particle at Point 10, Z = 0.4 m, R = 0.45 m.

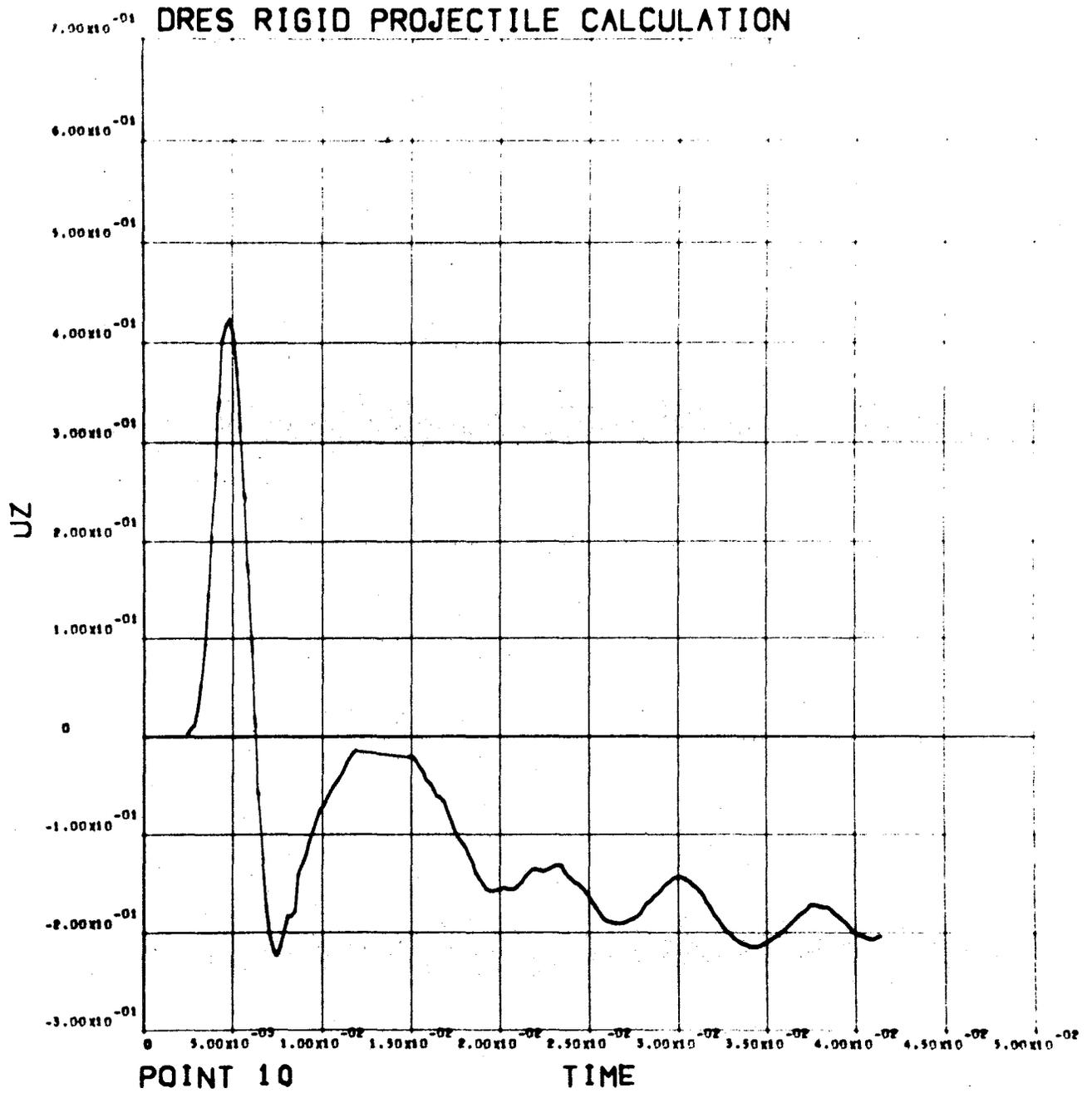


Figure A-54

Axial Velocity (m/s) versus Time (s) for Particle at Point 10, Z = 0.4 m, R = 0.45 m.

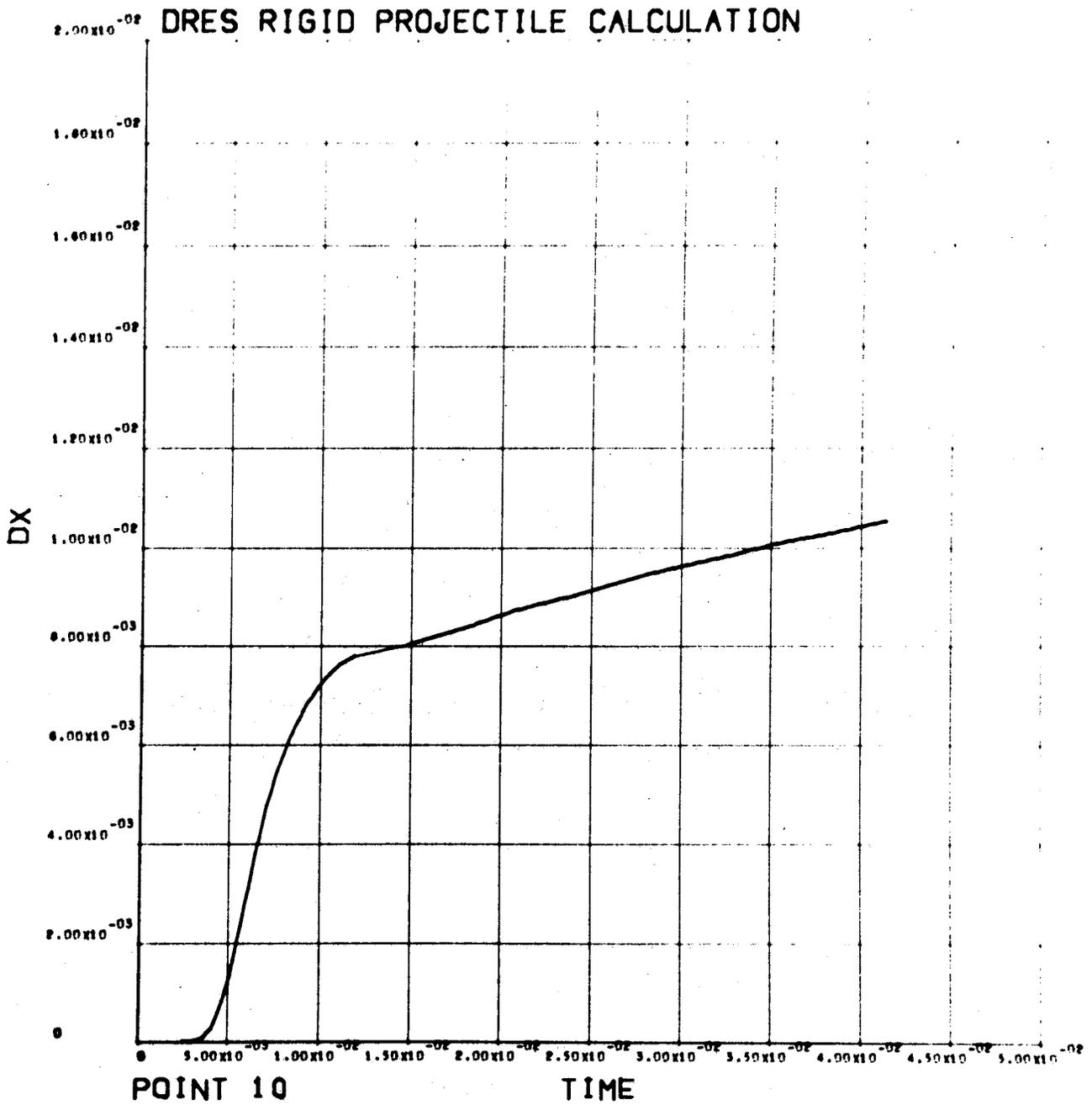


Figure A-55

Radial Displacement (m) versus Time (s) for Particle at Point 10, Z = 0.4 m, R = 0.45 m.

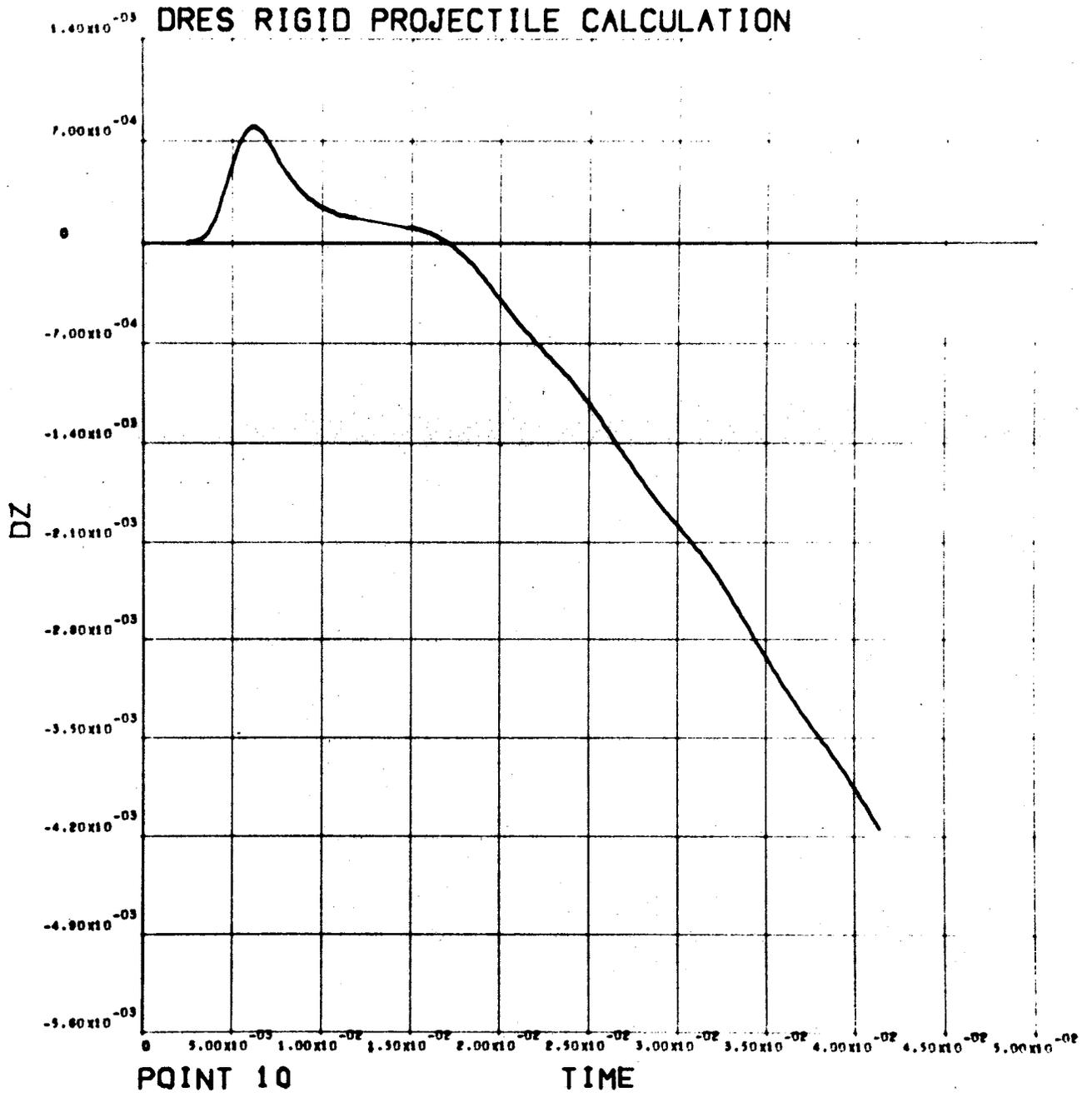


Figure A-56

Axial Displacement (m) versus Time (s) for Particle at Point 10, Z = 0.4 m, R = 0.45 m.

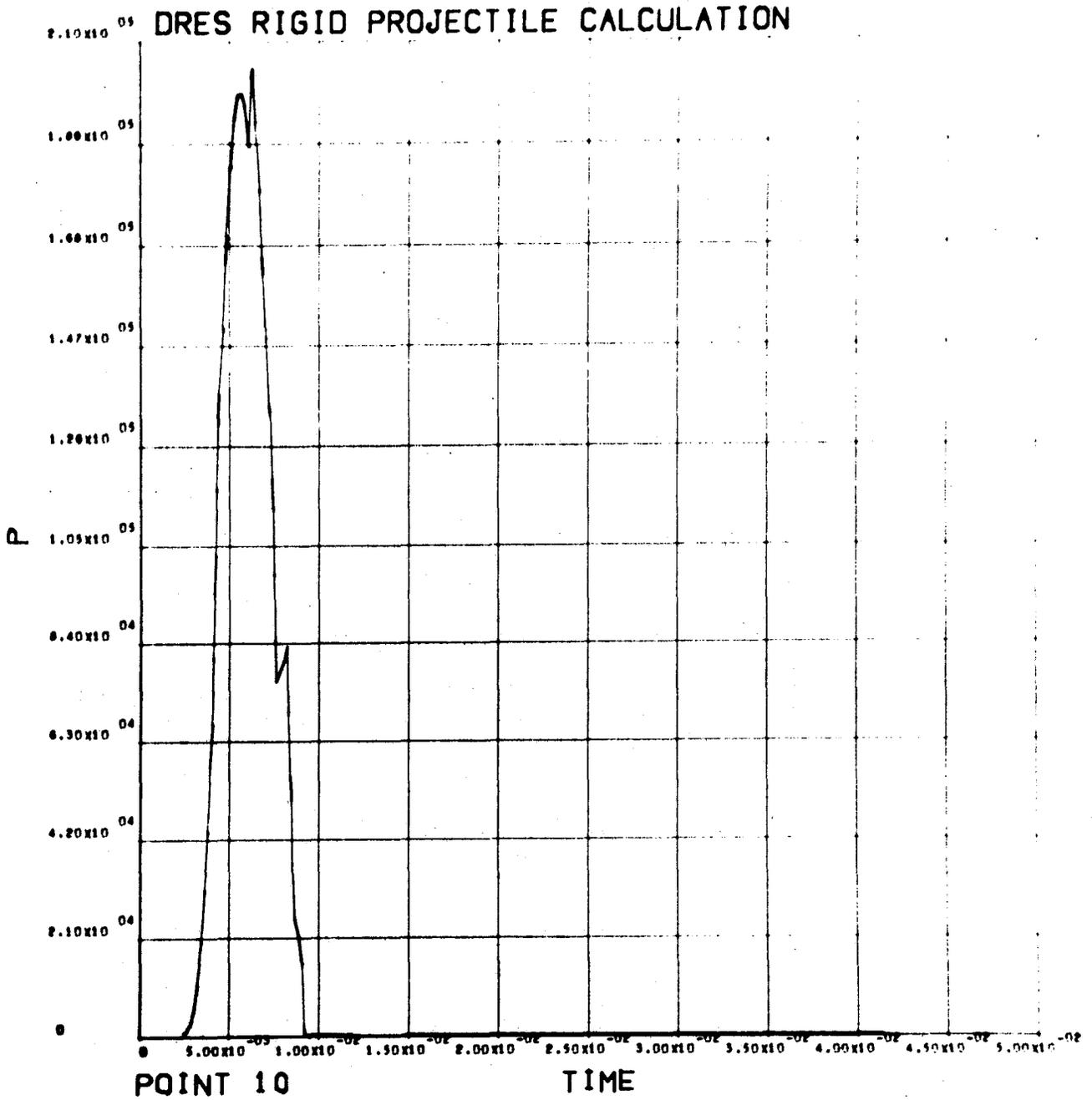


Figure A-57

Pressure (Pa) versus Time (s) for Particle at Point 10, Z = 0.4 m, R = 0.45 m.

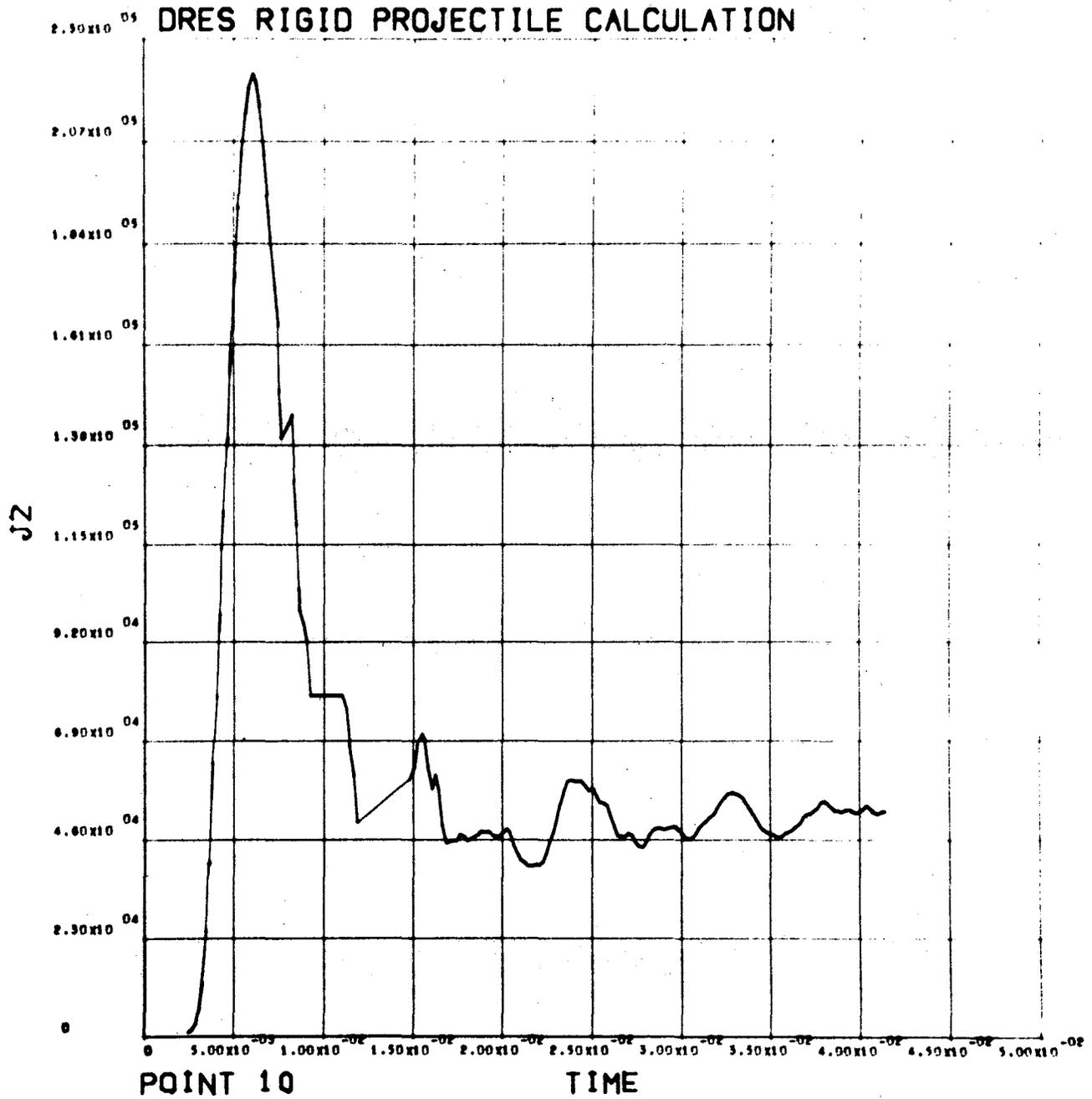


Figure A-58

Deviator Stress, J2, History (Pa) for Particle at Point 10, Z = 0.4 m, R = 0.45 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

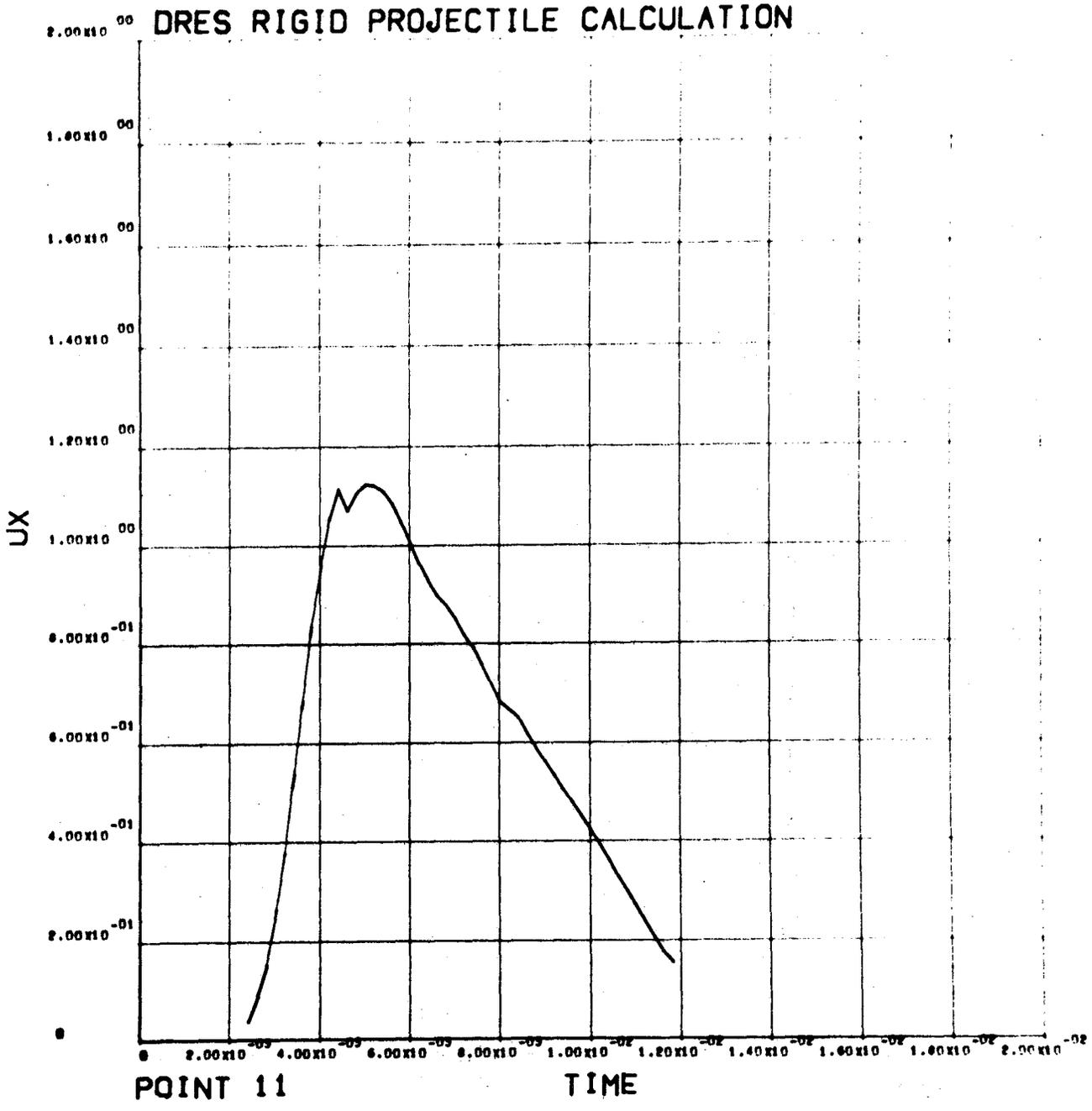


Figure A-59

Radial Velocity (m/s) versus Time (s) for Particle at Point 11, Z = 0.1 m, R = 0.45 m.

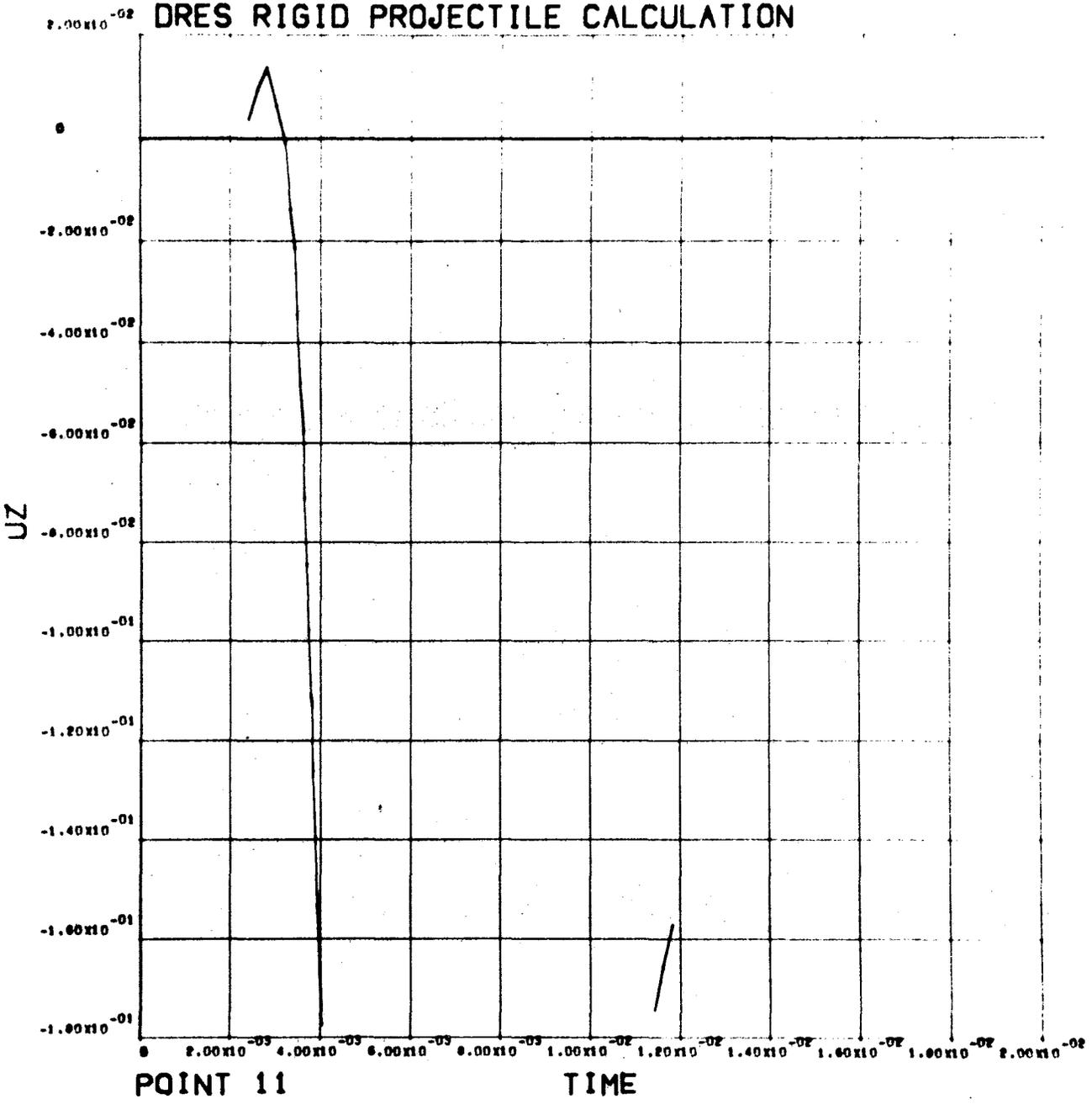


Figure A-60

Axial Velocity (m/s) versus Time (s) for Particle at Point 11, Z = 0.1 m, R = 0.45 m.

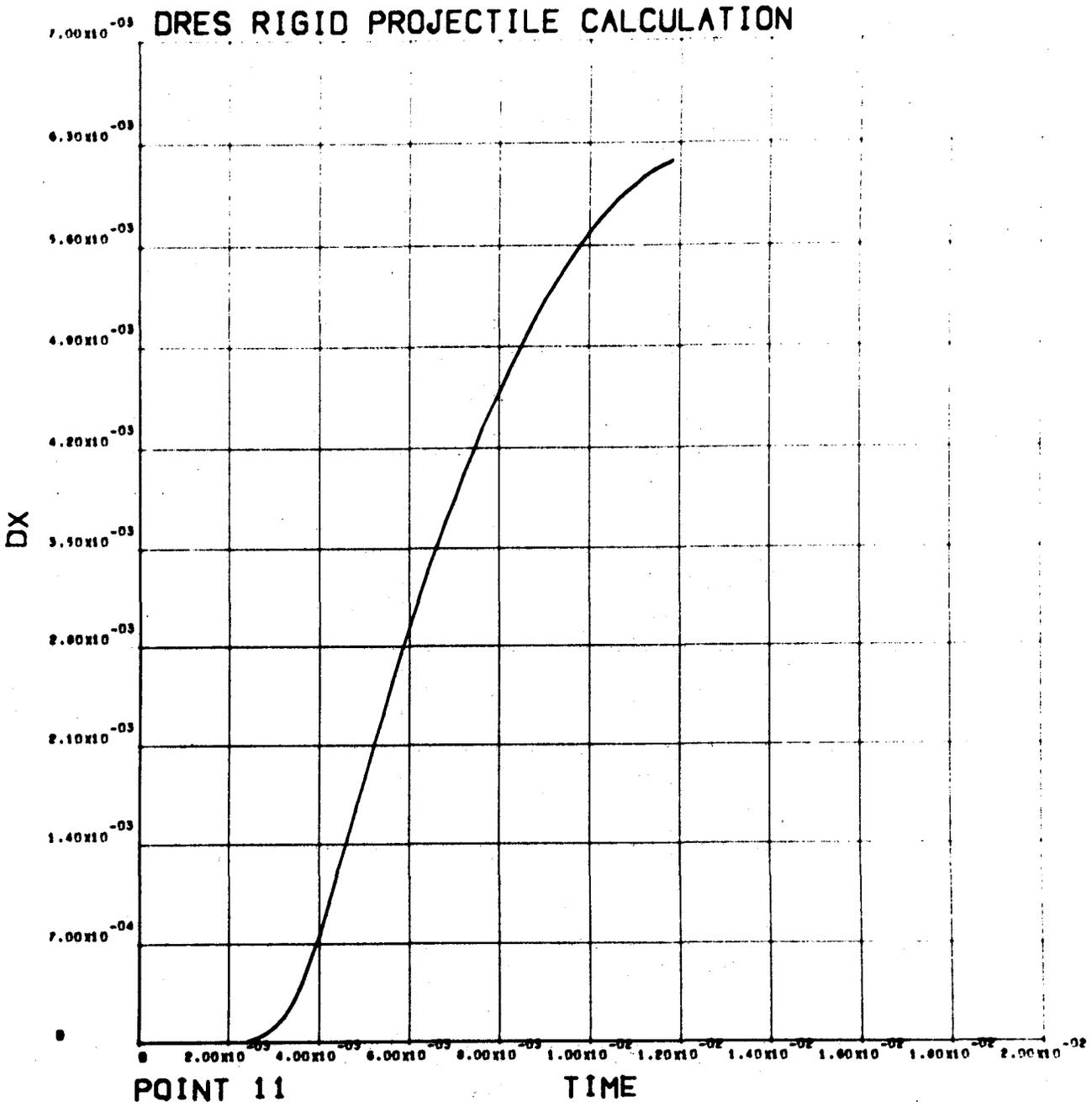


Figure A-61

Radial Displacement (m) versus Time (s) for Particle at Point 11, Z = 0.1 m, R = 0.45 m.

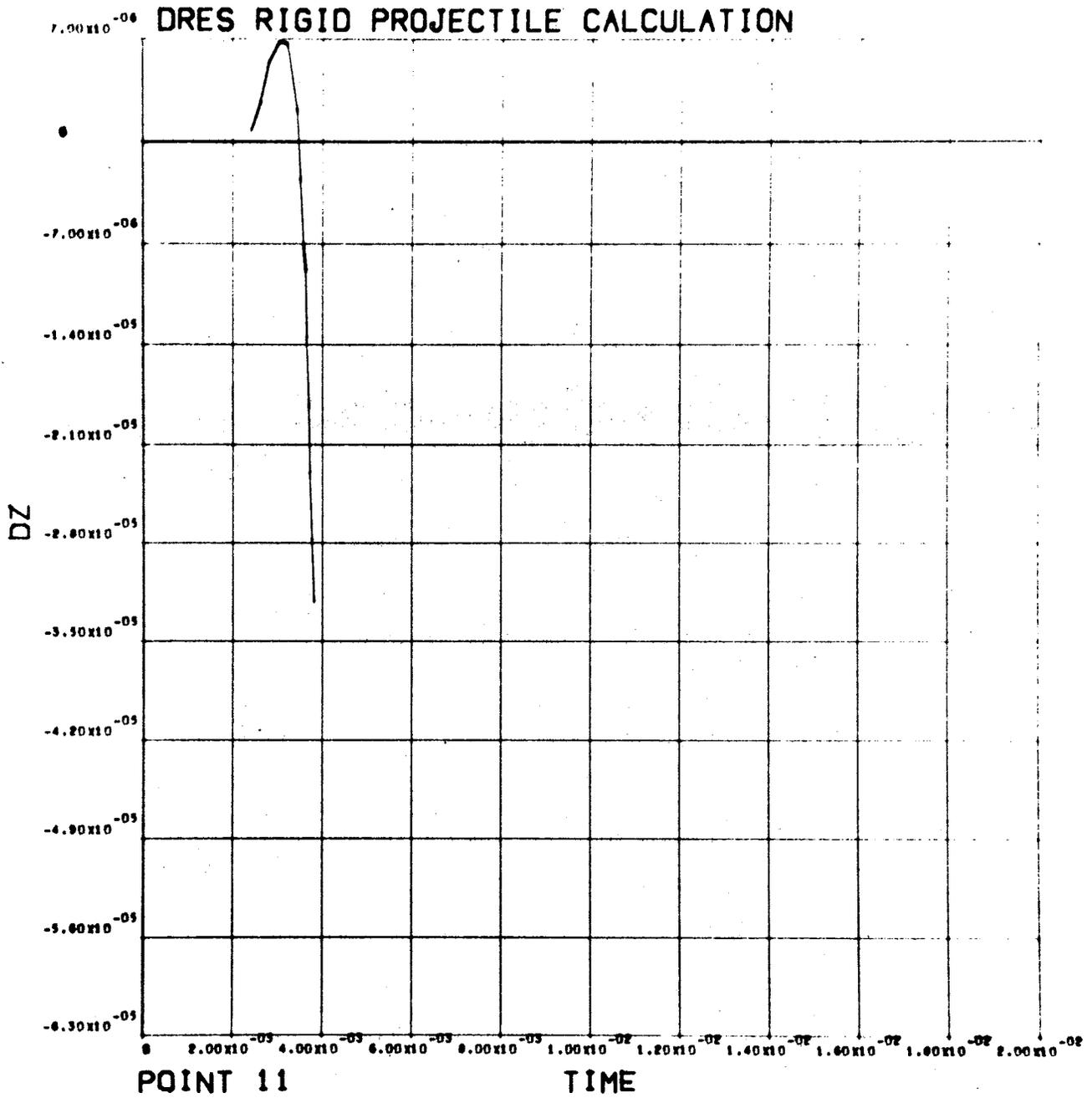


Figure A-62

Axial Displacement (m) versus Time (s) for Particle at Point 11, Z = 0.1 m, R = 0.45 m.

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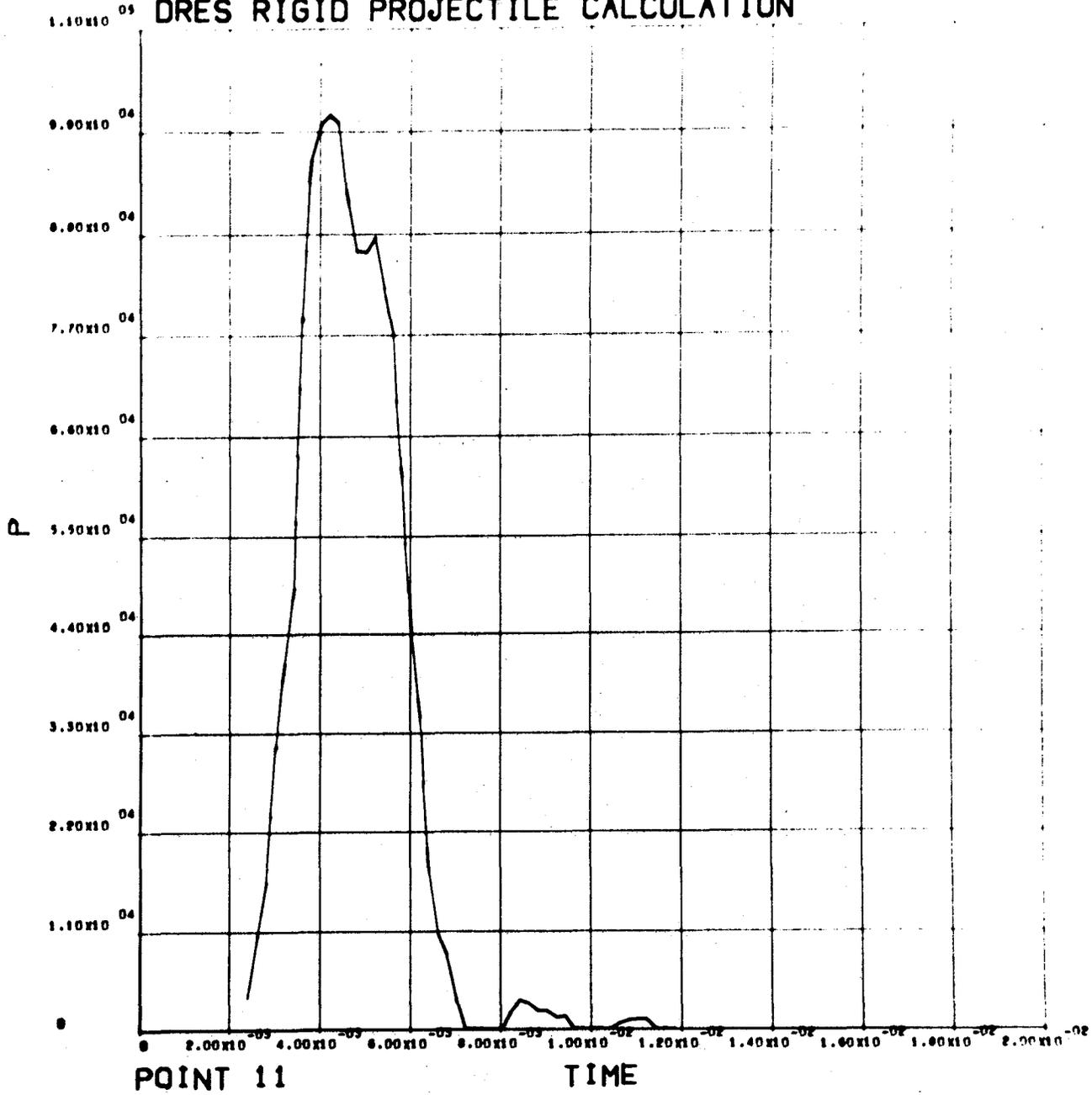


Figure A-63

Pressure (Pa) versus Time (s) for Particle at Point 11, Z = 0.1 m, R = 0.45 m.

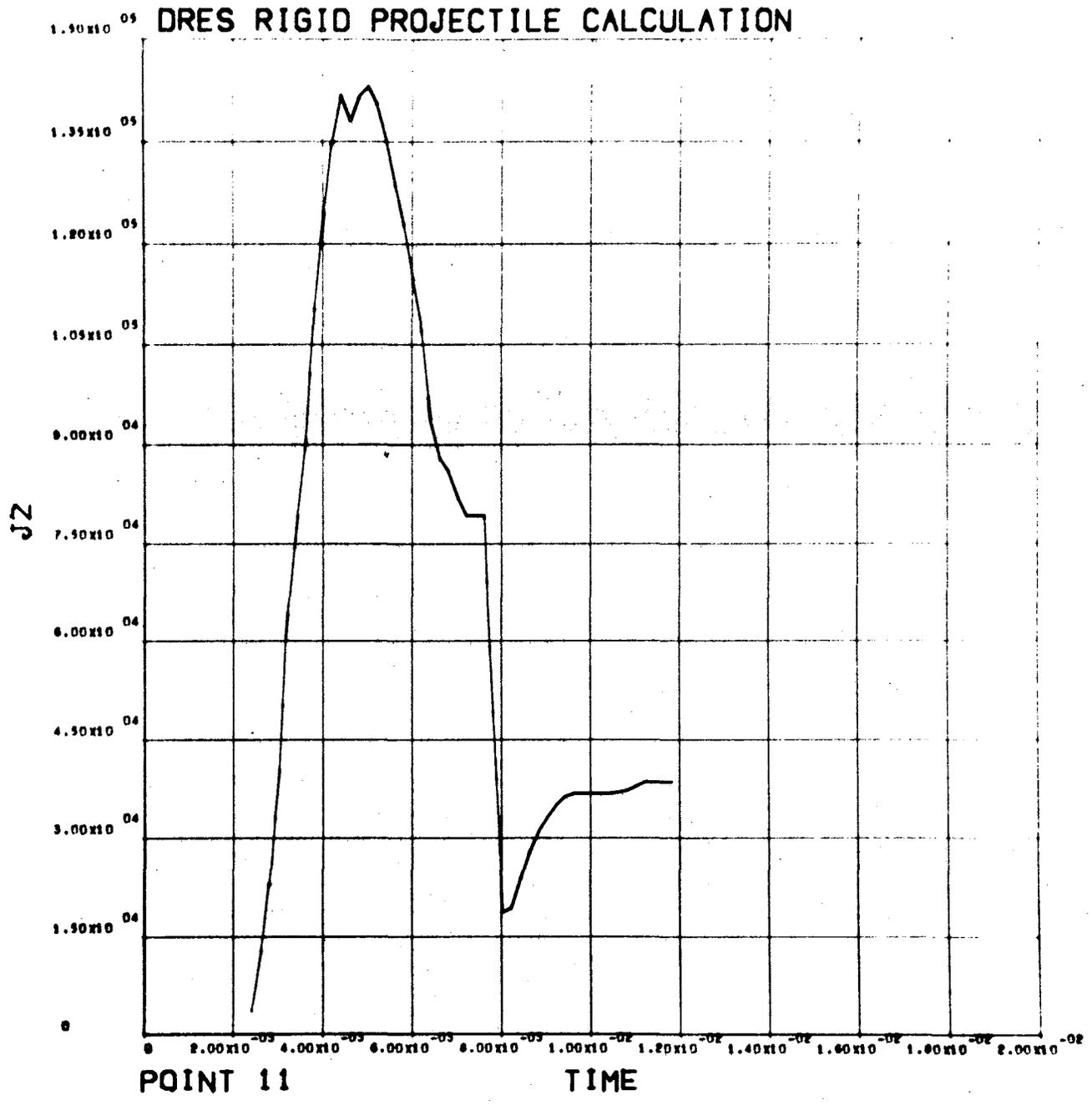


Figure A-64

Deviator Stress, J2, History (Pa) for Particle at Point 11, Z = 0.1 m, R = 0.45 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

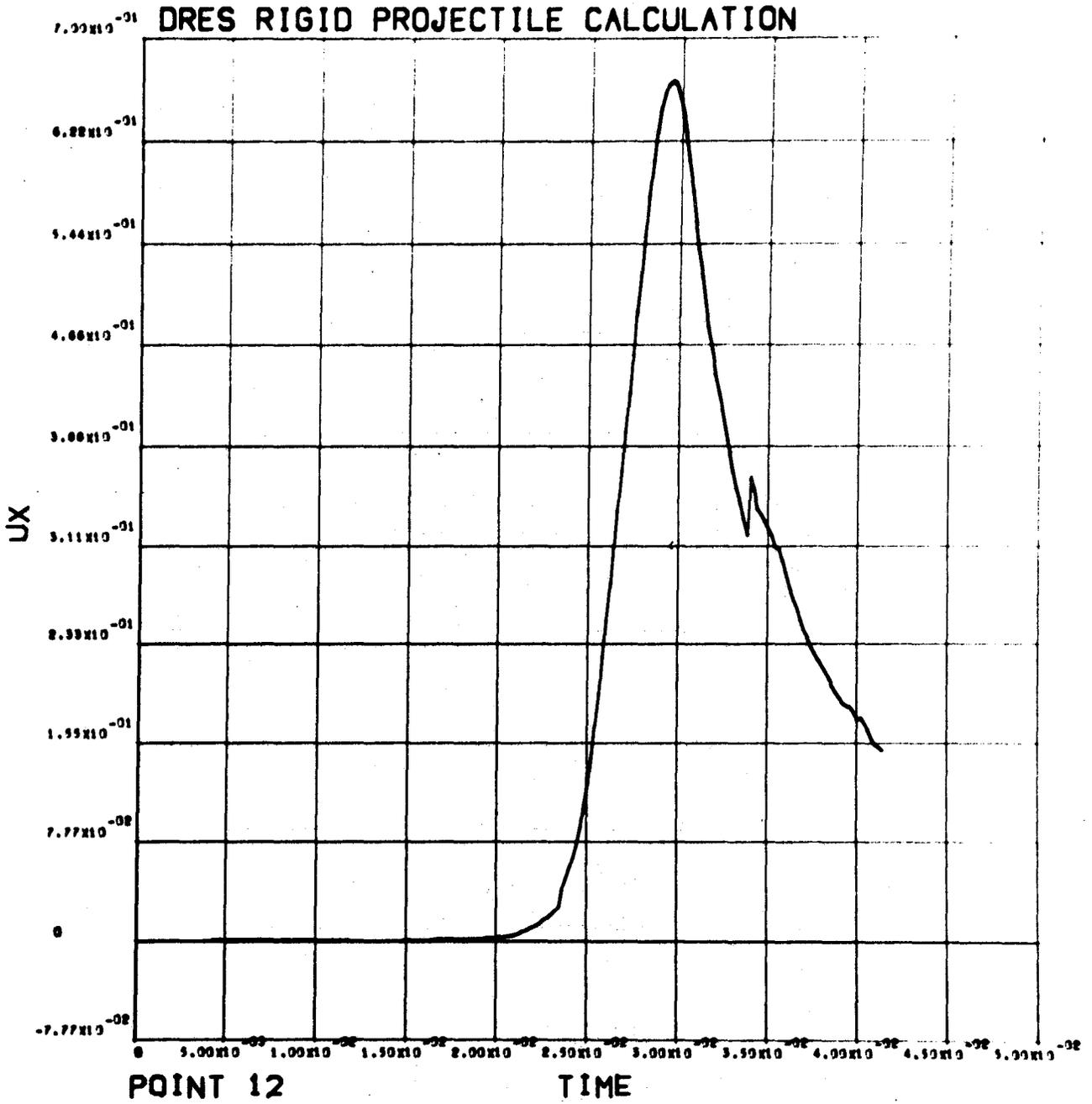


Figure A-65

Radial Velocity (m/s) versus Time (s) for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

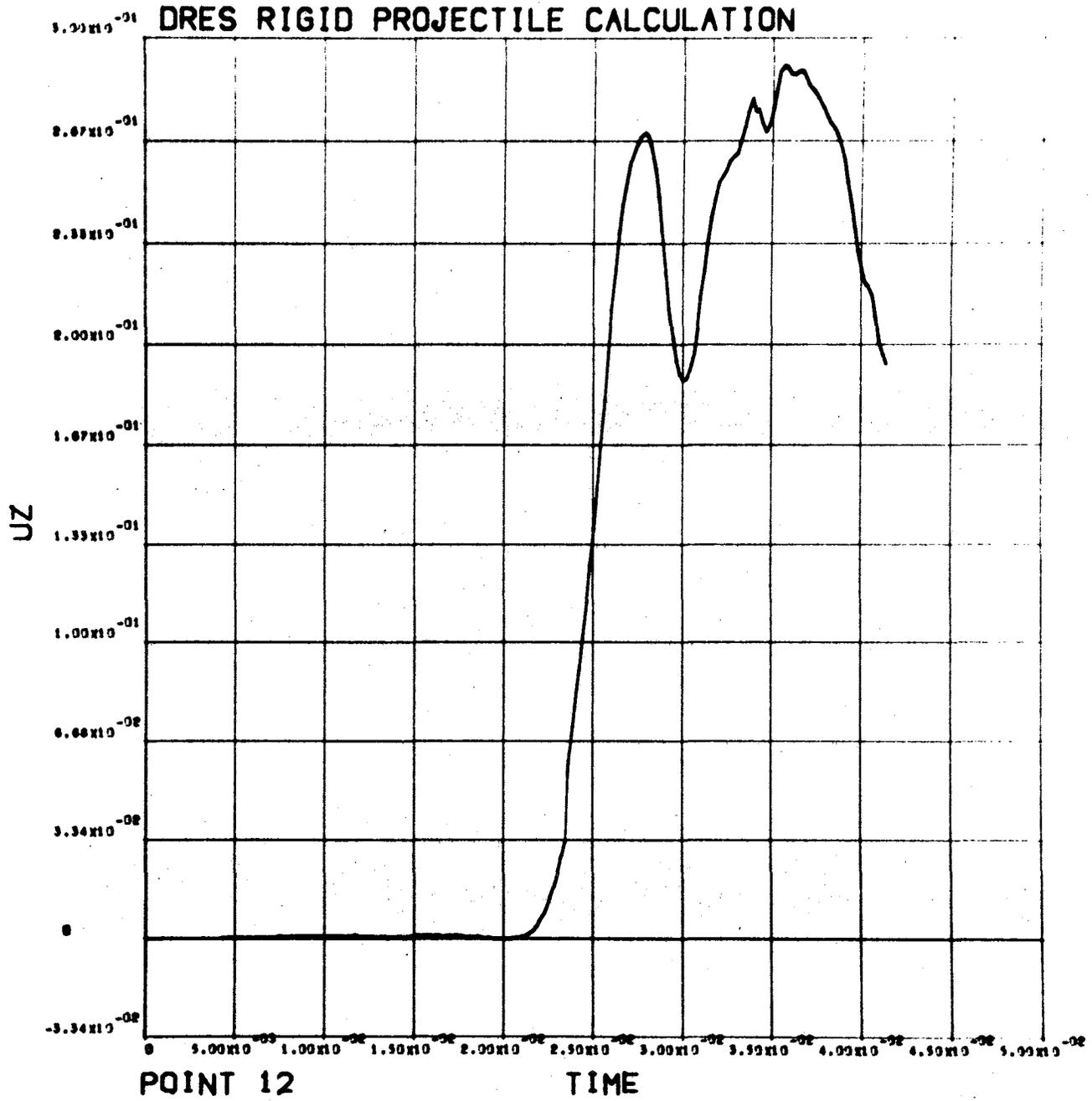


Figure A-66

Axial Velocity (m/s) versus Time (s) for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

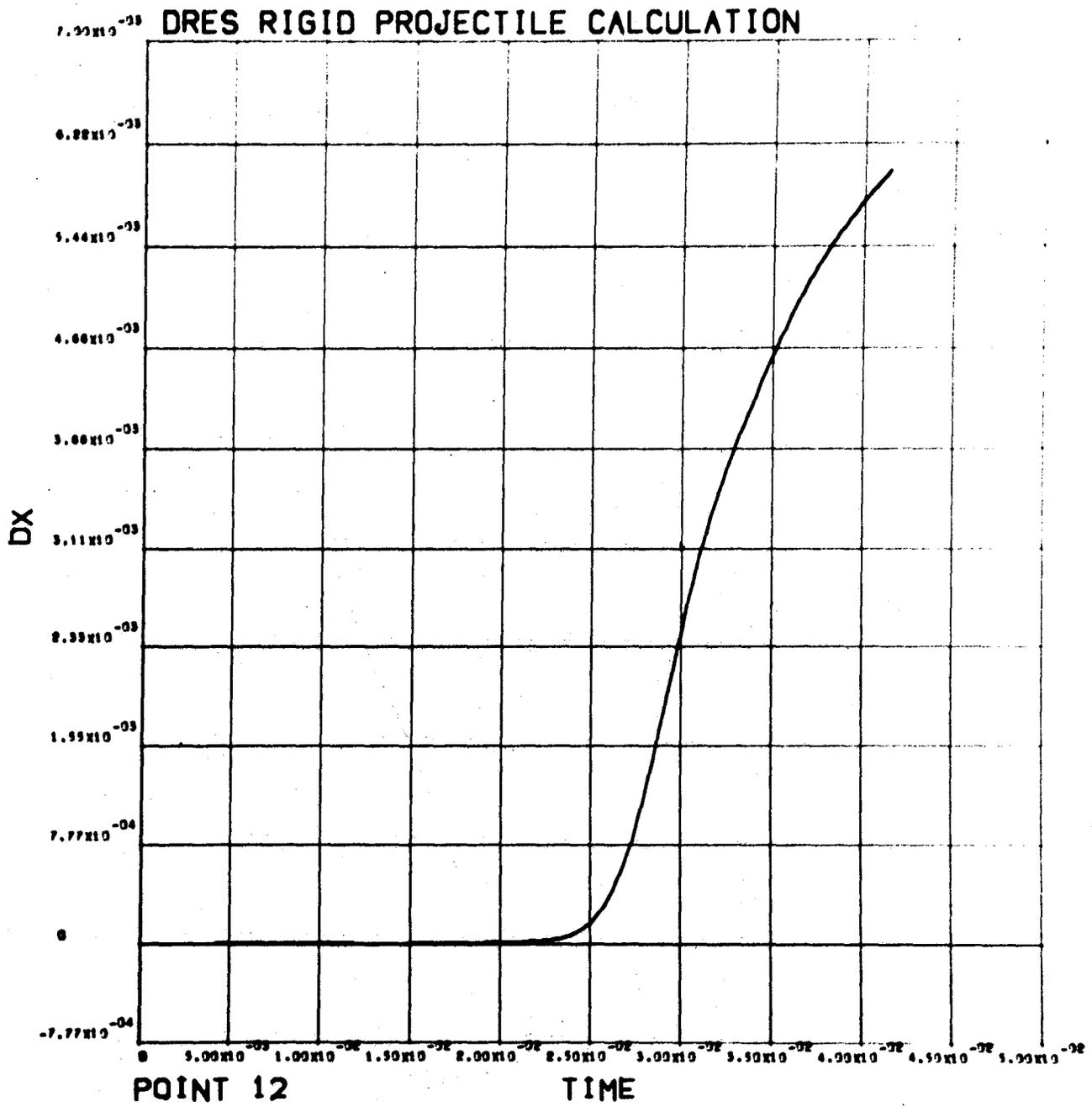


Figure A-67

Radial Displacement (m) versus Time (s) for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

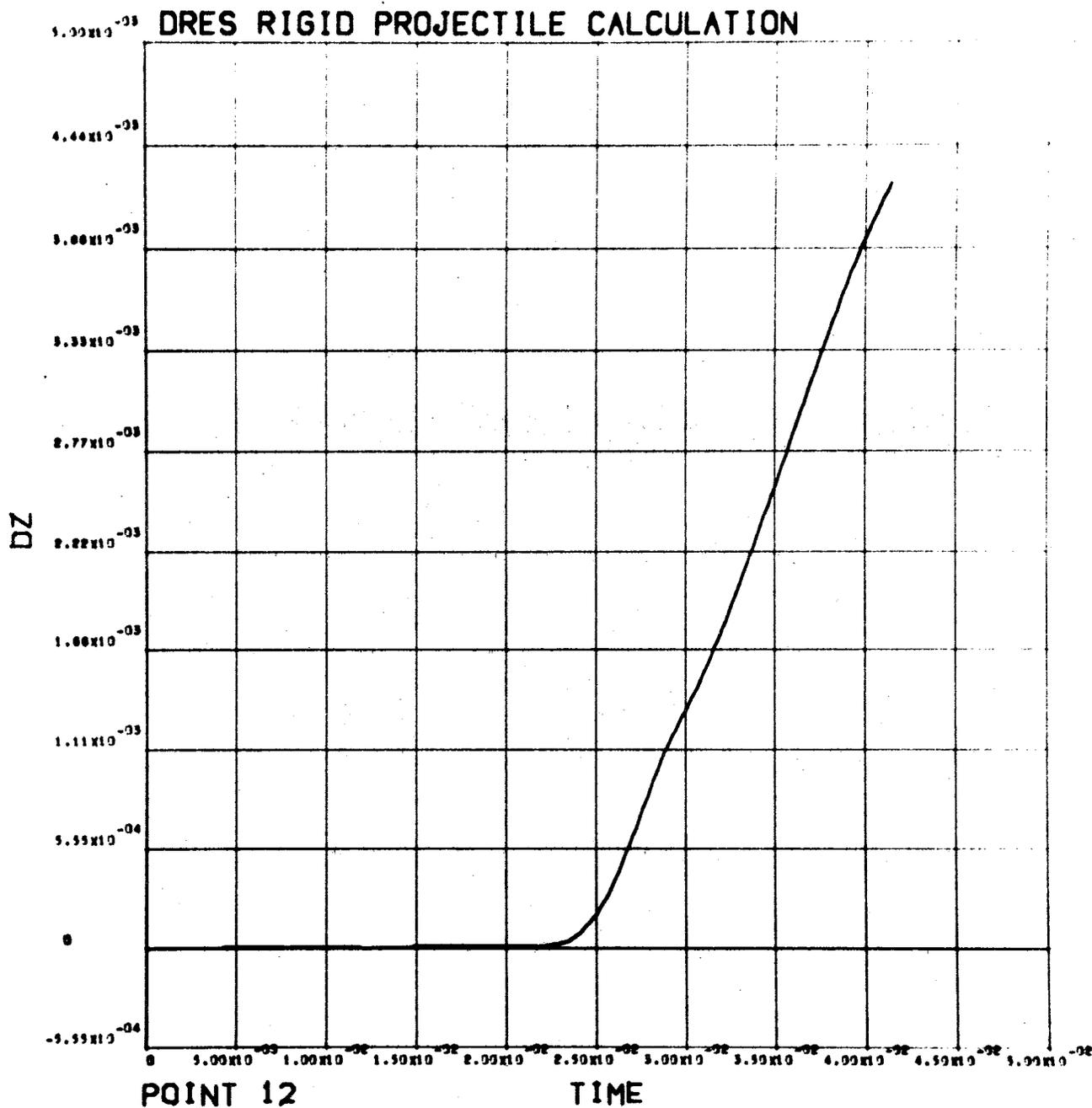


Figure A-68  
 Axial Displacement (m) versus Time (s) for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

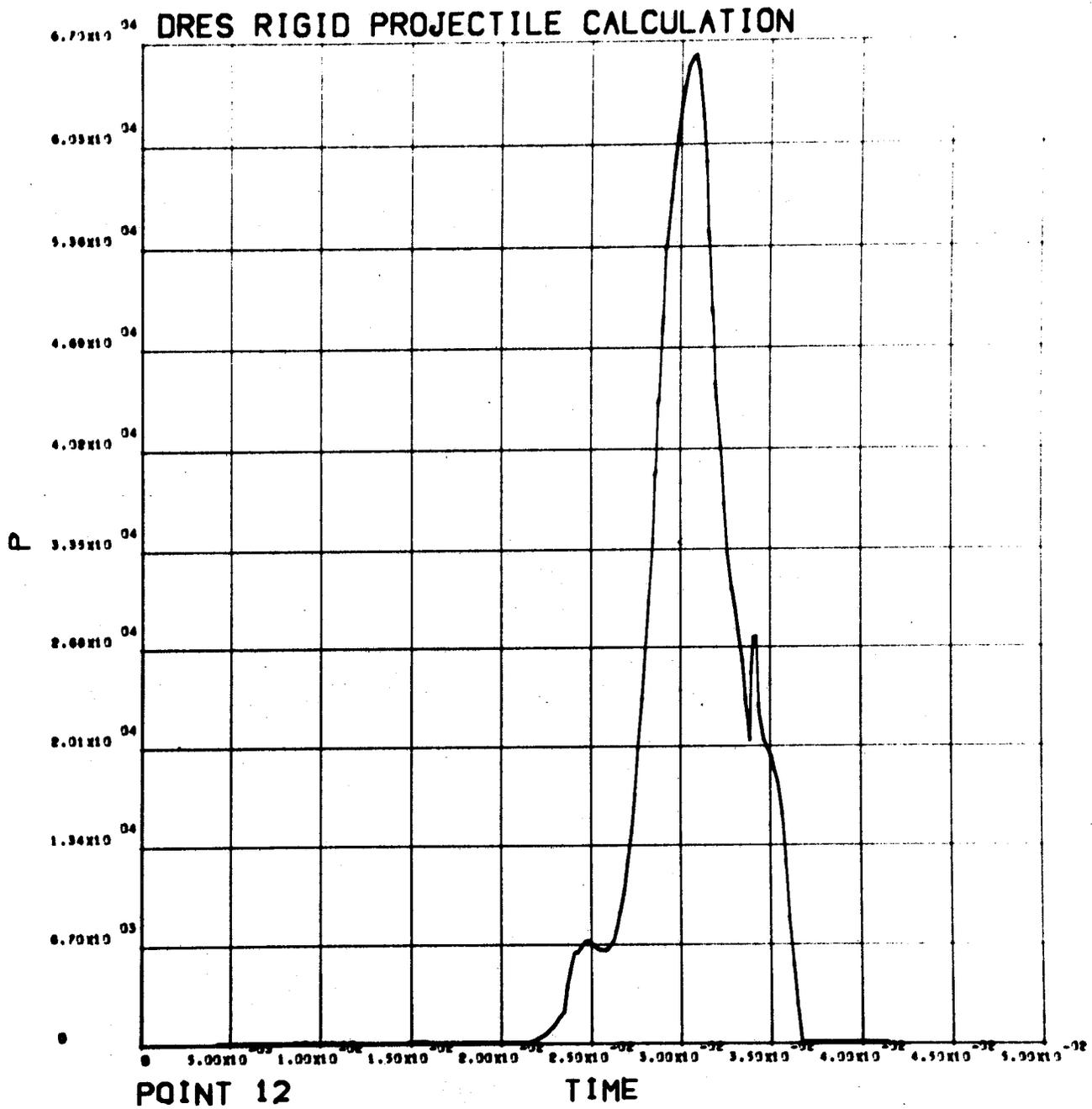


Figure A-69

Pressure (Pa) versus Time (s) for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

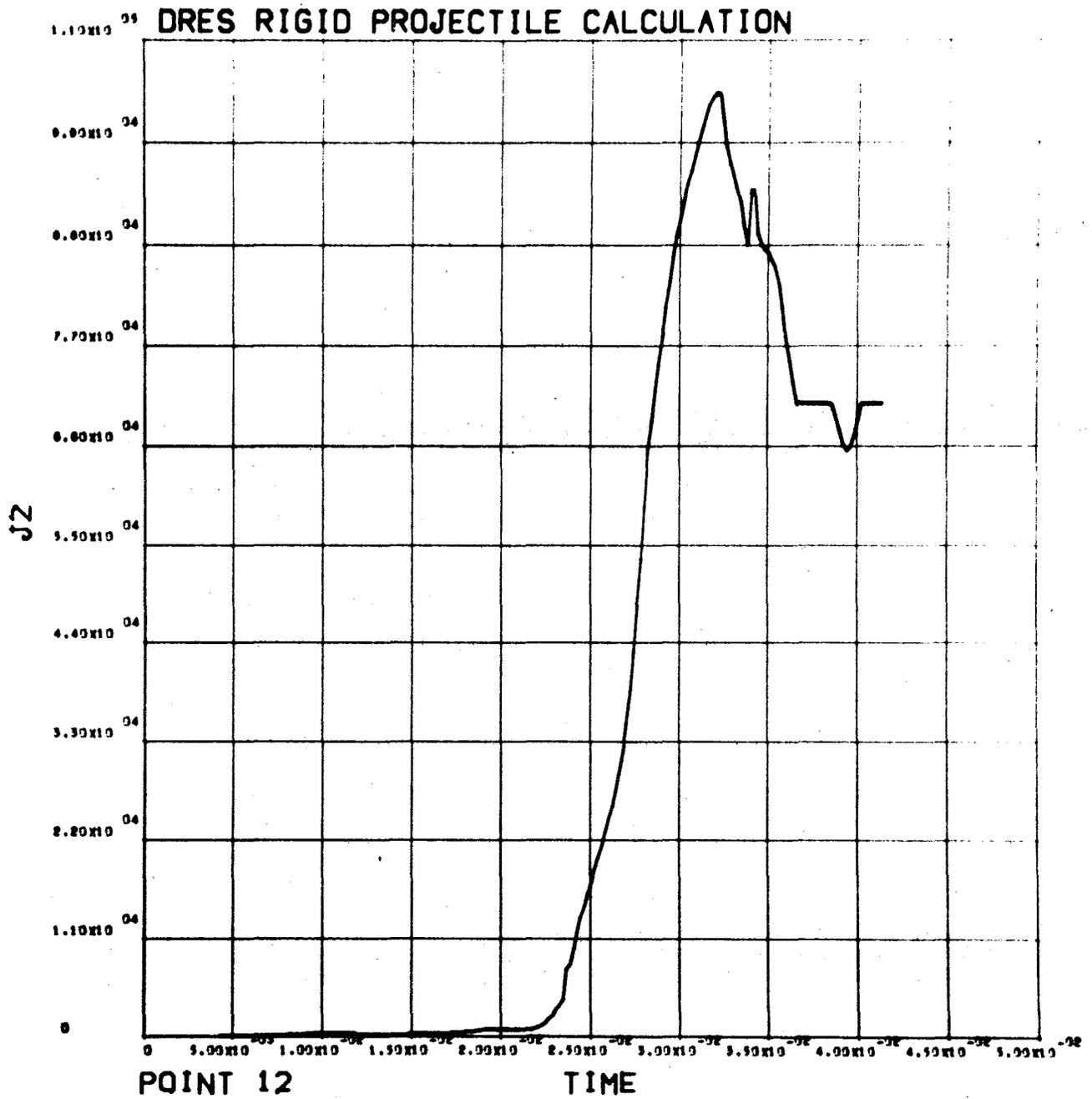


Figure A-70

Deviator Stress, J2, History (Pa) for Particle at Point 12, Z = 3.6 m, R = 0.9 m  
 (Octahedral Shear Stress =  $\sqrt{2/3}(J2)$ ).

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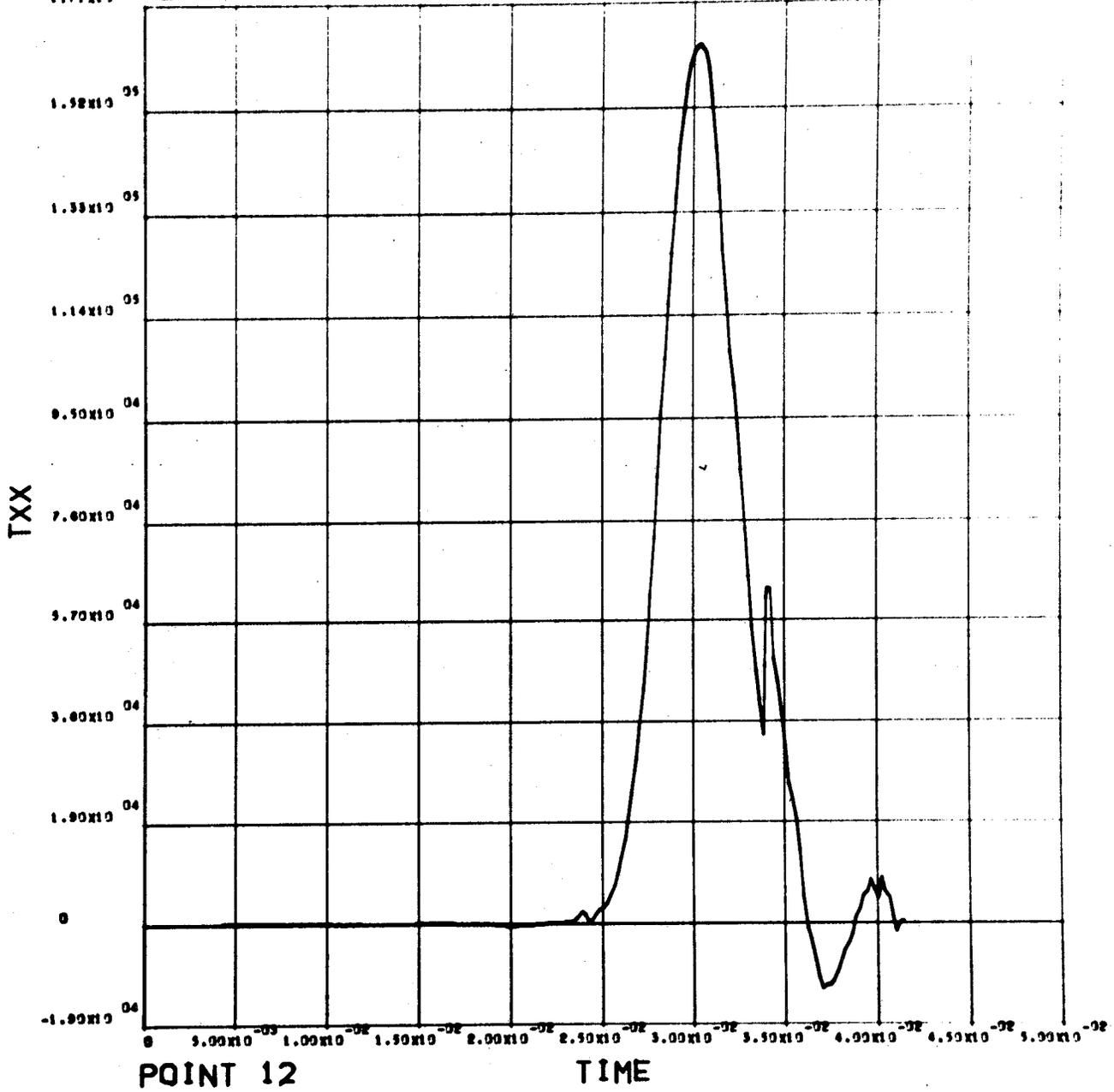


Figure A-71

Radial Stress (Pa) History for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

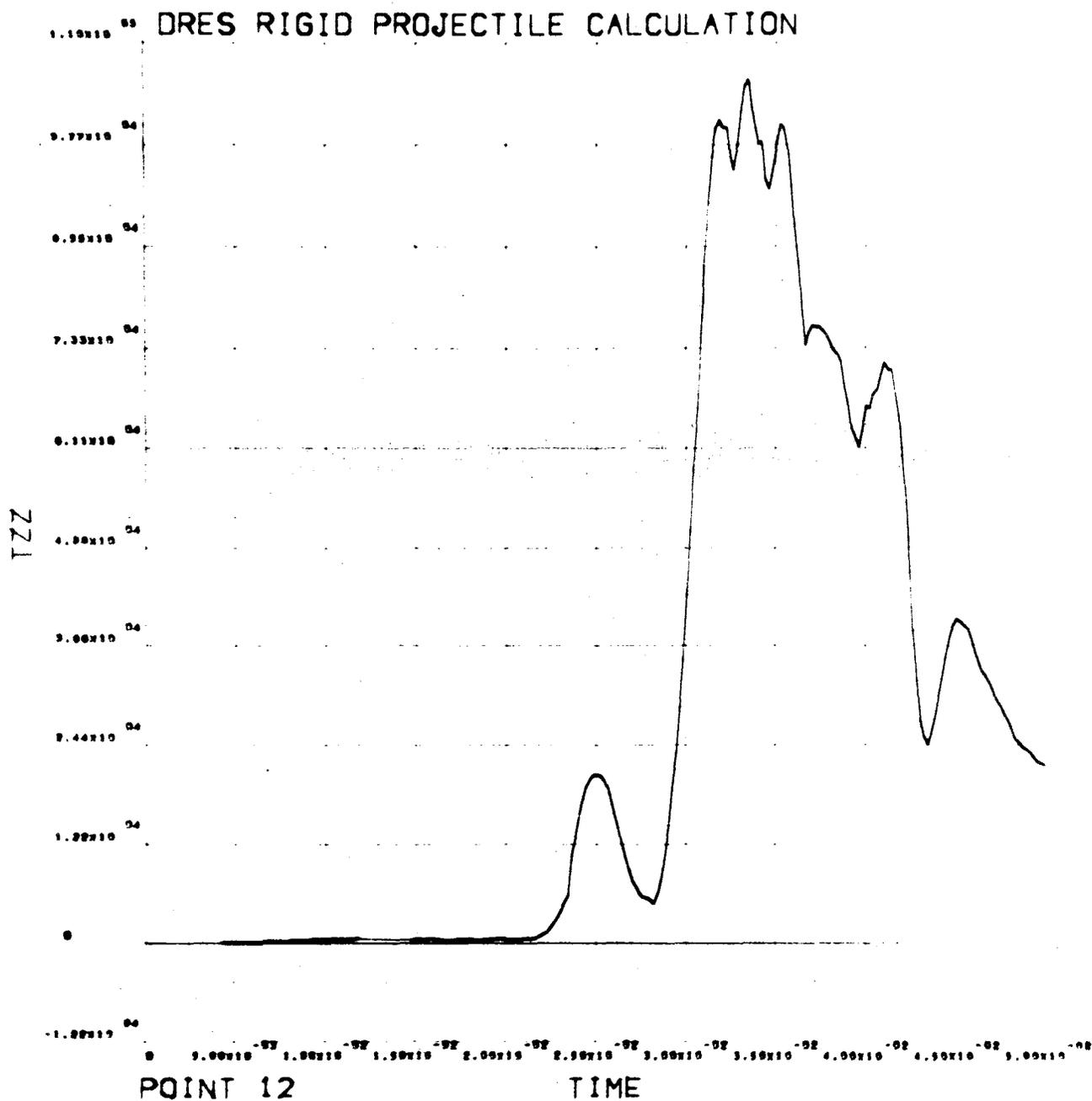


Figure A-72

Axial Stress (Pa) History for Particle at Point 12, Z = 3.6 m, R = 0.9 m.

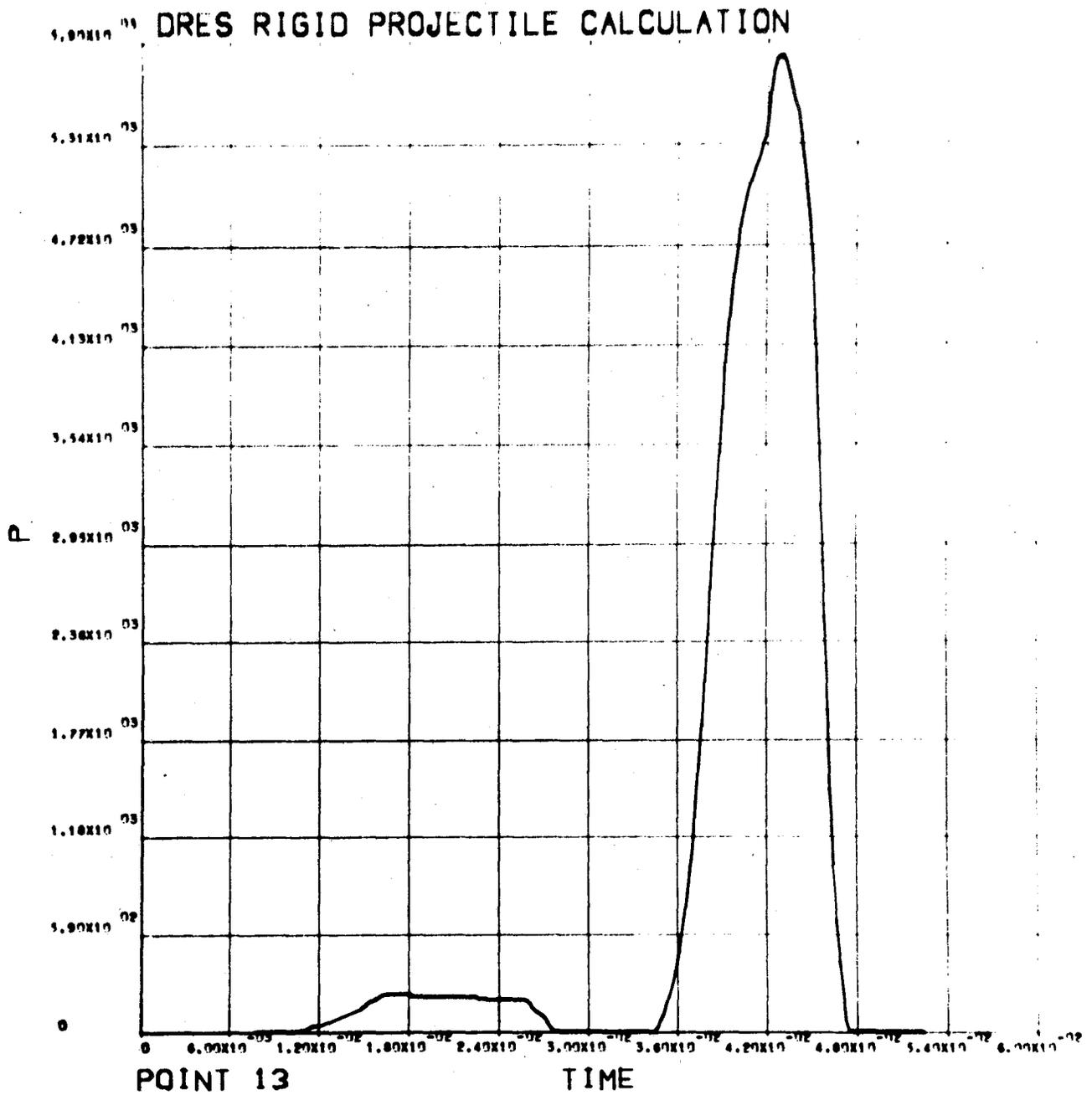


Figure A-73

Pressure (Pa) versus Time (s) for Particle at Point 13, Z = 5.4 m, R = 1.5 m.

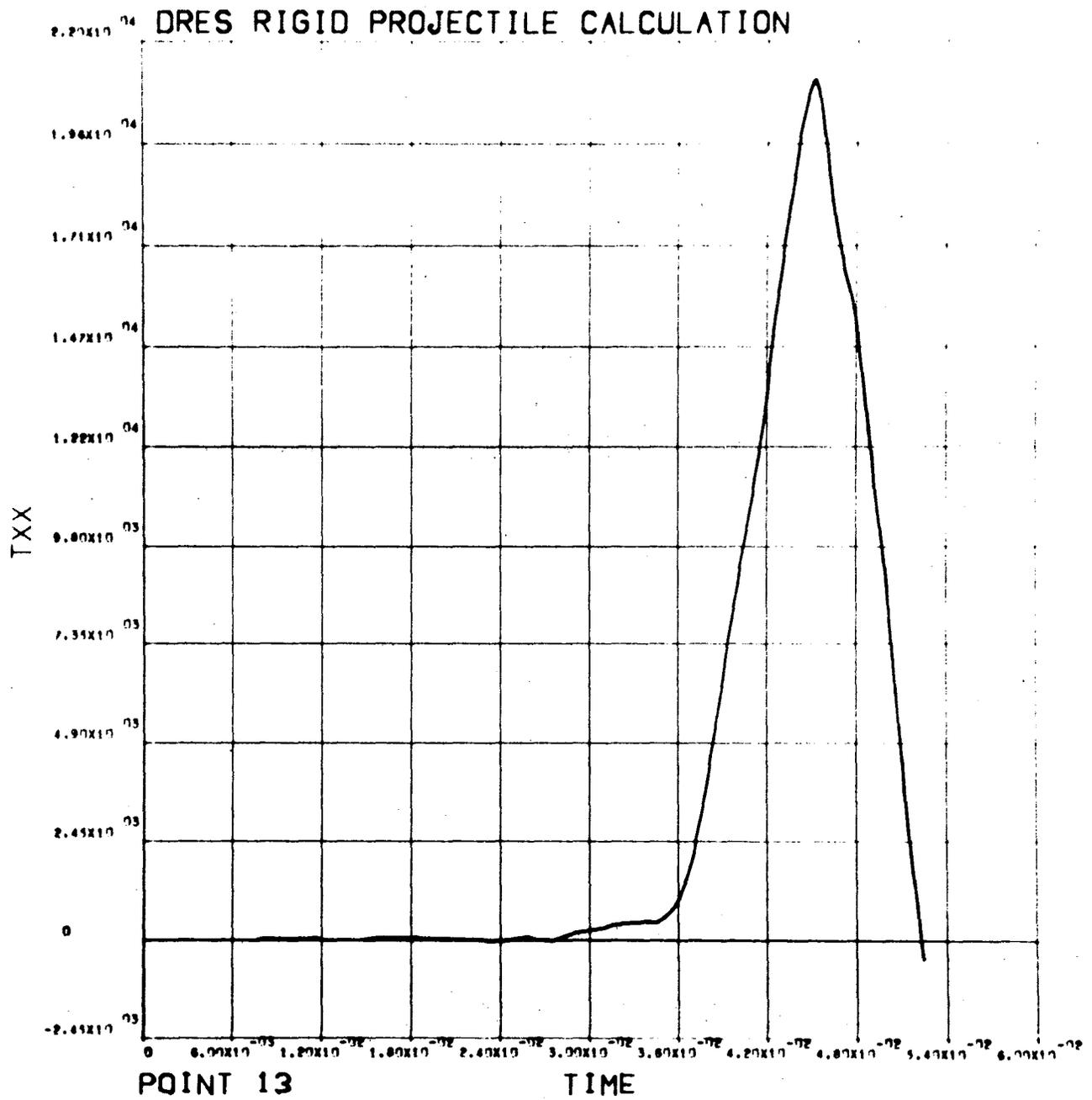


Figure A-74

Radial Stress (Pa) History for Particle at Point 13, Z = 5.4 m, R = 1.5 m.

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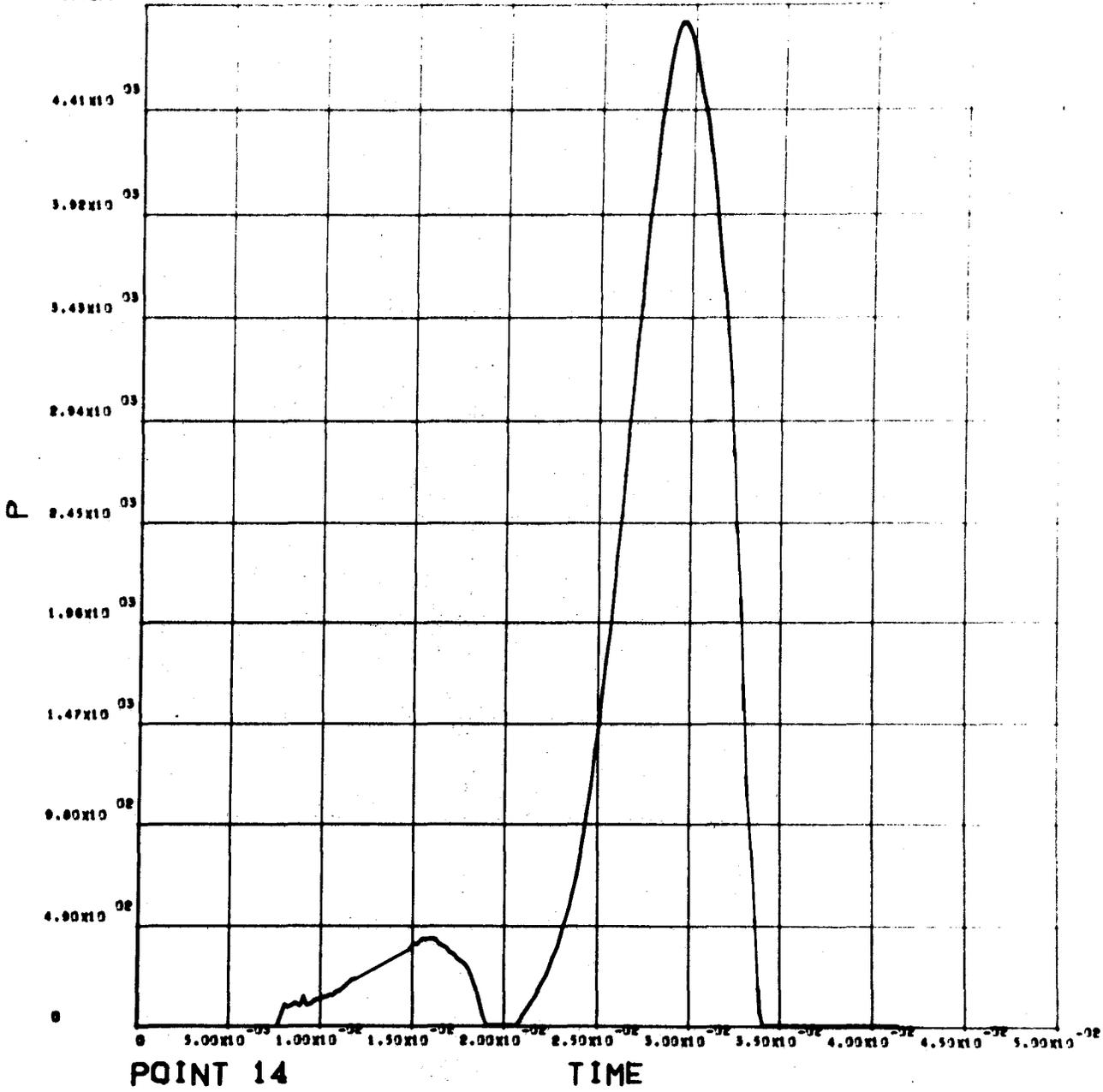


Figure A-75

Pressure (Pa) versus Time (s) for Particle at Point 14, Z = 3.6 m, R = 1.5 m.

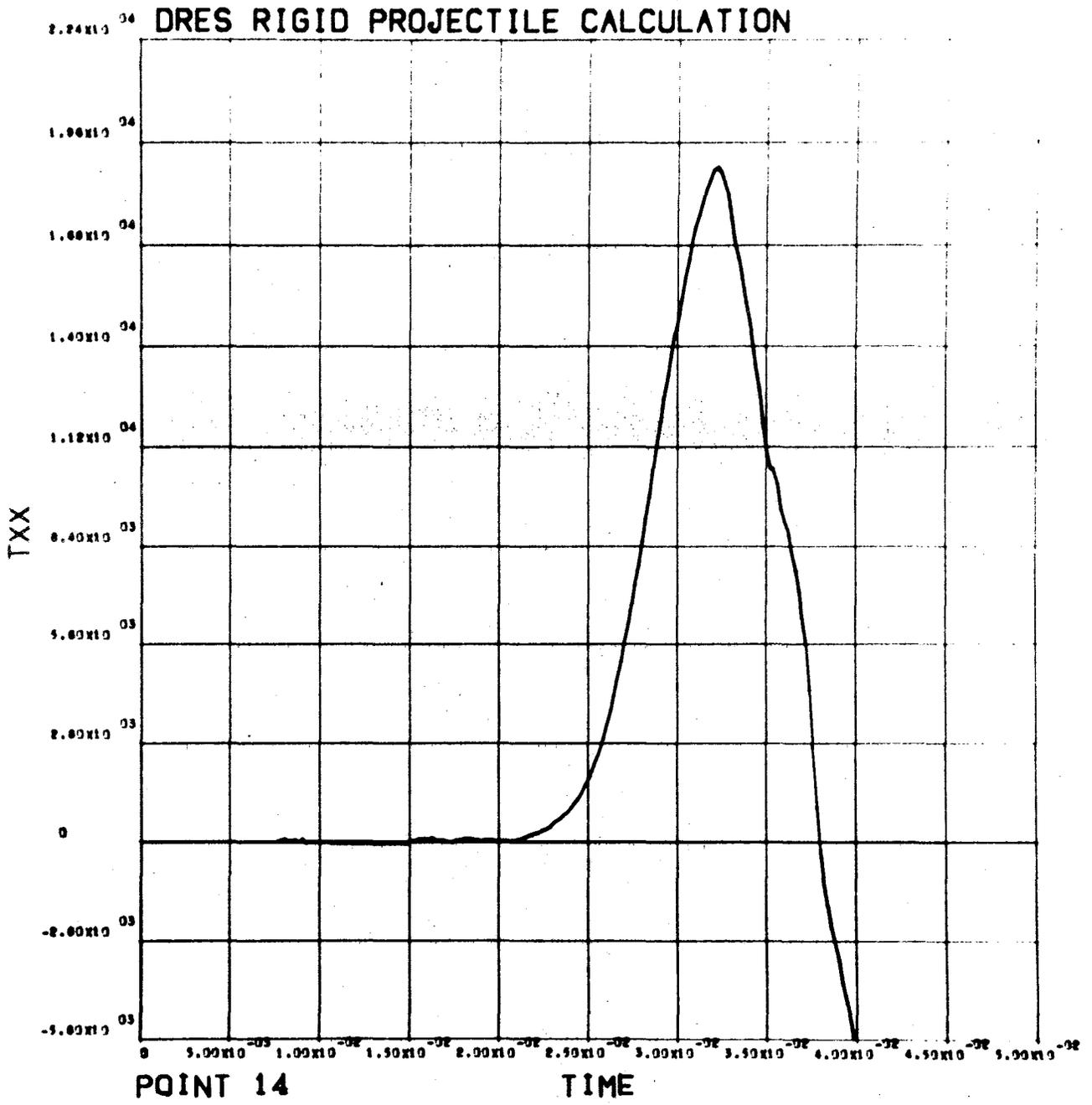


Figure A-76

Radial Stress (Pa) History for Particle at Point 14, Z = 3.6 m, R = 1.5 m.

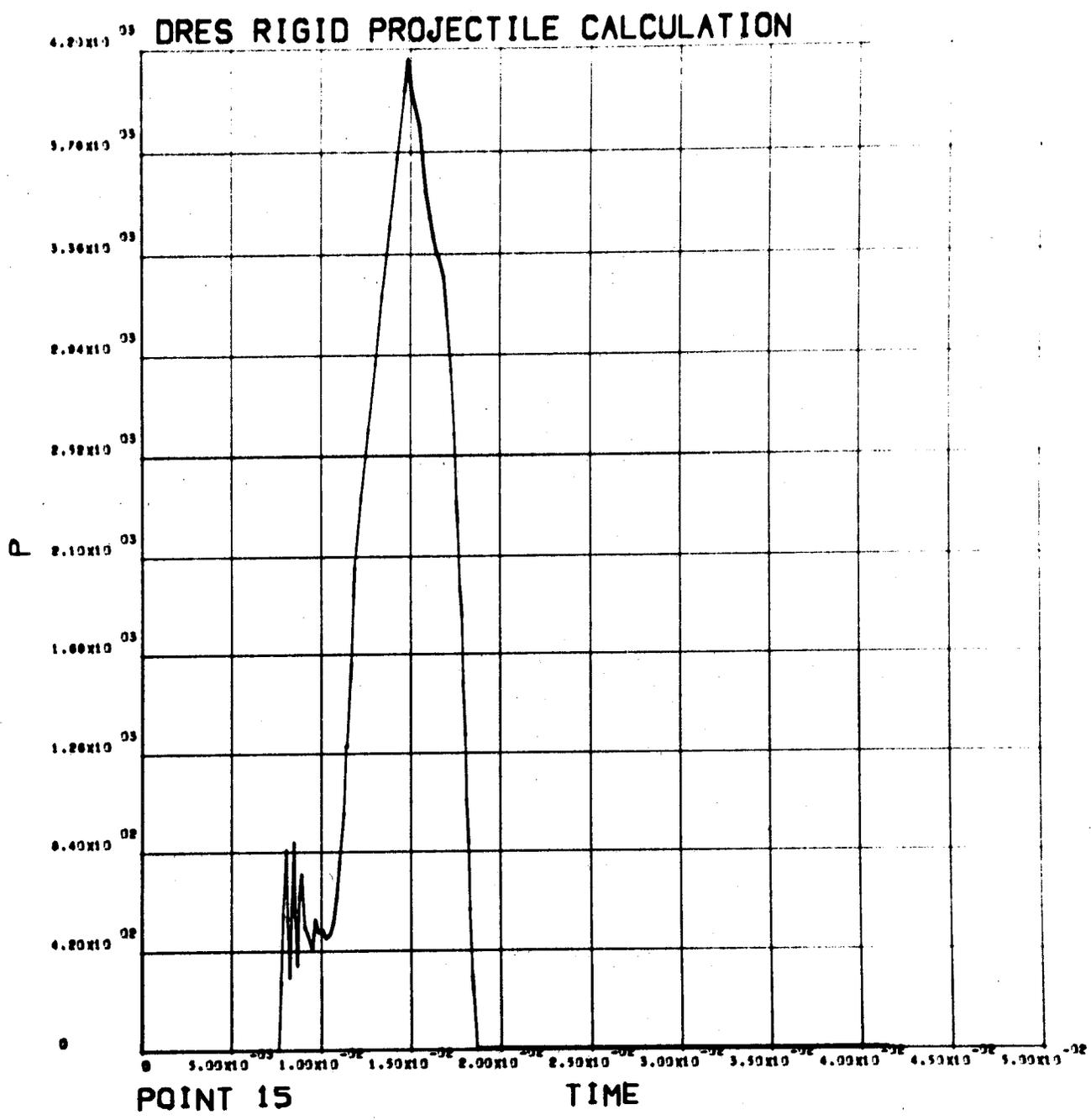


Figure A-77

Pressure (Pa) versus Time (s) for Particle at Point 15, Z = 1.8 m, R = 1.5 m.

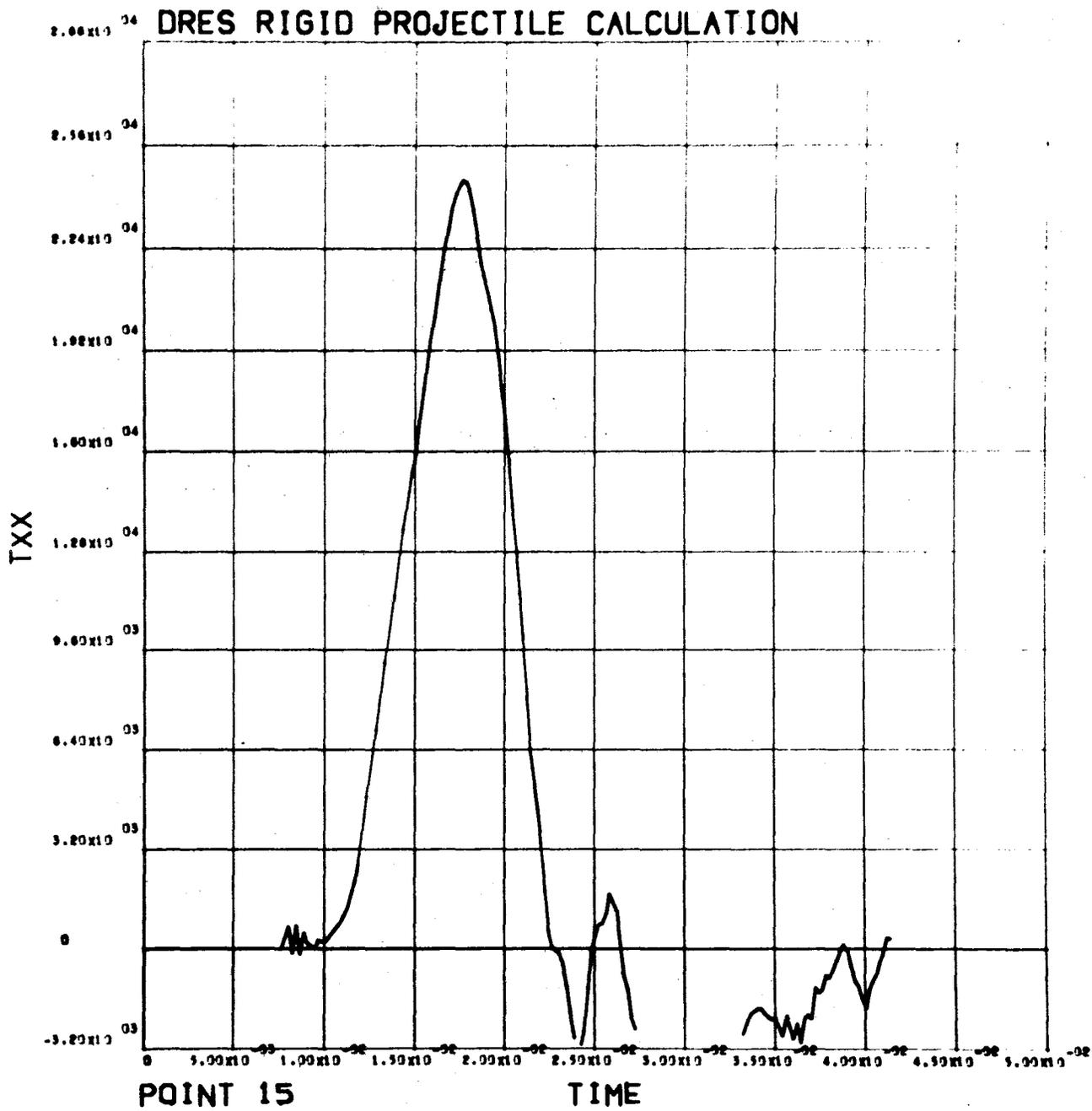
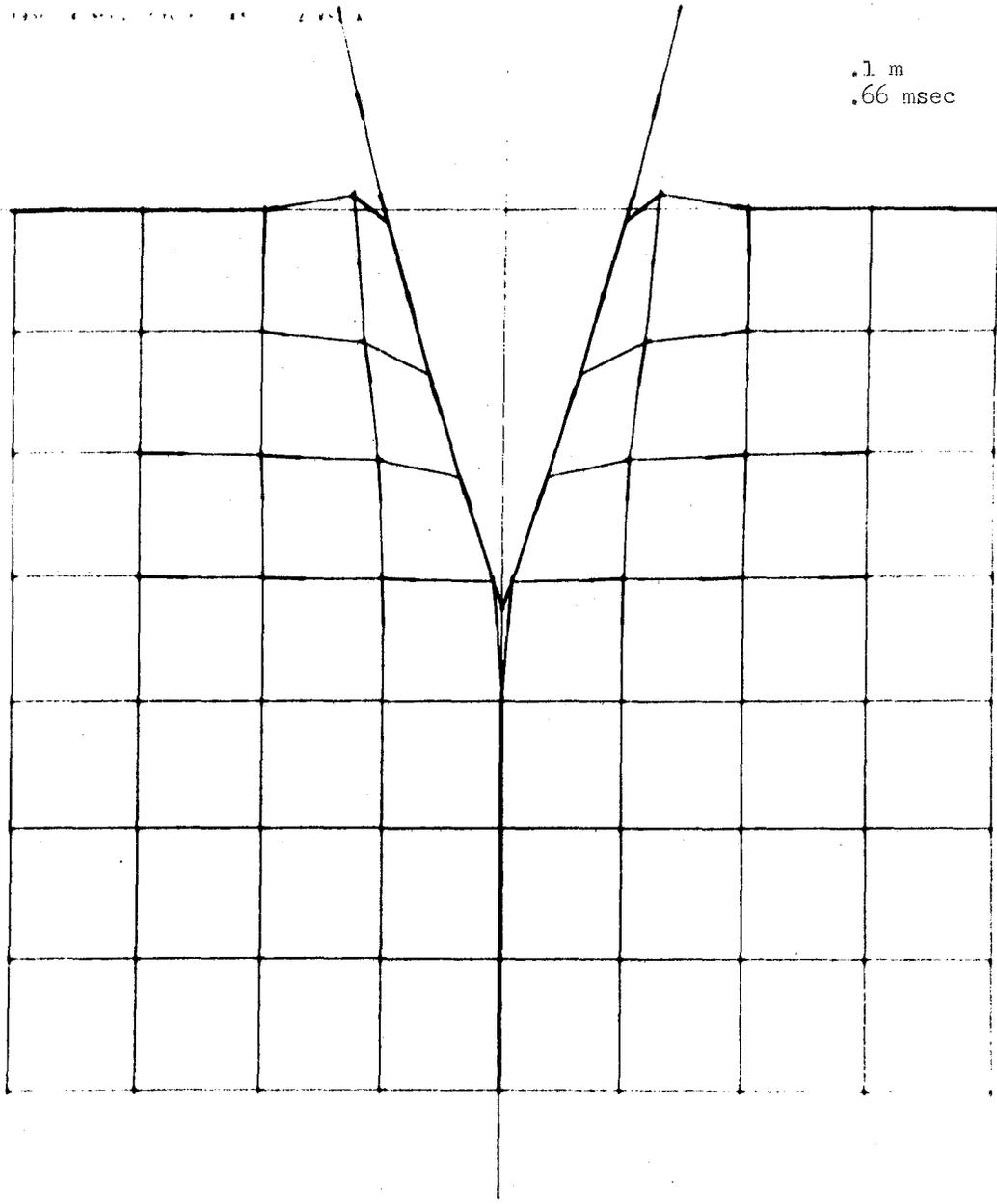


Figure A-78

Radial Stress (Pa) History for Particle at Point 15, Z = 1.8 m, R = 1.5 m.

27 12 1954  
100 500 1000 2000 4000 8000 16000



.1 m  
.66 msec

Figure A-79

Lagrangian Coordinates When Projectile Has Penetrated to Depth of 0.1 m.

TIME: 4.570010E-04

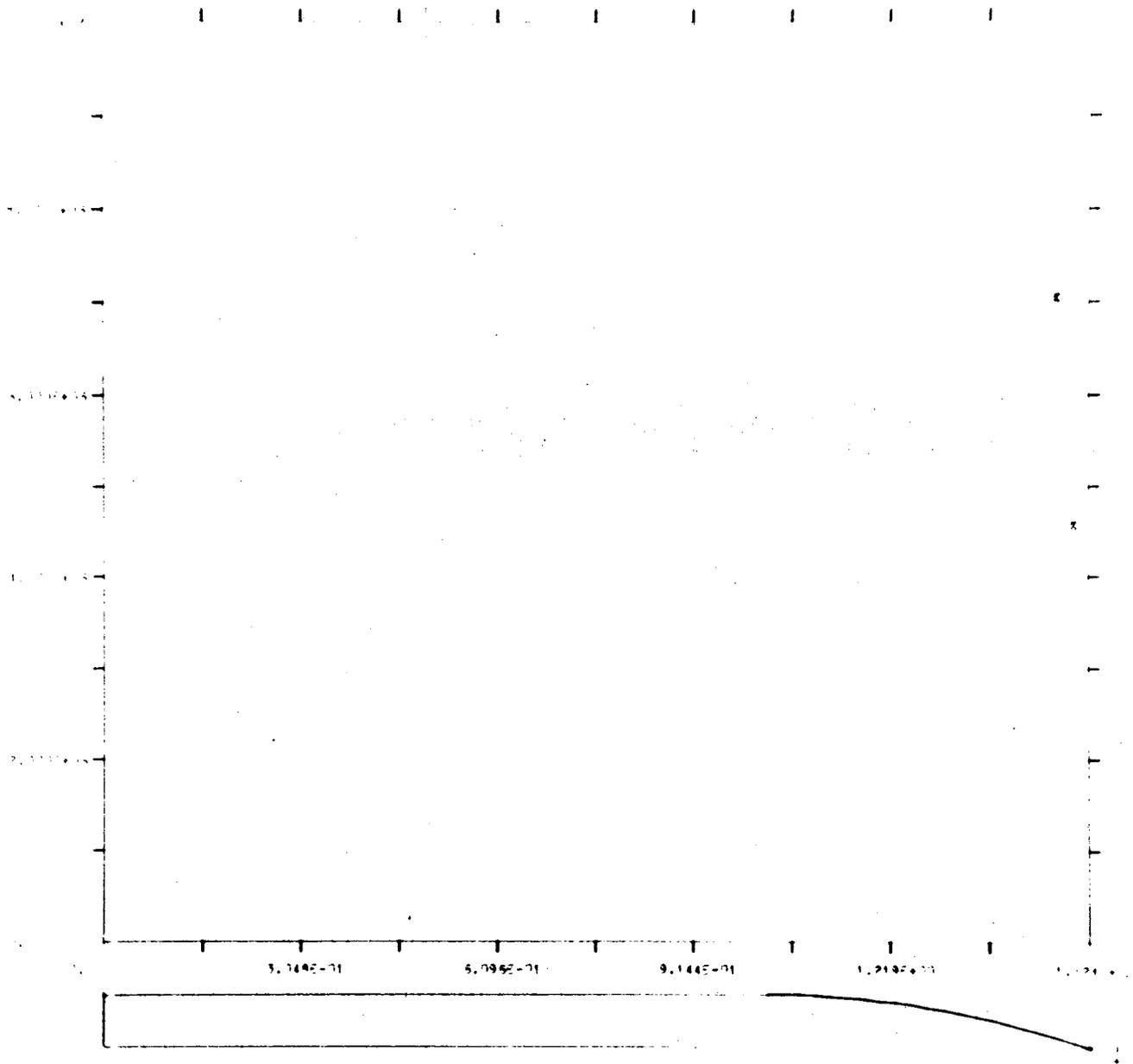


Figure A-80

Normal Stress (Pa) Along Surface of Projectile When Projectile is at 0.1 m Depth.

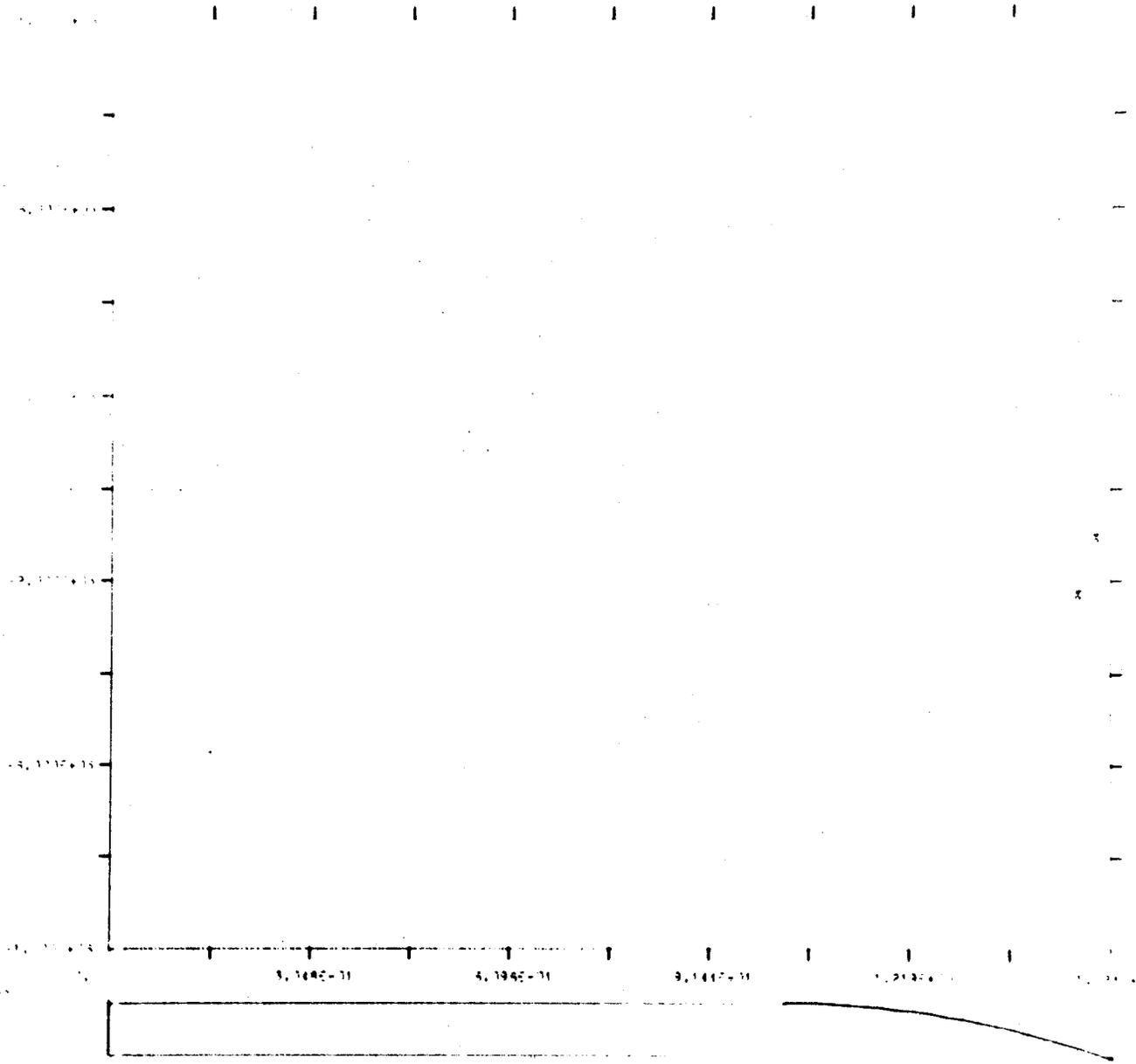


Figure A-81

Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 0.1 m Depth.

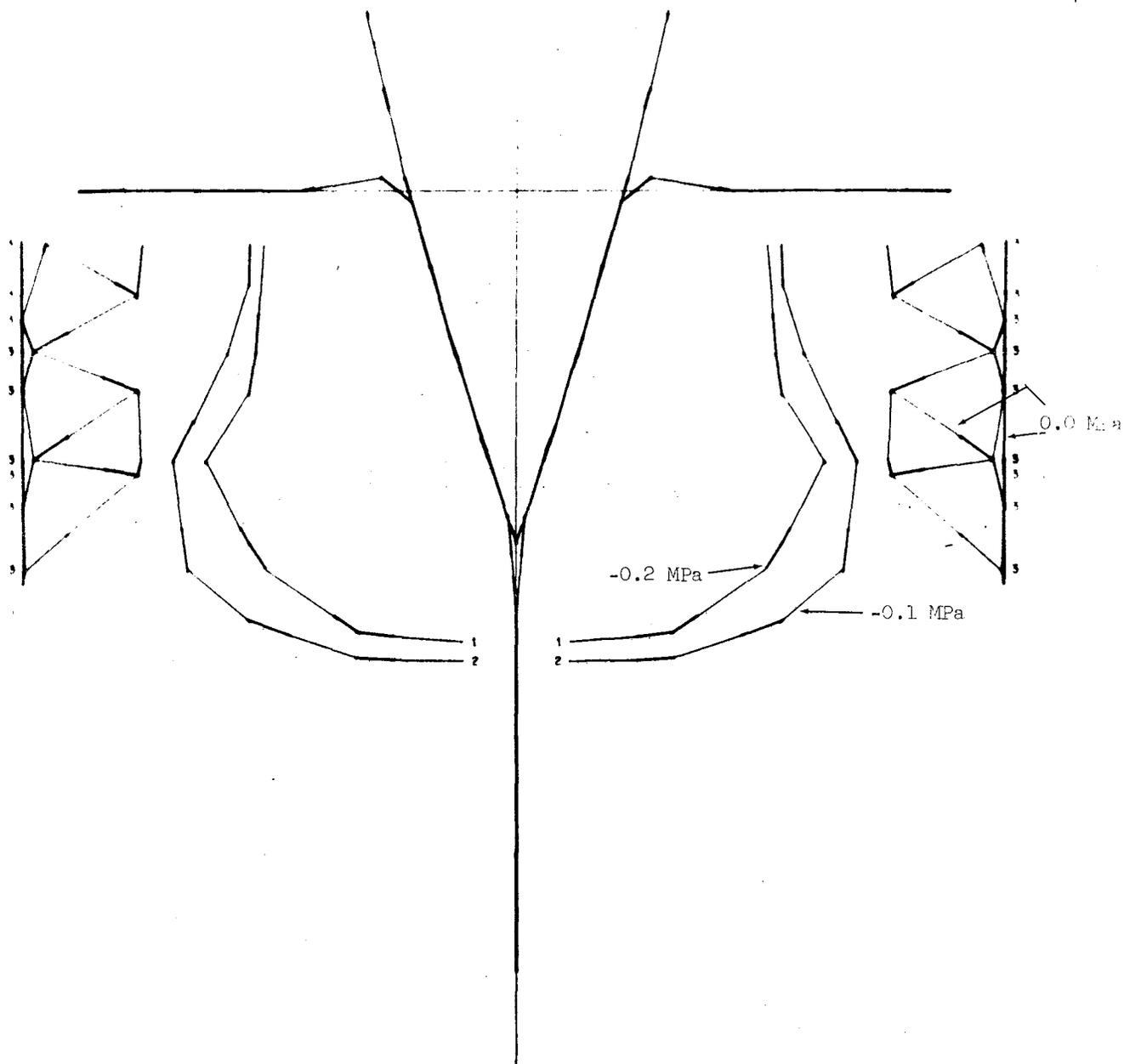


Figure A-82

Contours of Axial Stress in Target. Projectile at 0.1 m Depth.

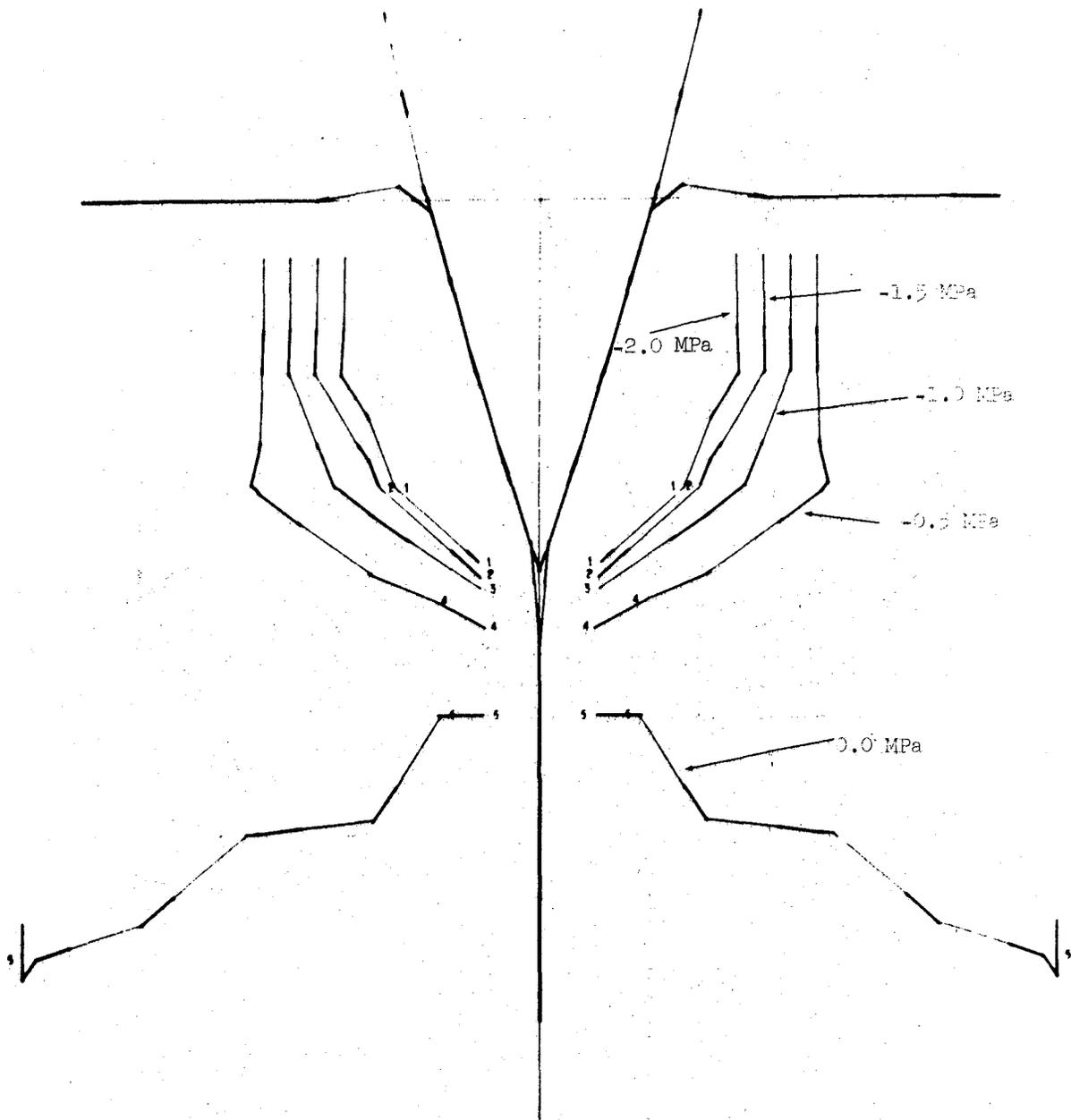


Figure A-83

Contours of Radial Stress in Target. Projectile at 0.1 m Depth.

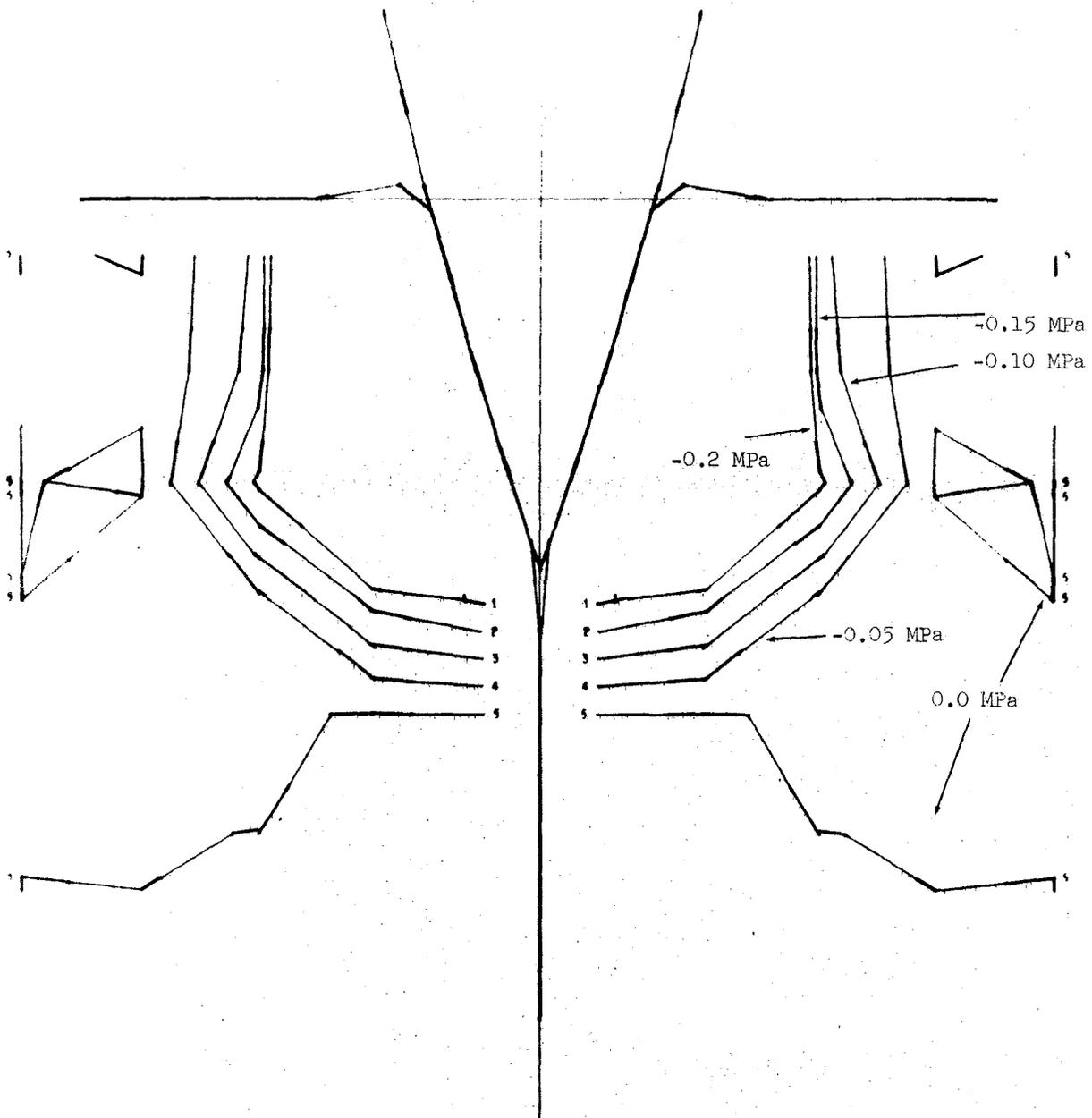


Figure A-84

Contours of Hoop Stress in Target. Projectile at 0.1 m Depth.

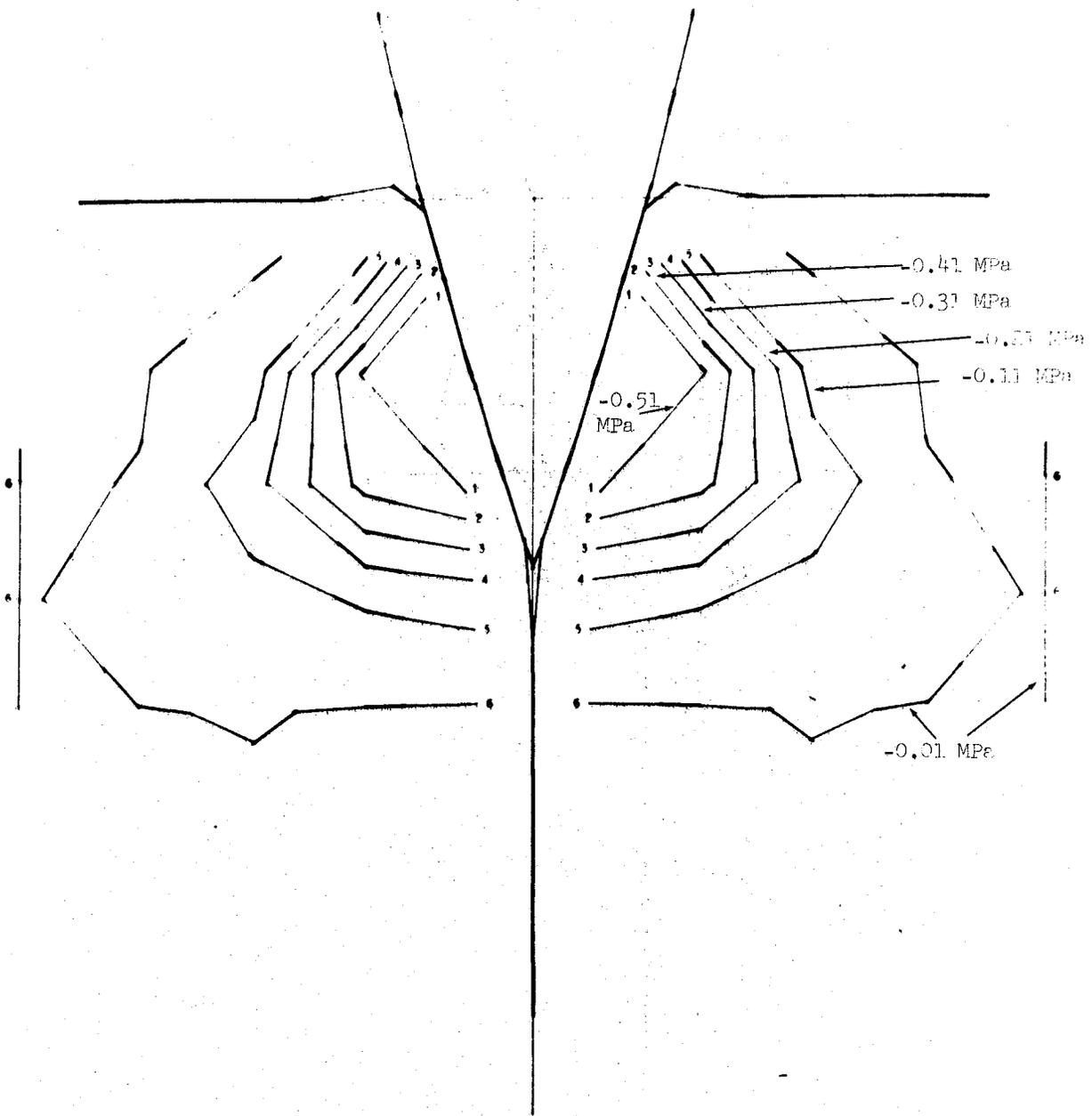


Figure A-85

Contours of Radial-Vertical Shear Stress in Target. Projectile at 0.1 m Depth.

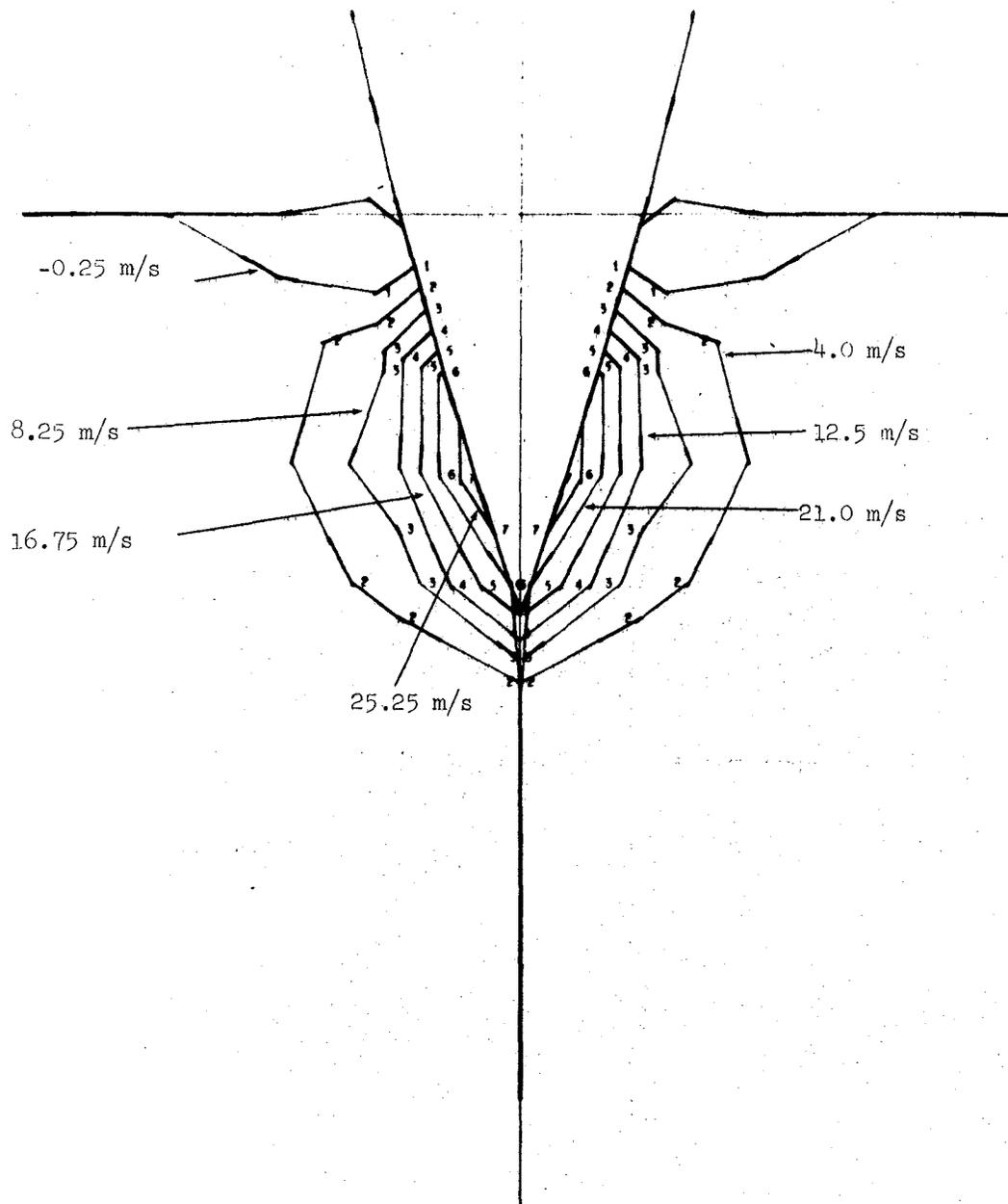


Figure A-86

Contours of Vertical Velocity in Target. Projectile at 0.1 m Depth.

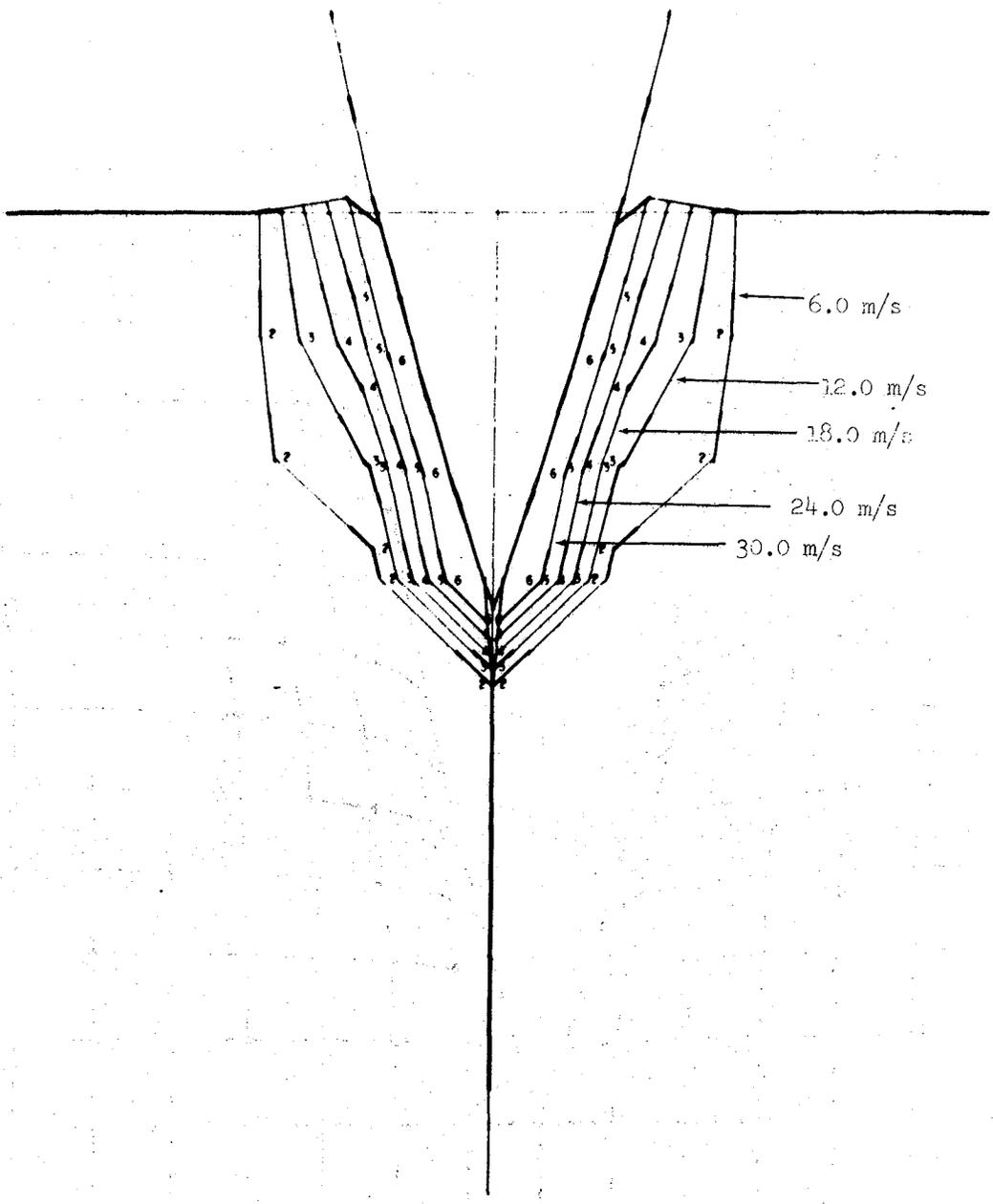


Figure A-87

Contours of Radial Velocity in Target. Projectile at 0.1 m Depth.

EXPLICIT CALCULATION  
CYCLE 174 Z VS. X

.4 m  
2.6 msec

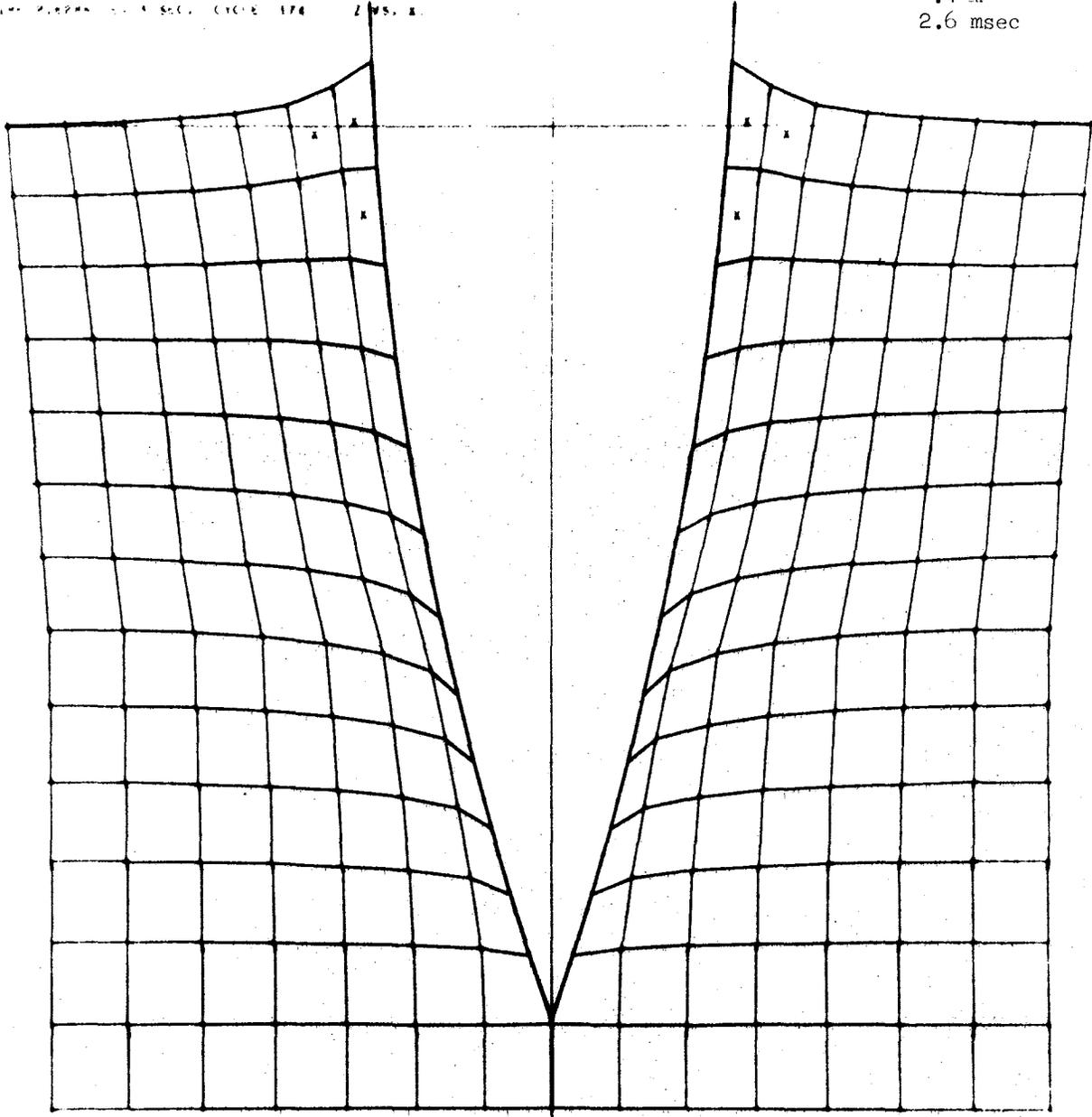


Figure A-88

Lagrangian Coordinates When Projectile has Penetrated to Depth of 0.4 m.

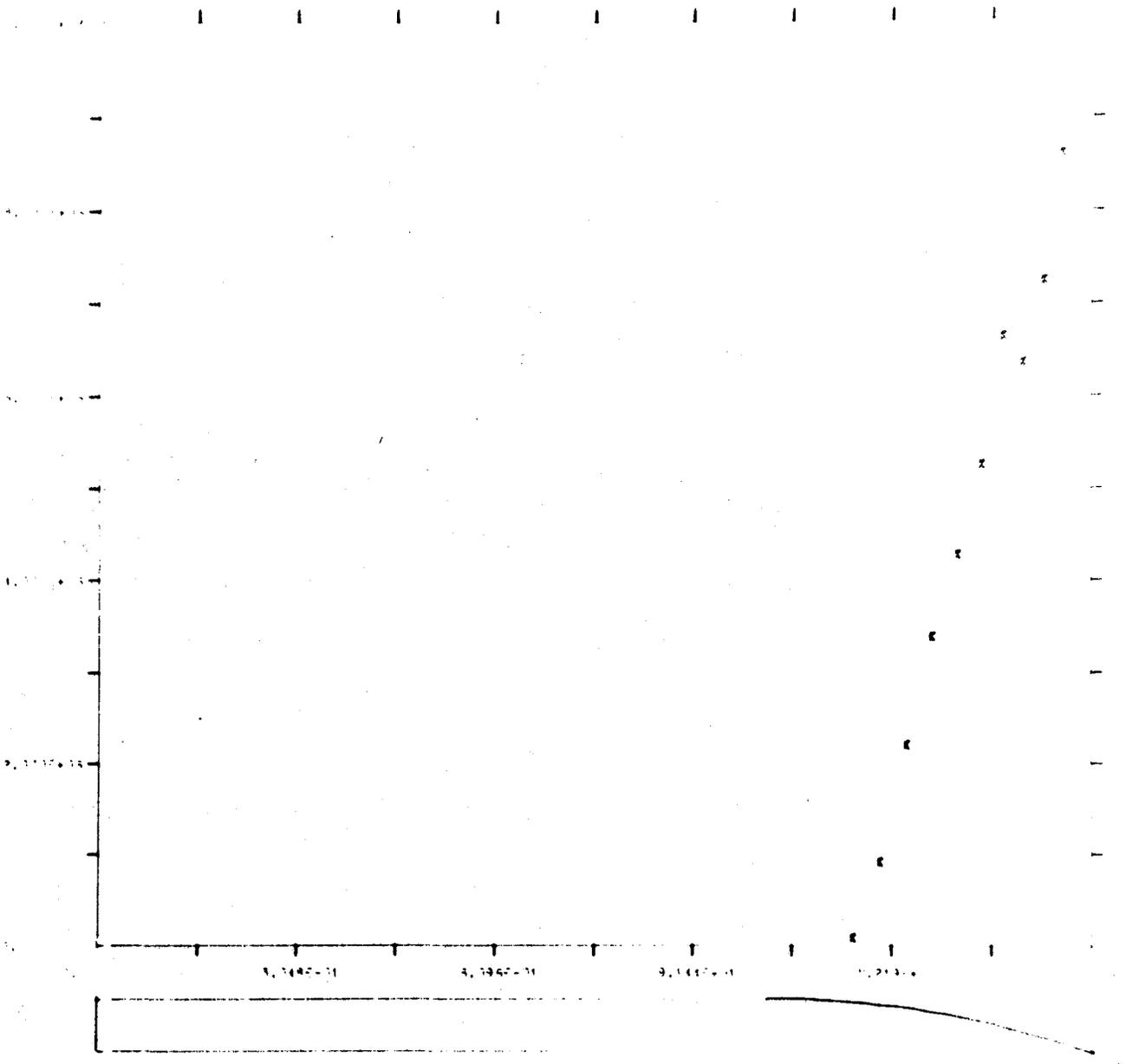


Figure A-89

Normal Stress (Pa) Along Surface of Projectile When Projectile is at 0.4 m Depth.

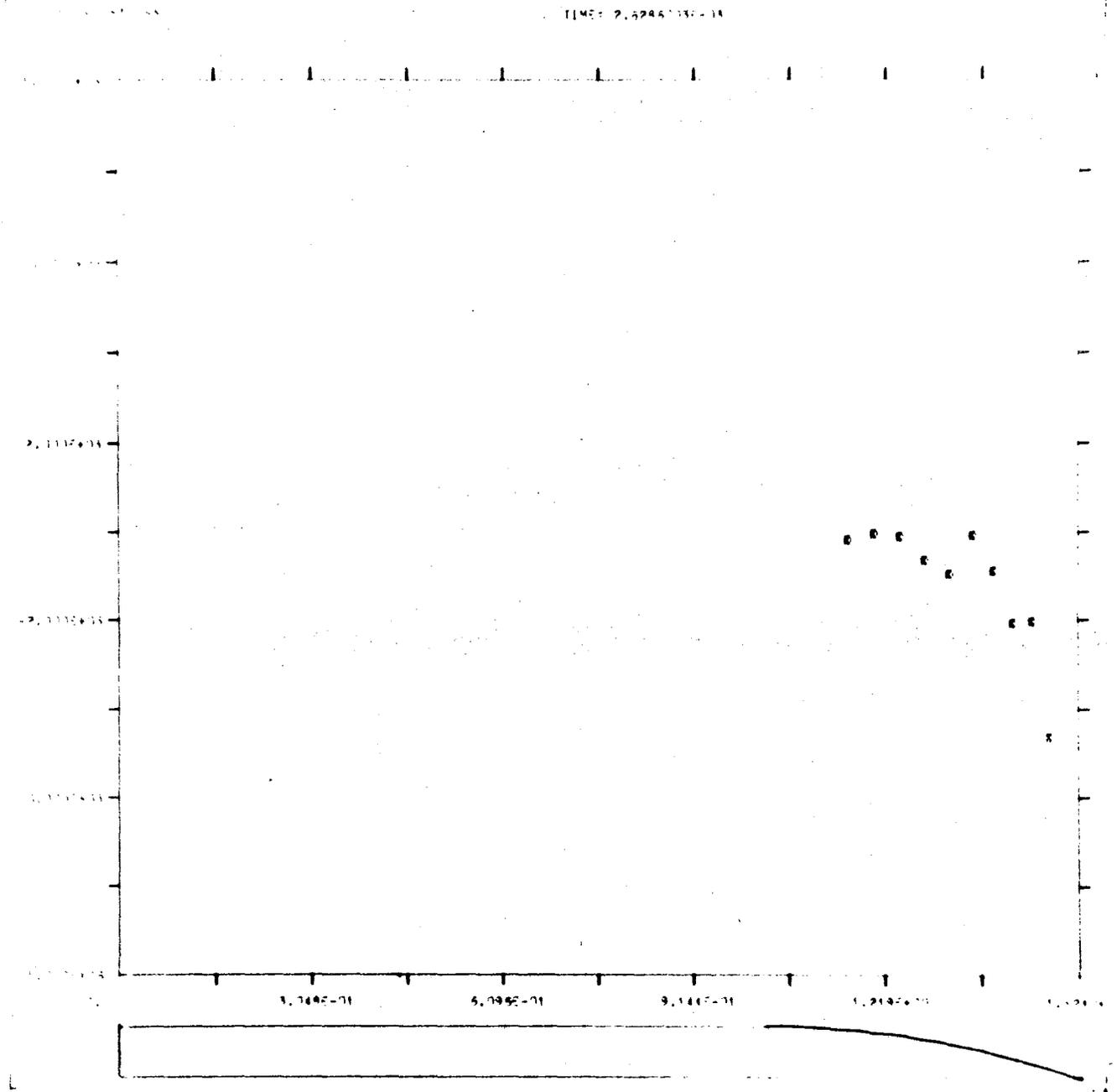


Figure A-90

Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 0.4 m Depth.

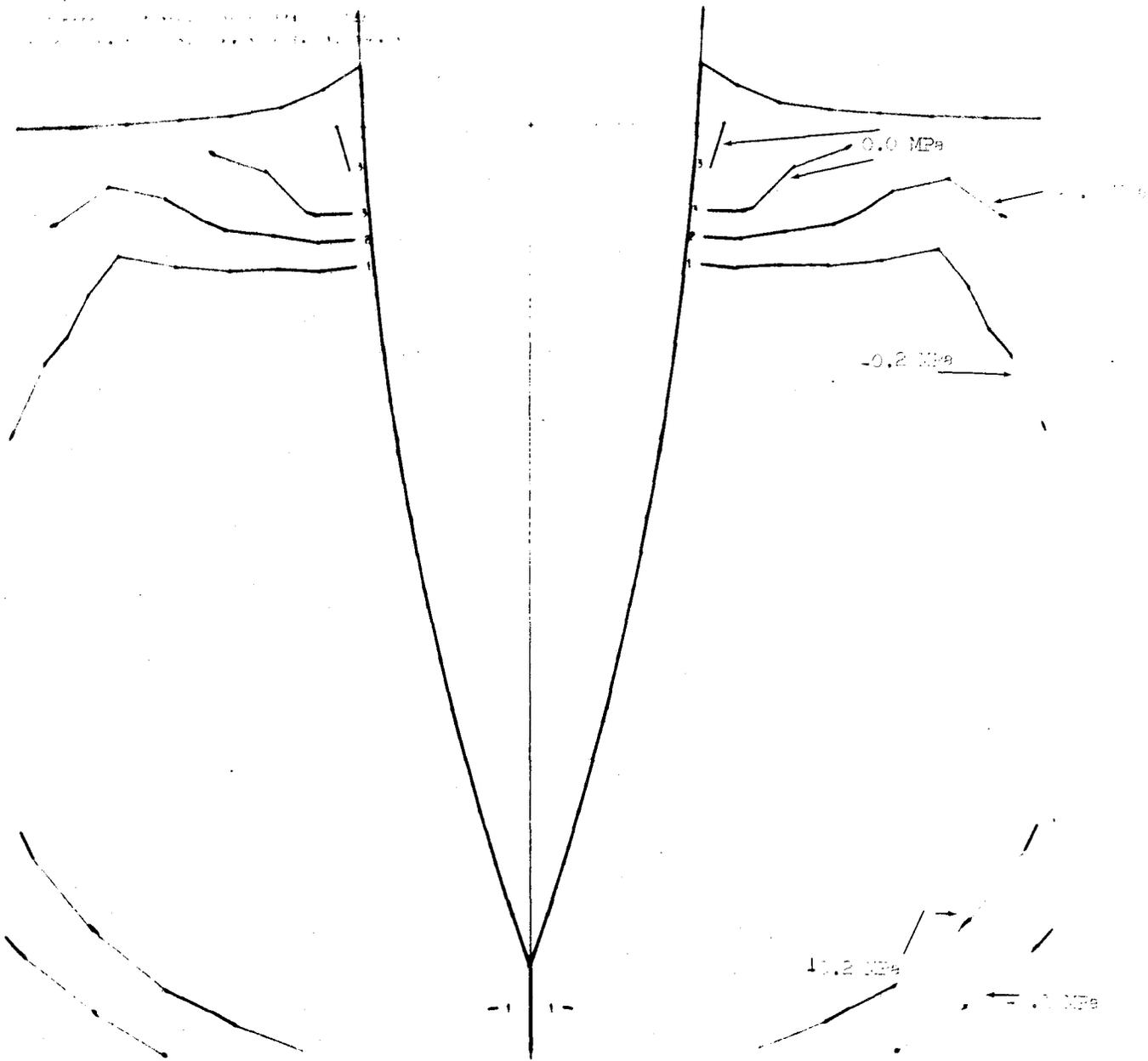


Figure A-91  
 Contours of Axial Stress in Target. Projectile at 0.4 m Depth.

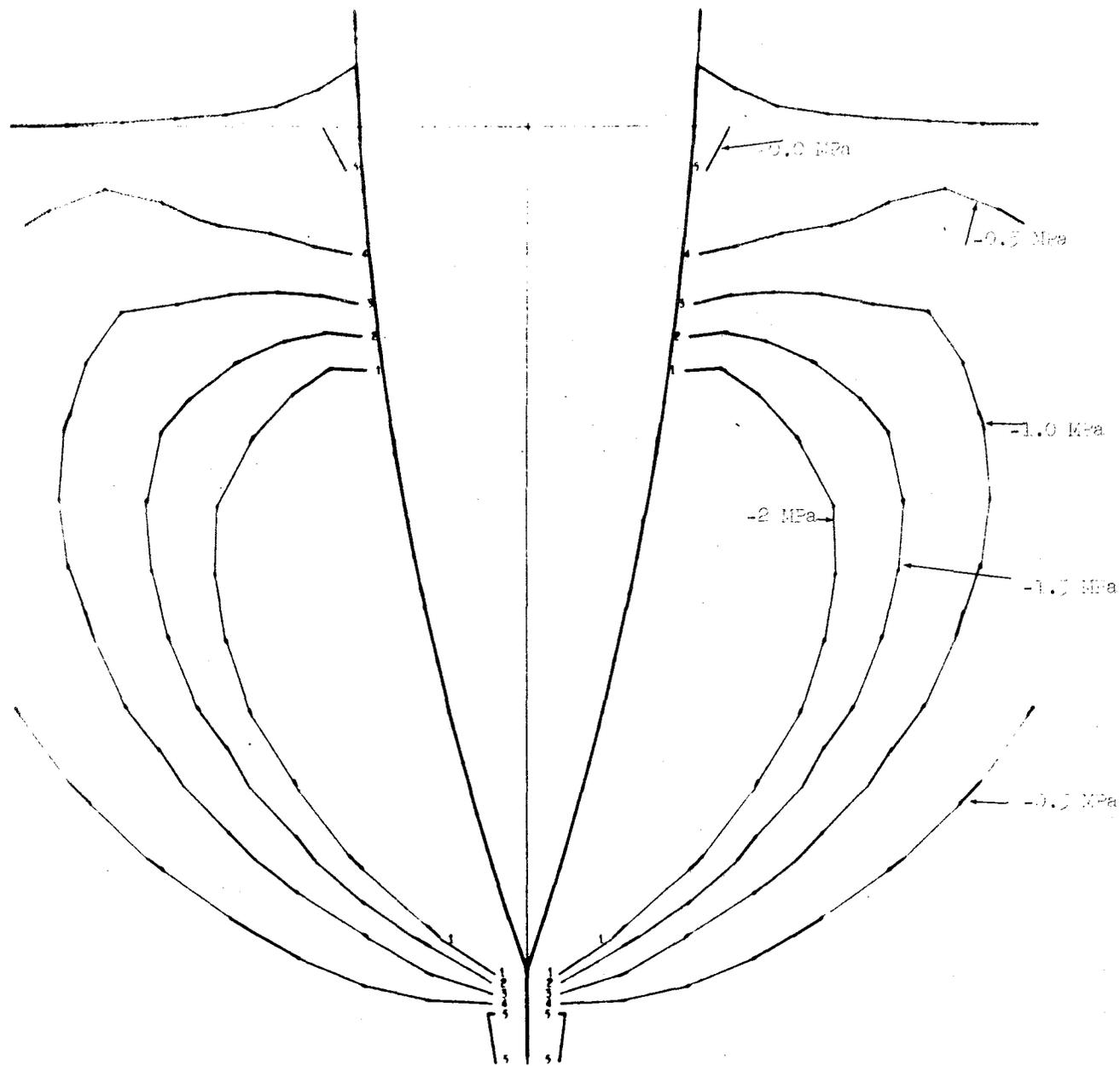


Figure A-92

Contours of Radial Stress in Target. Projectile at 0.4 m Depth.

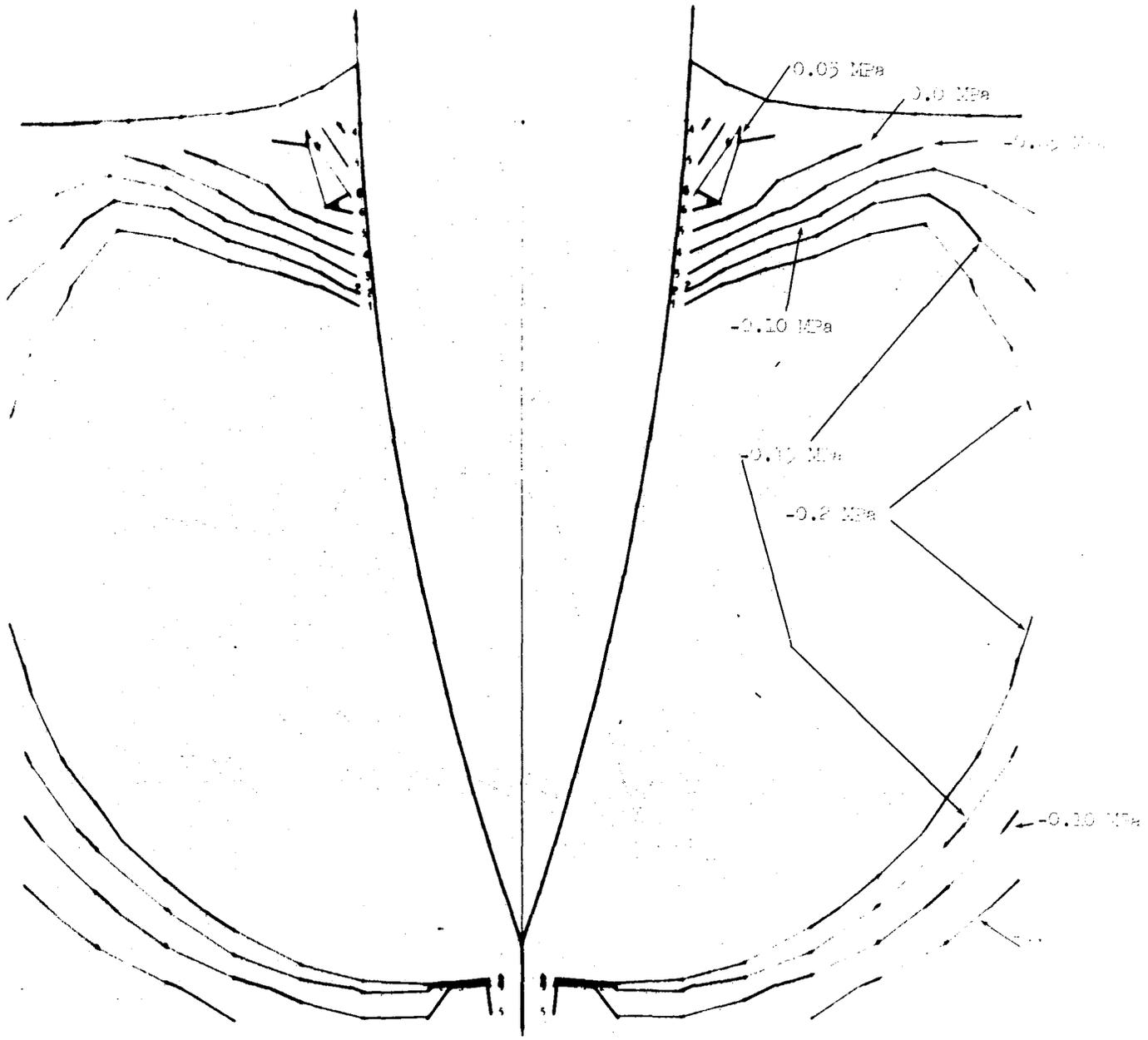


Figure A-93  
Contours of Hoop Stress in Target. Projectile at 0.4 m Depth.

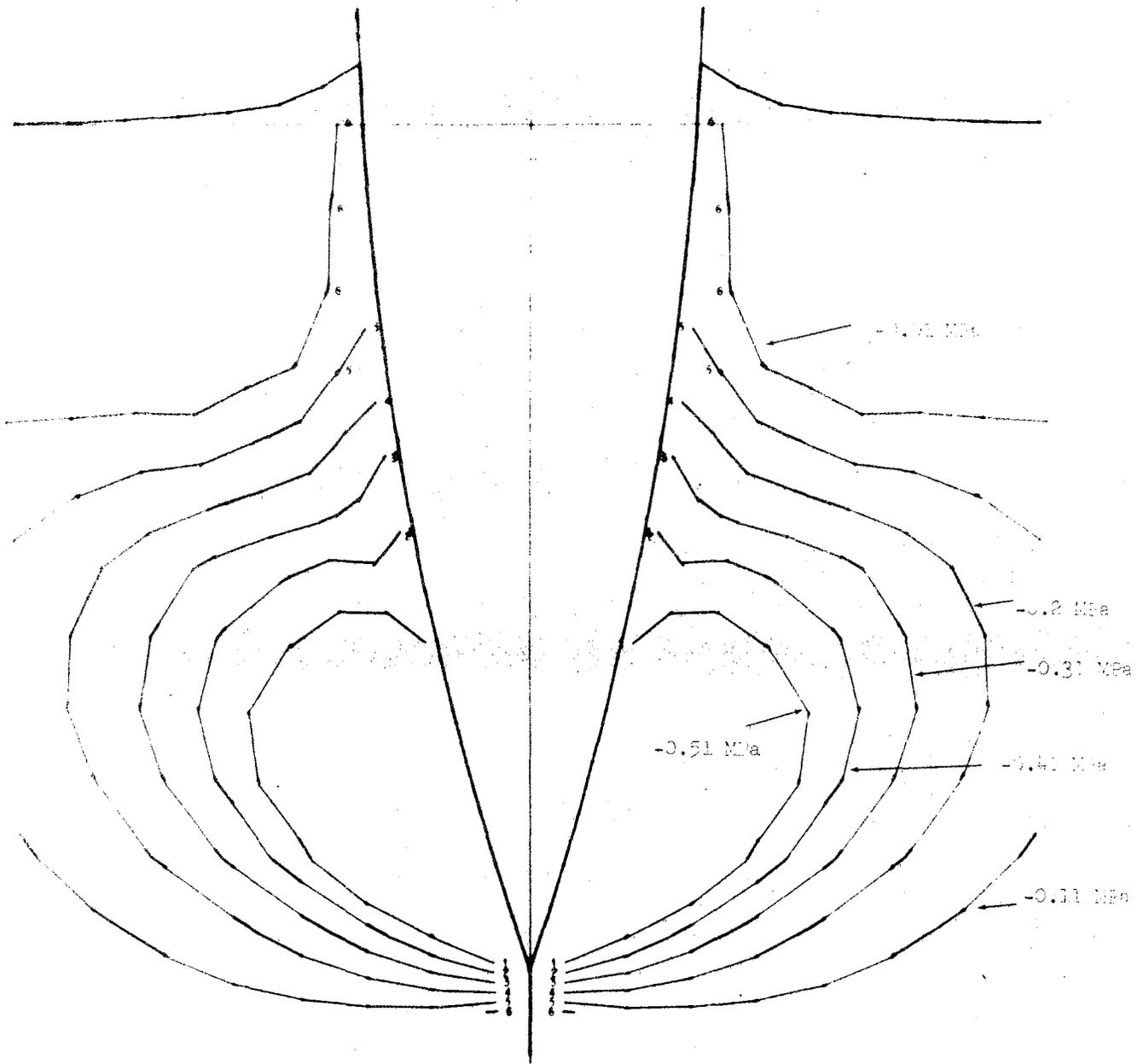


Figure A-94

Contours of Radial-Vertical Shear Stress in Target. Projectile at 0.4 m Depth.

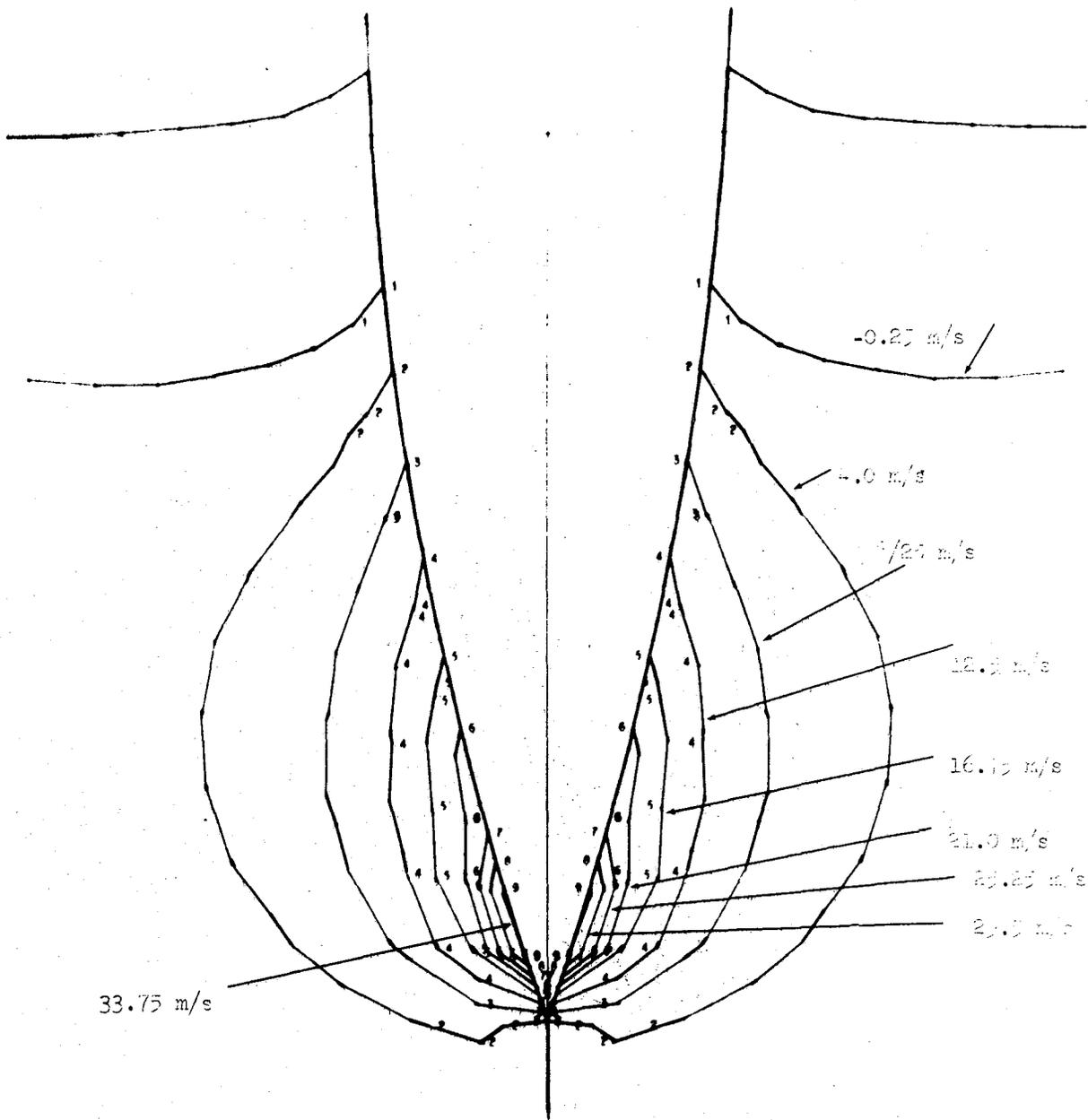


Figure A-95

Contours of Vertical Velocity in Target. Projectile at 0.4 m Depth.

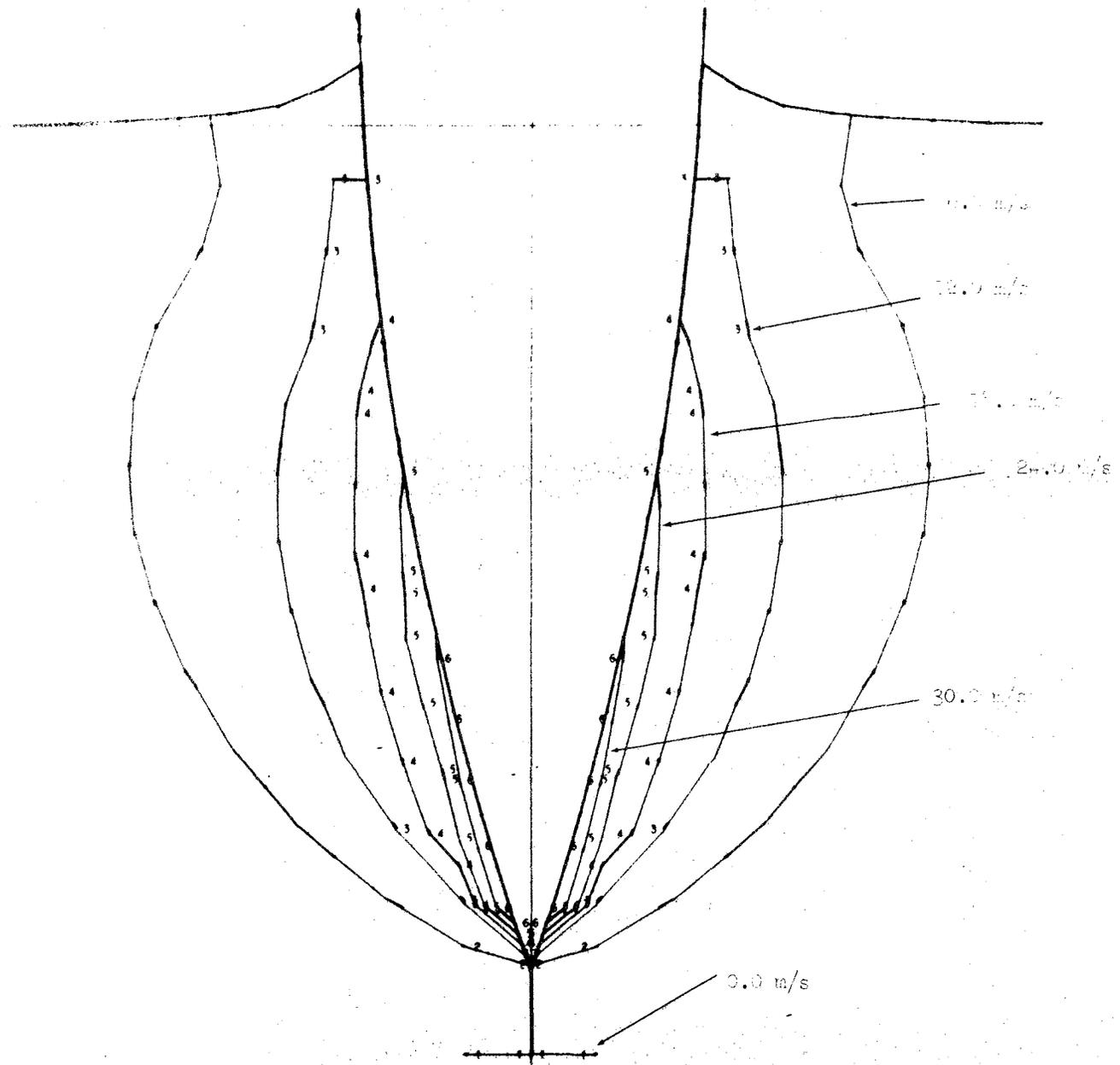


Figure A-96

Contours of Radial Velocity in Target. Projectile at 0.4 m Depth.

2.0 m  
13.4 m sec

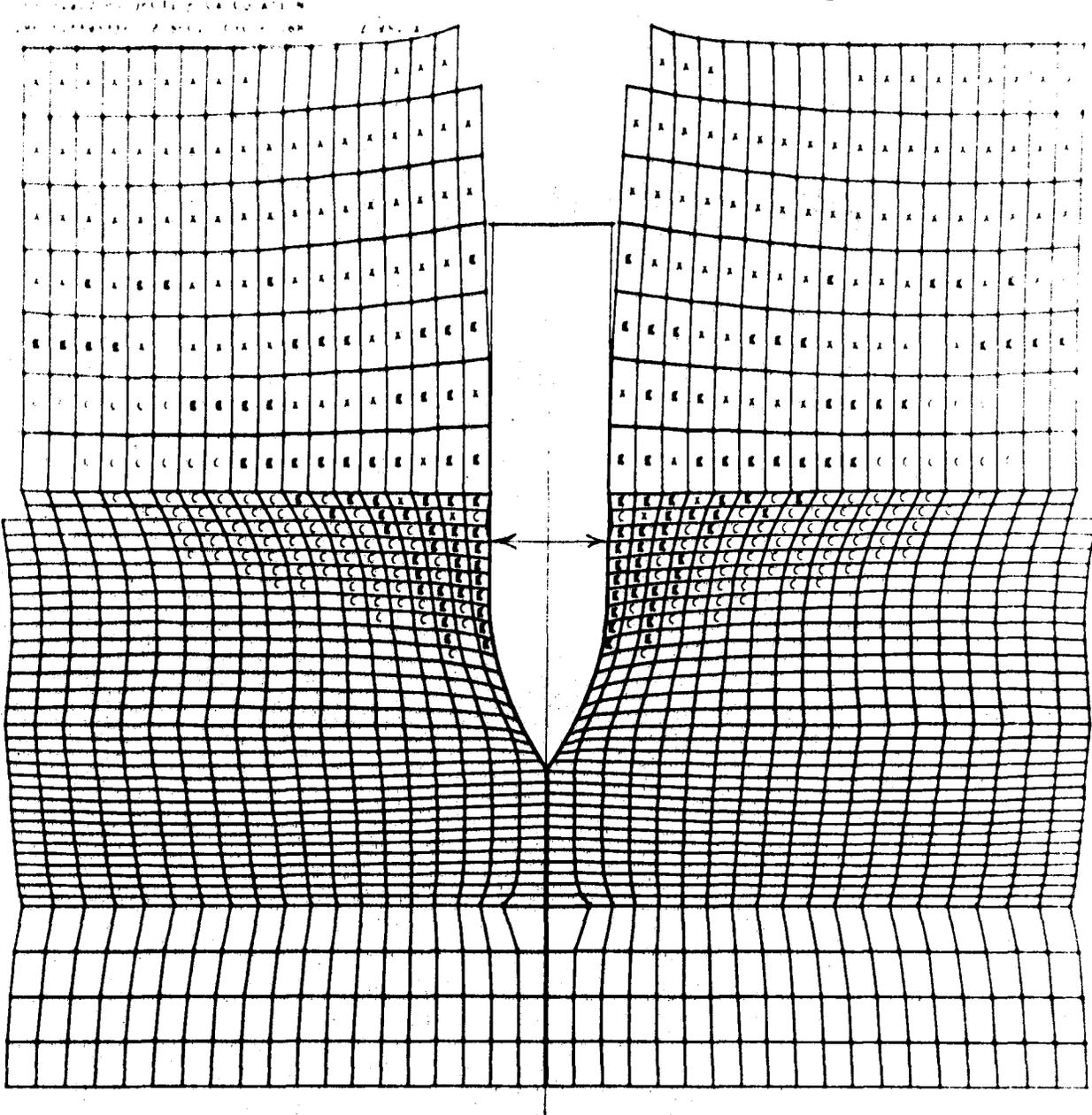


Figure A-97

Lagrangian Coordinates When Projectile has Penetrated to Depth of 2.0 m. Radial Dimensions Doubled for Clarity.



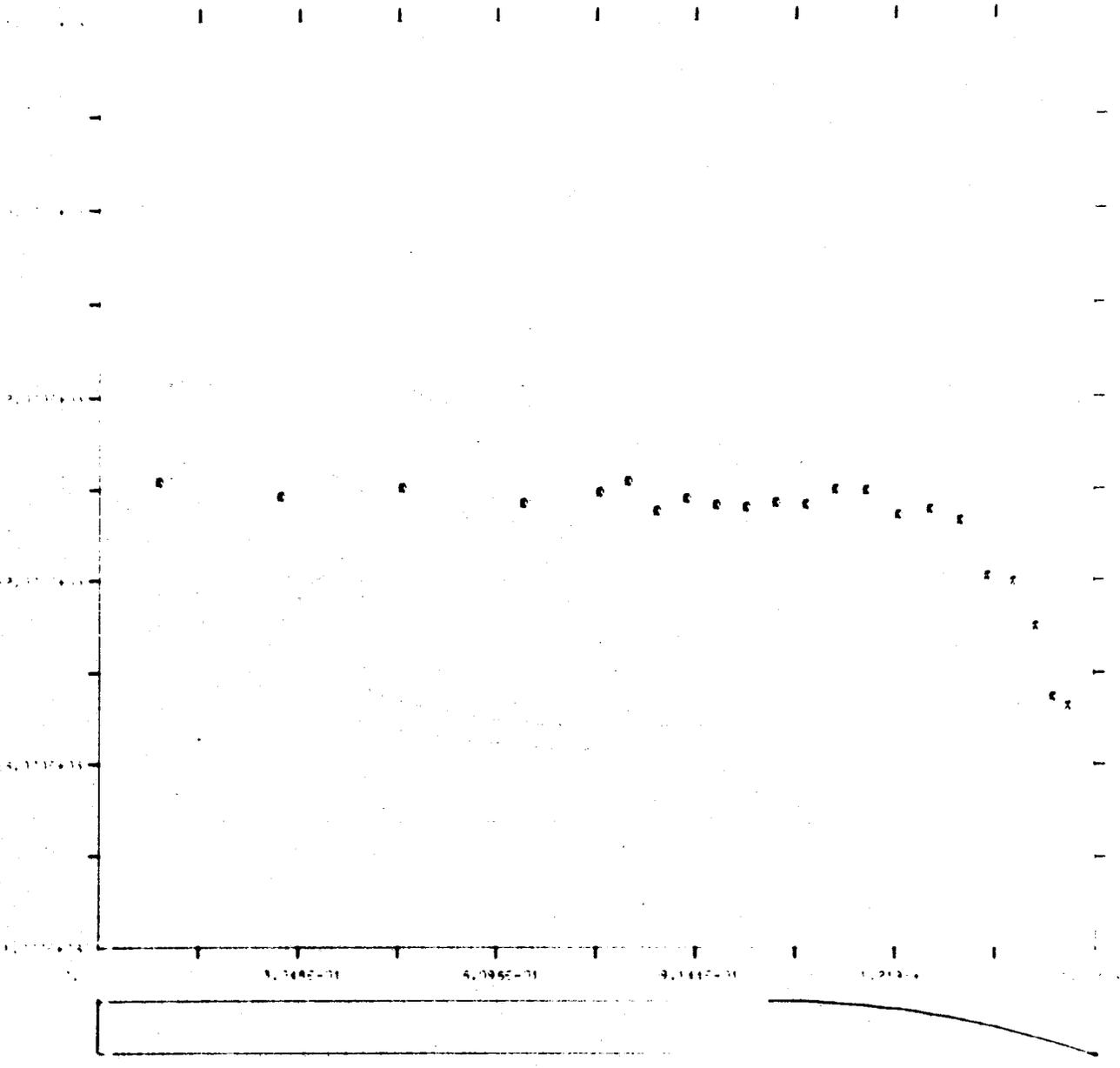


Figure A-99  
Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 2.0 m Depth.

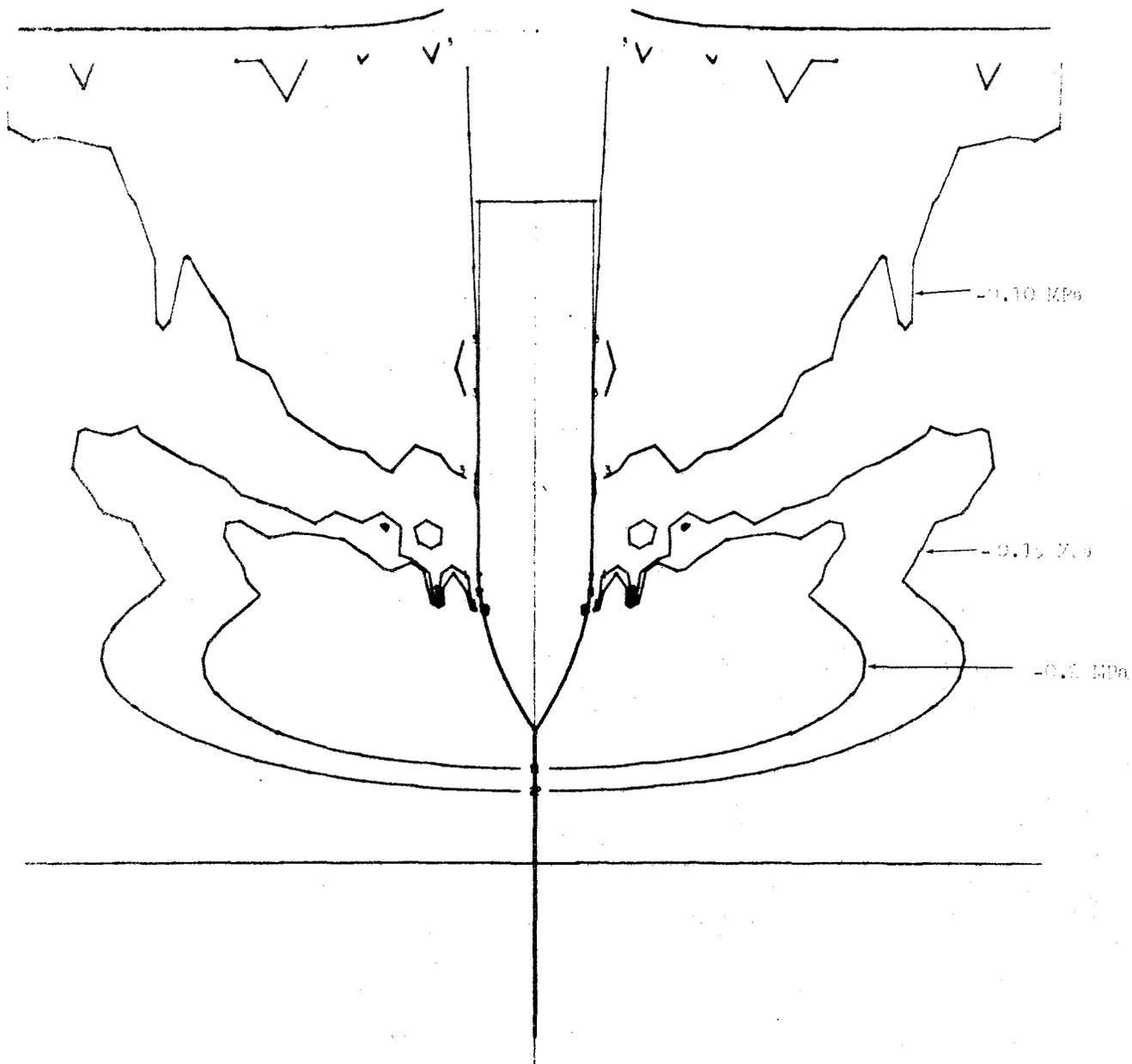


Figure A-100  
Contours of Axial Stress in Target. Projectile at 2.0 m Depth.

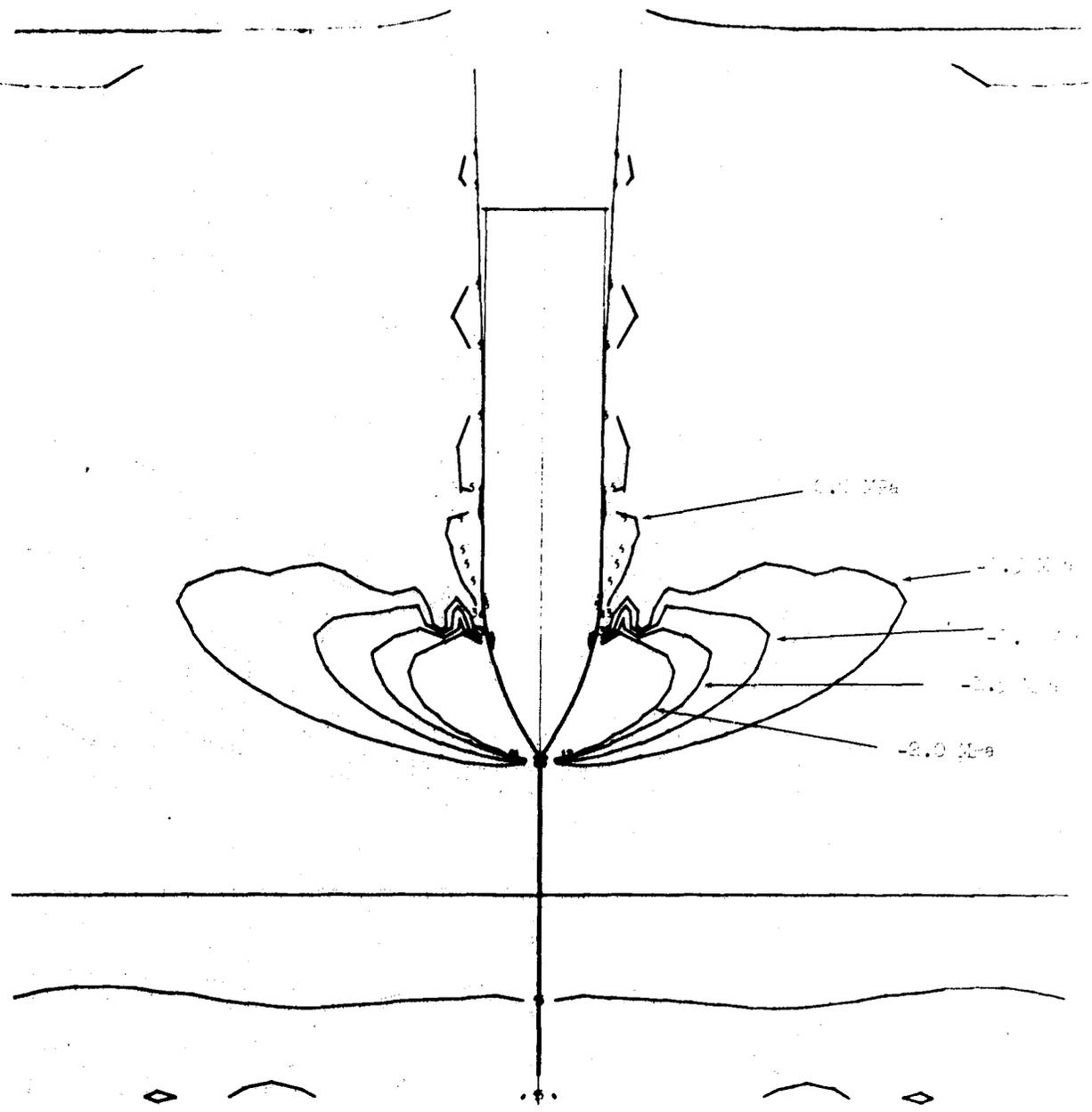


Figure A-101  
Contours of Radial Stress in Target. Projectile at 2.0 m Depth.

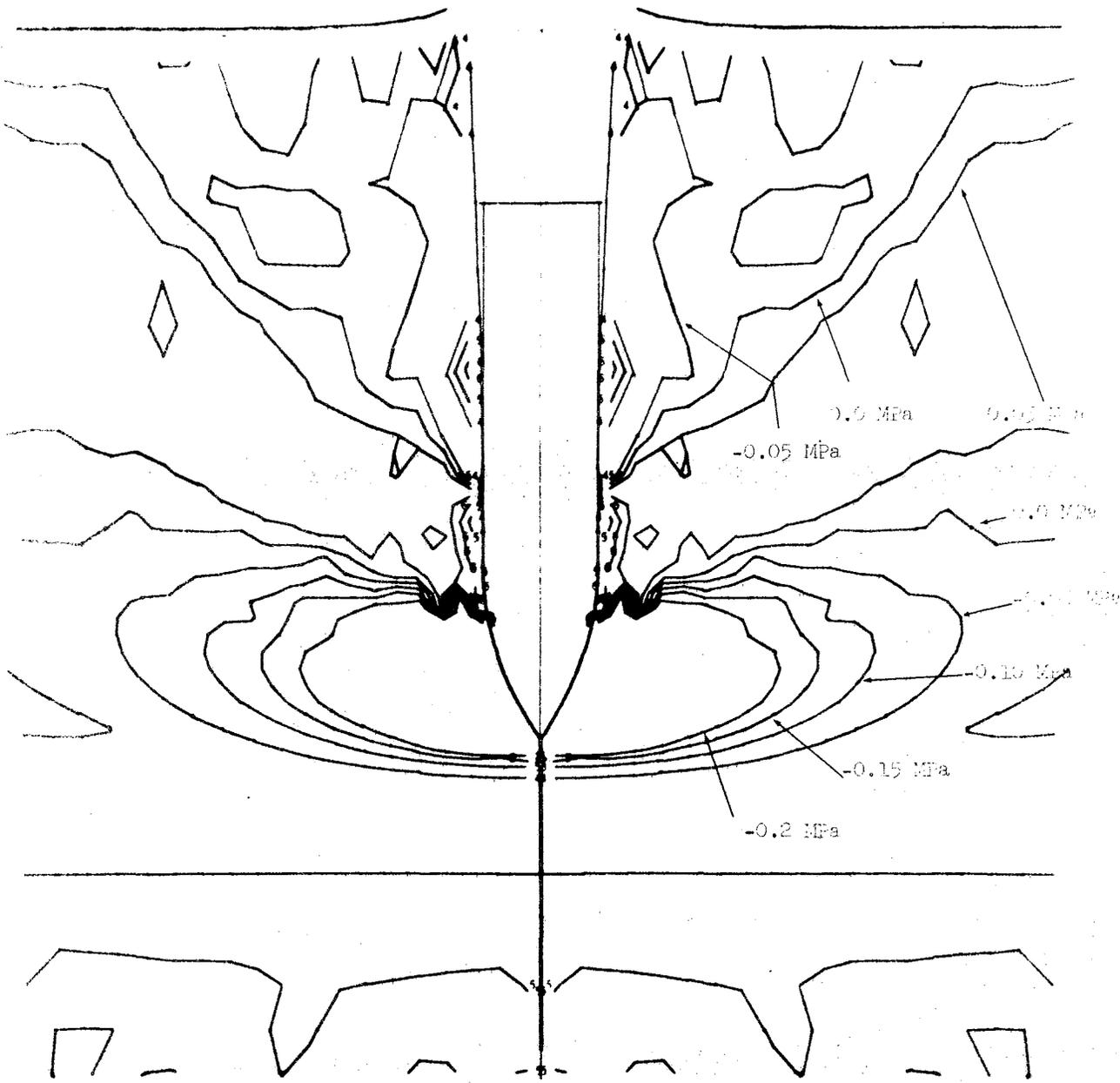


Figure A-102

Contours of Hoop Stress in Target. Projectile at 2.0 m Depth.

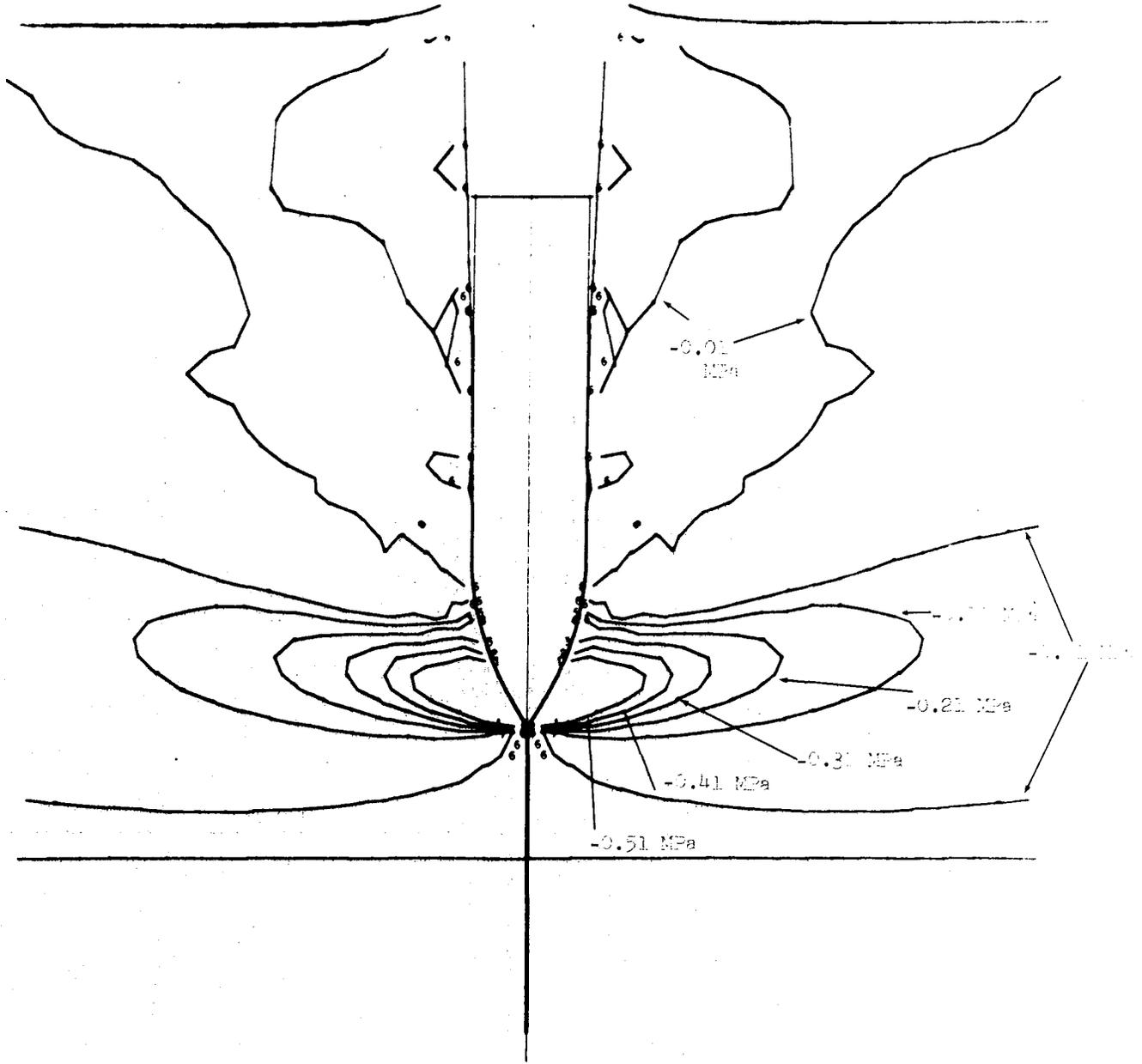


Figure A-103  
 Contours of Radial Vertical Shear Stress in Target. Projectile at 2.0 m Depth.

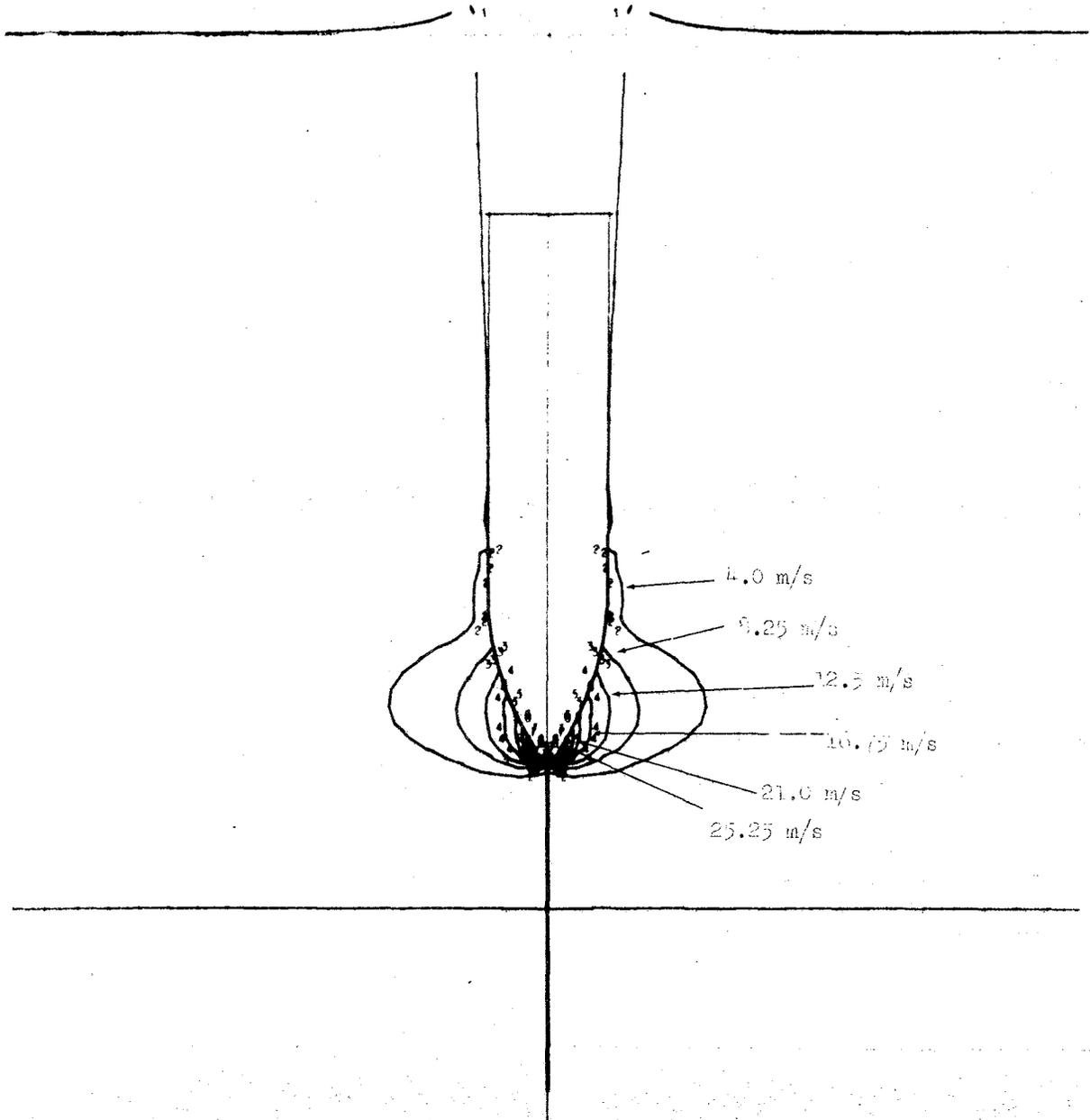


Figure A-104

Contours of Vertical Velocity in Target. Projectile at 2.0-m Depth.

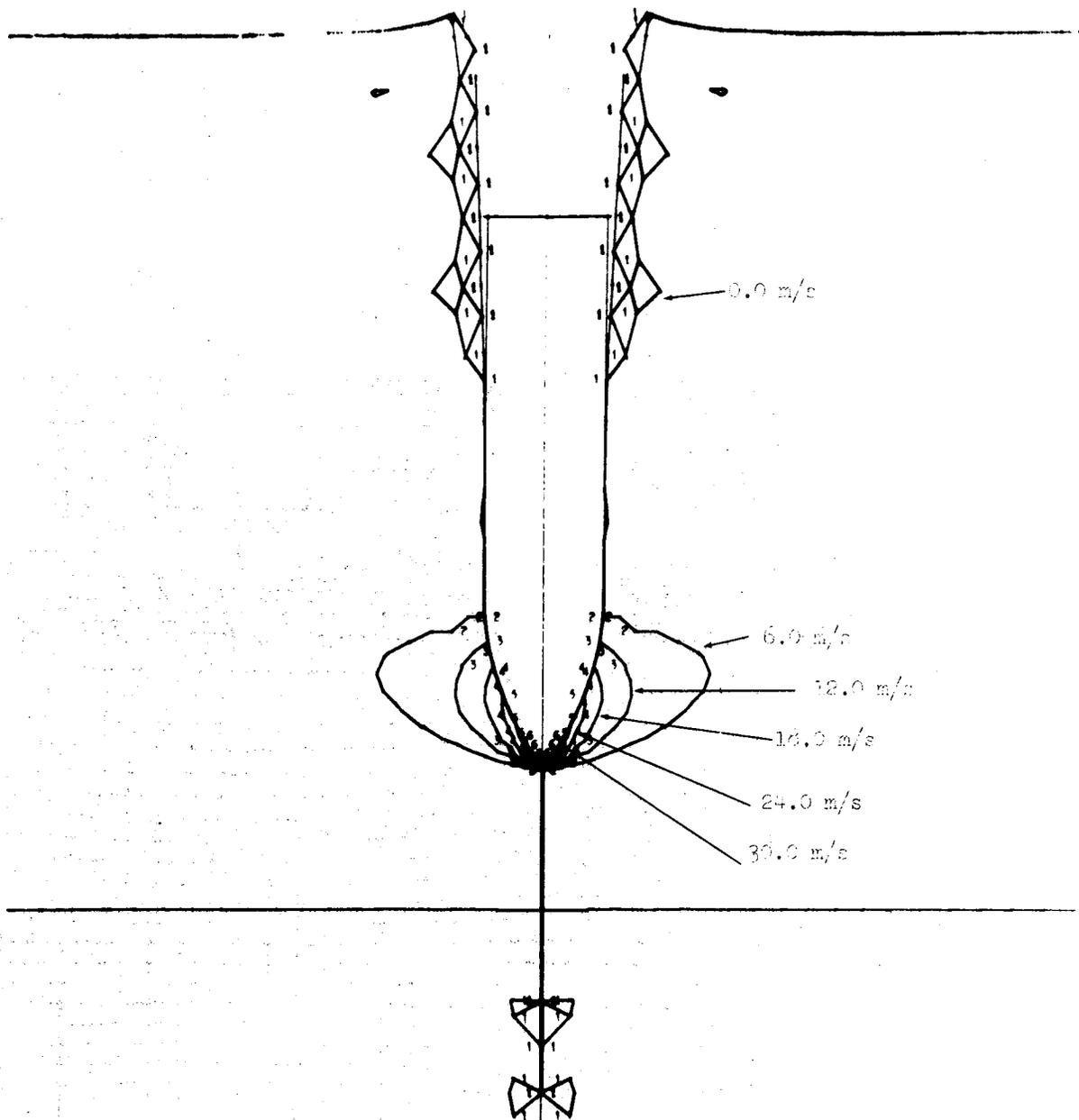


Figure A-105

Contours of Radial Velocity in Target. Projectile at 2.0 m Depth.

2.8 m  
18.9 msec

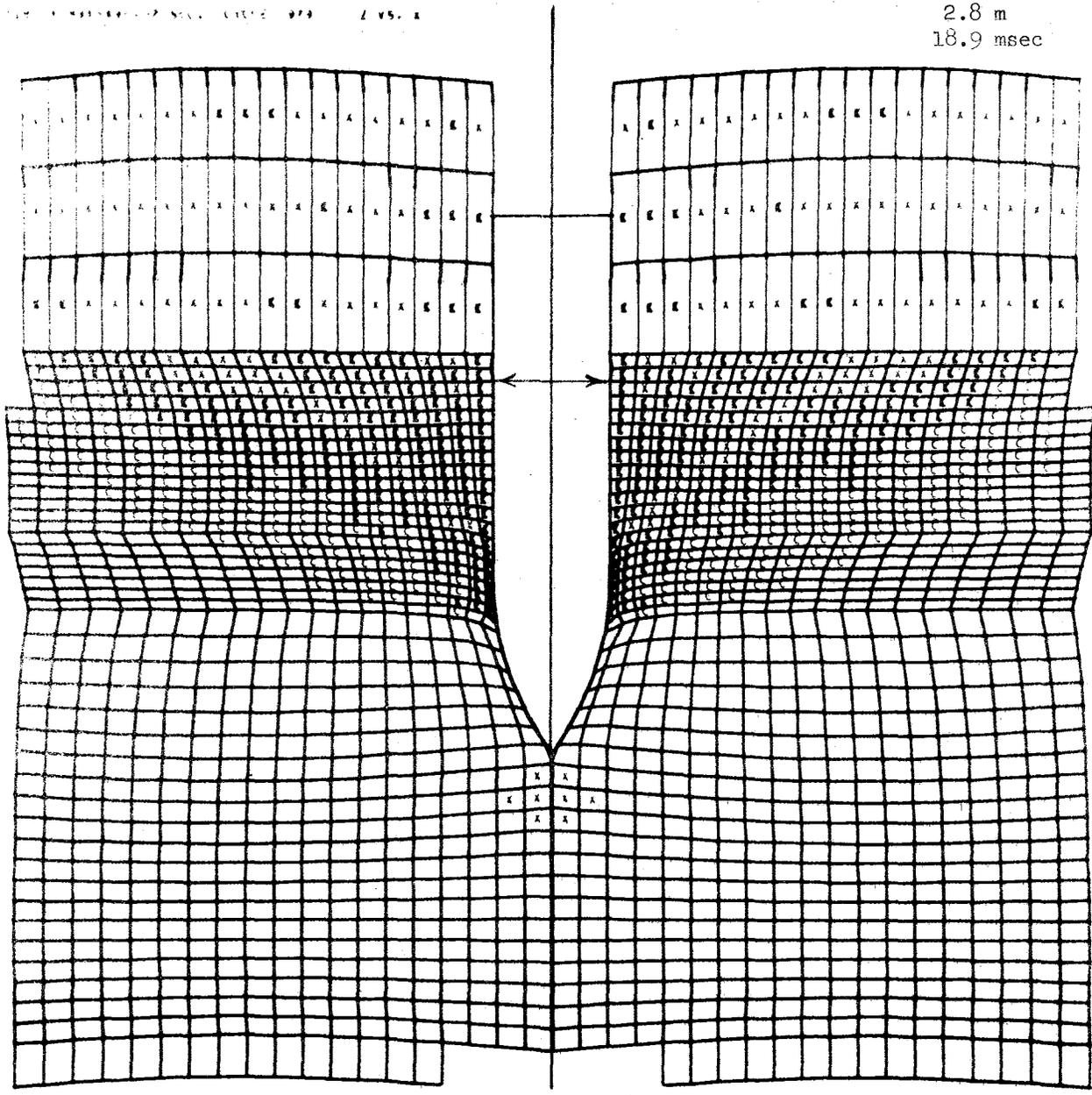


Figure A-106

Lagrangian Coordinates When Projectile has Penetrated to Depth of 2.8 m. Radial Dimensions Doubled for Clarity.

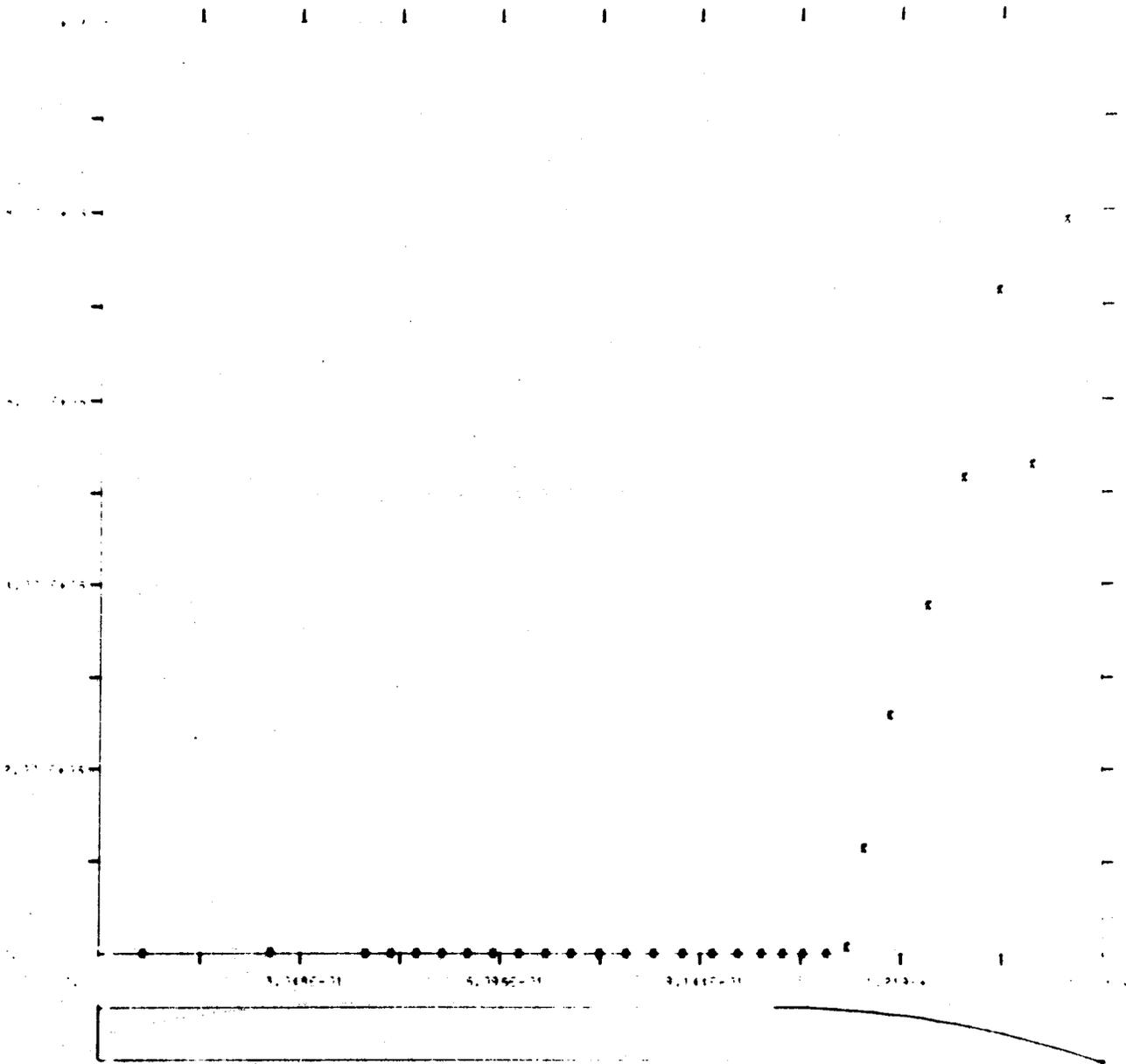


Figure A-107

Normal Stress (Pa) Along Surface of Projectile When Projectile is at 2.8 m Depth.

TIME: 1.893192E-02

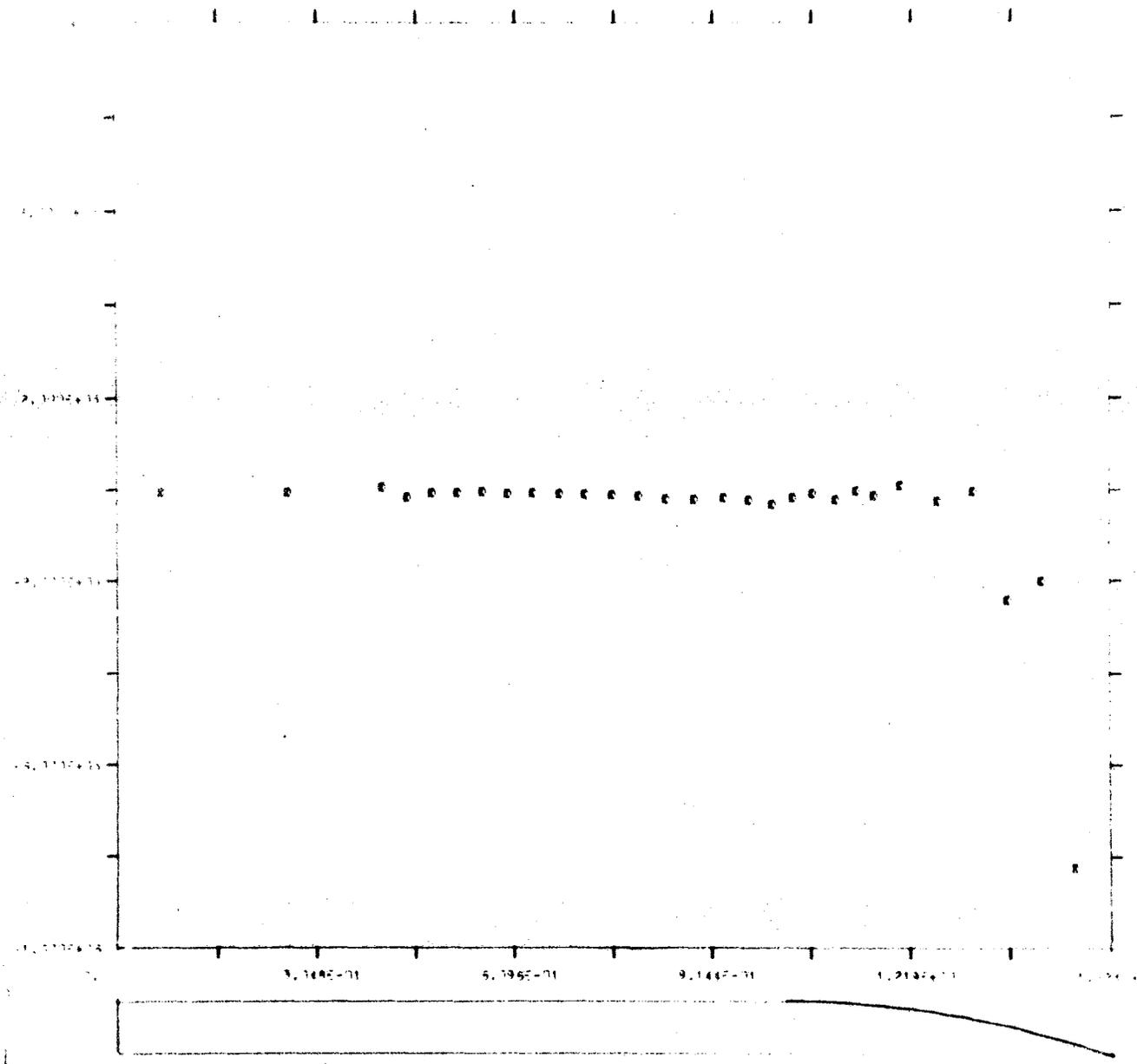


Figure A-108  
Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 2.8 m Depth.

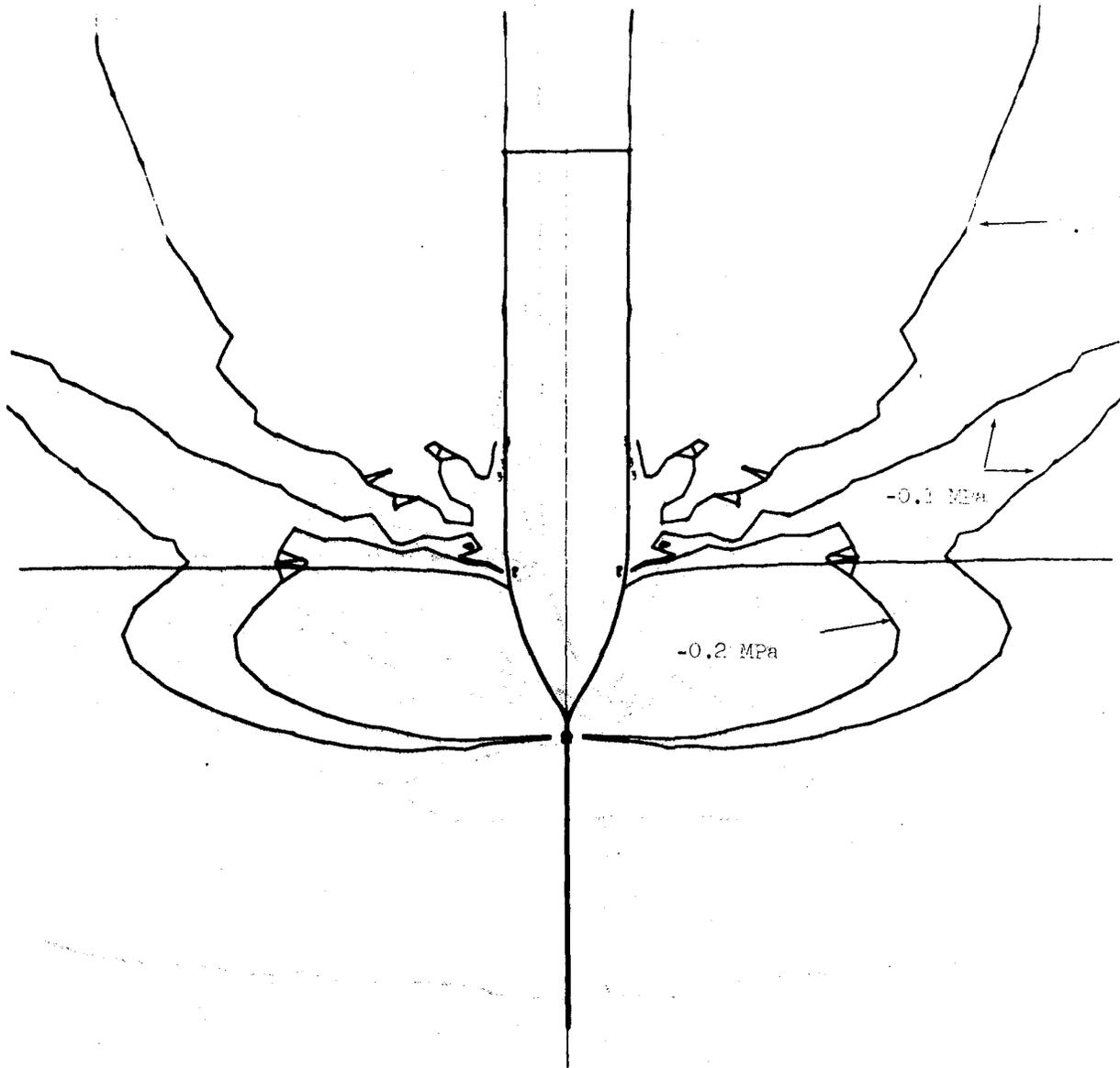


Figure A-109  
Contours of Axial Stress in Target. Projectile at 2.8 m Depth.

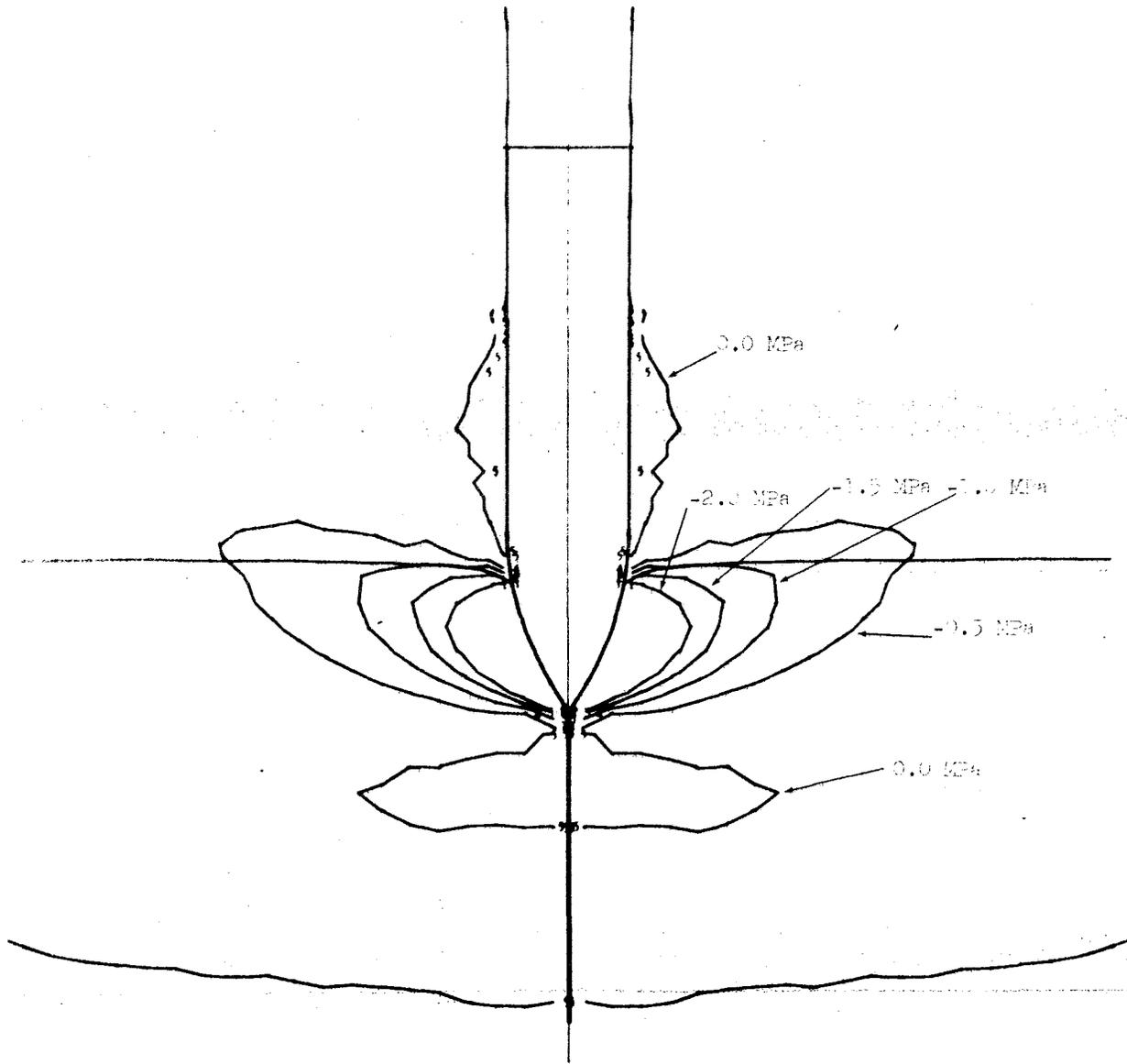


Figure A-110  
Contours of Radial Stress in Target. Projectile at 2.8 m Depth.

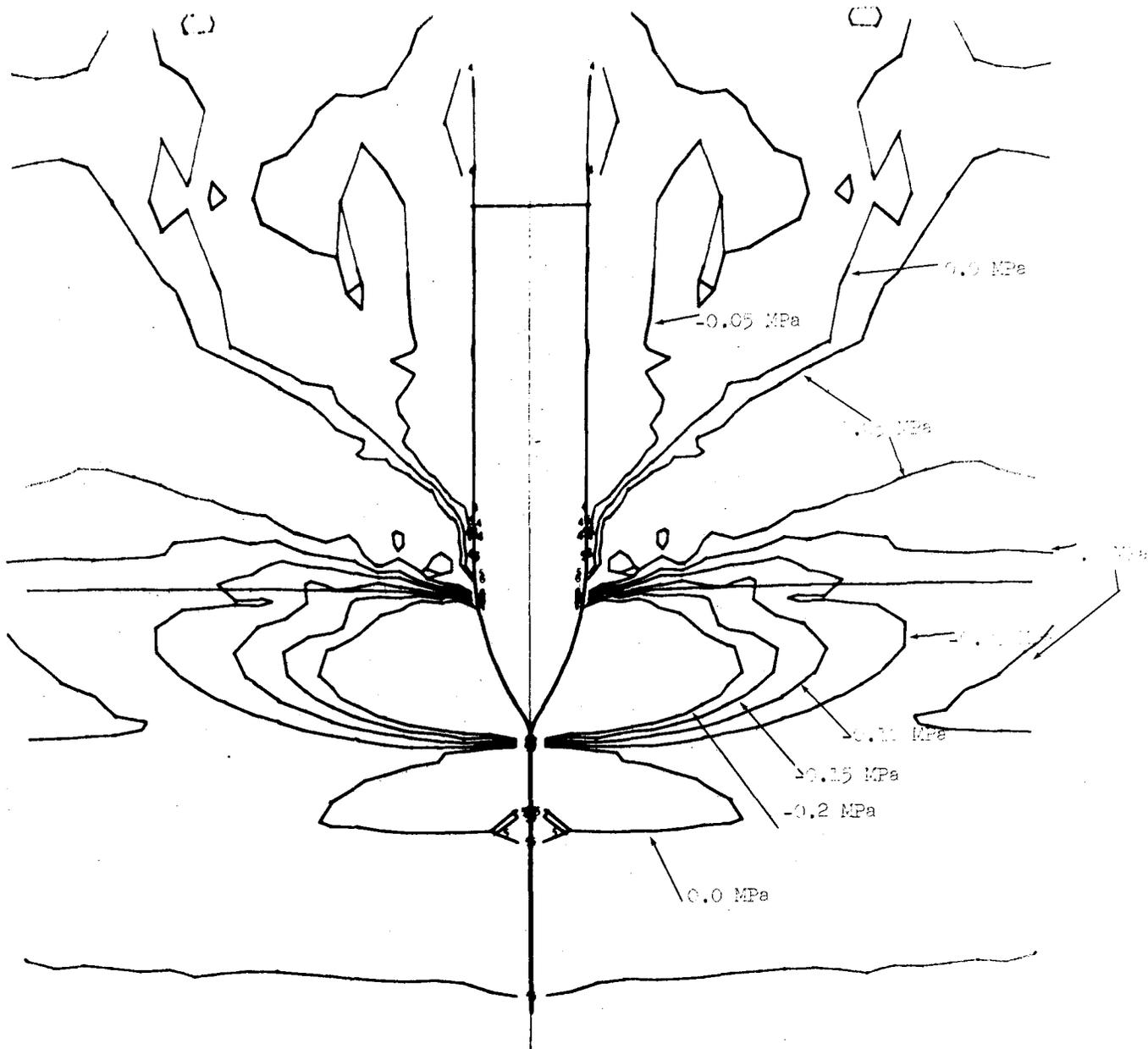


Figure A-111  
 Contours of Hoop Stress in Target. Projectile at 2.8 m Depth.

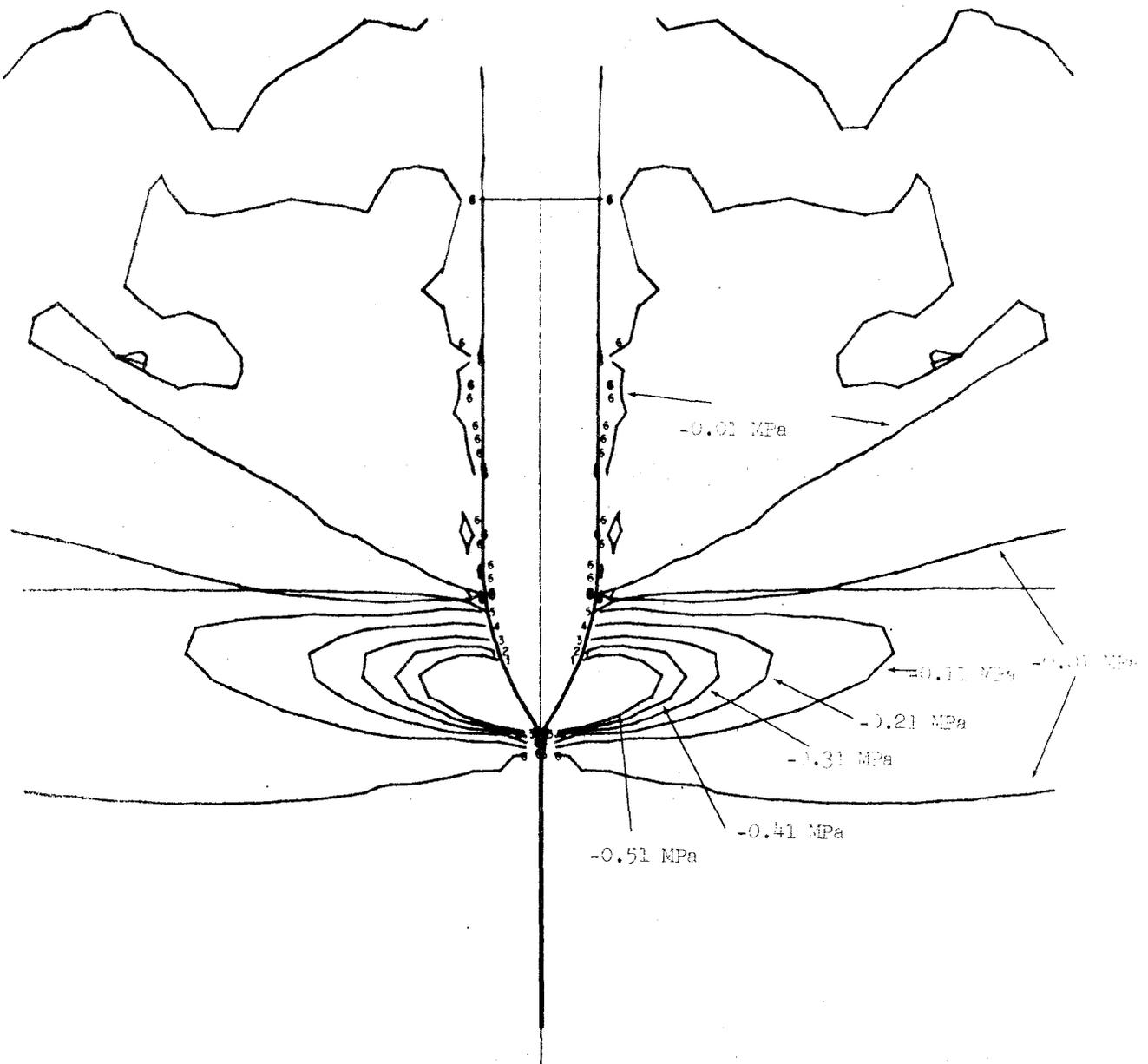


Figure A-112

Contours of Radial Vertical Shear Stress in Target. Projectile at 2.8 m Depth.

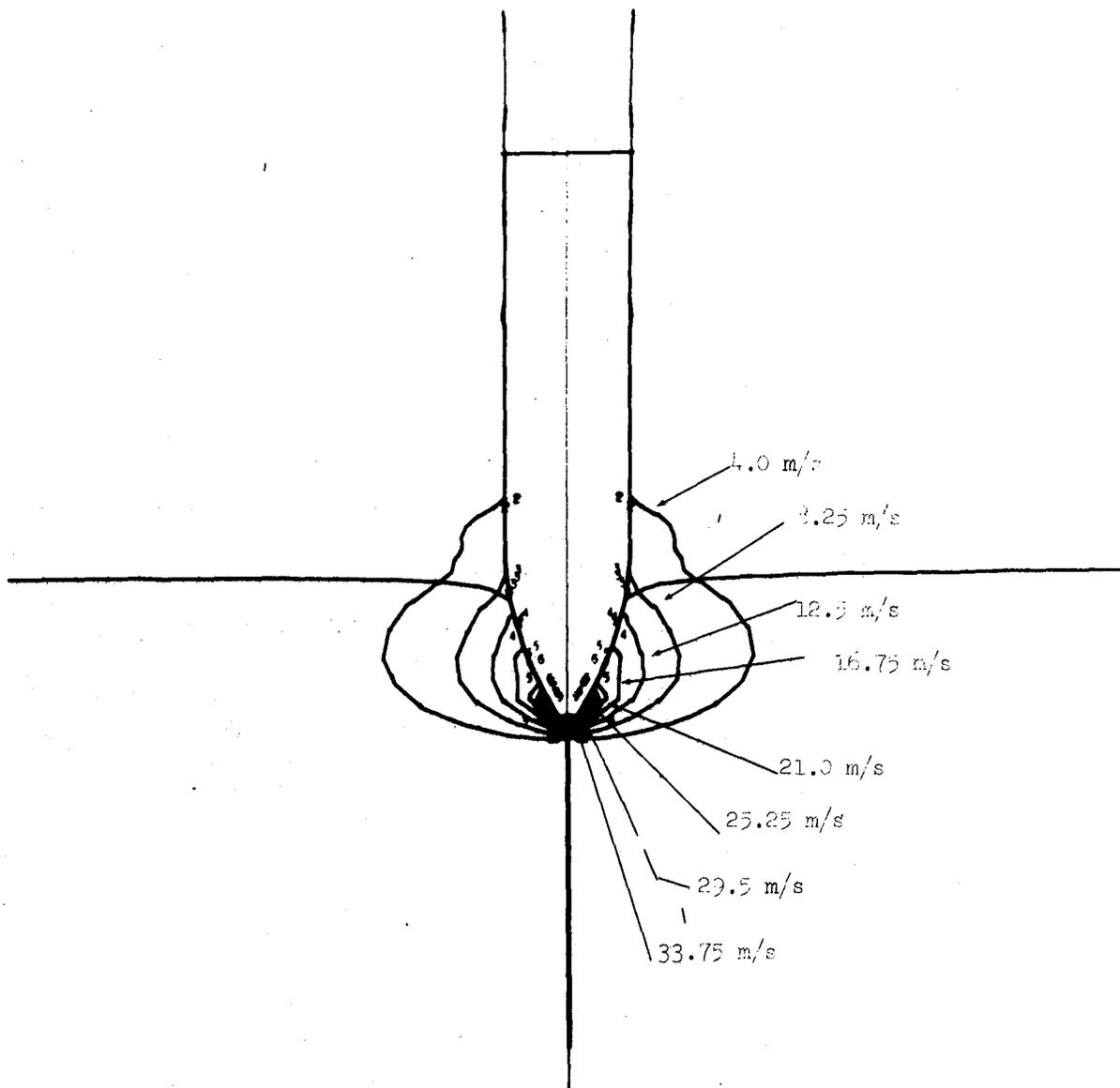


Figure A-113  
Contours of Vertical Velocity in Target. Projectile at 2.8 m Depth.

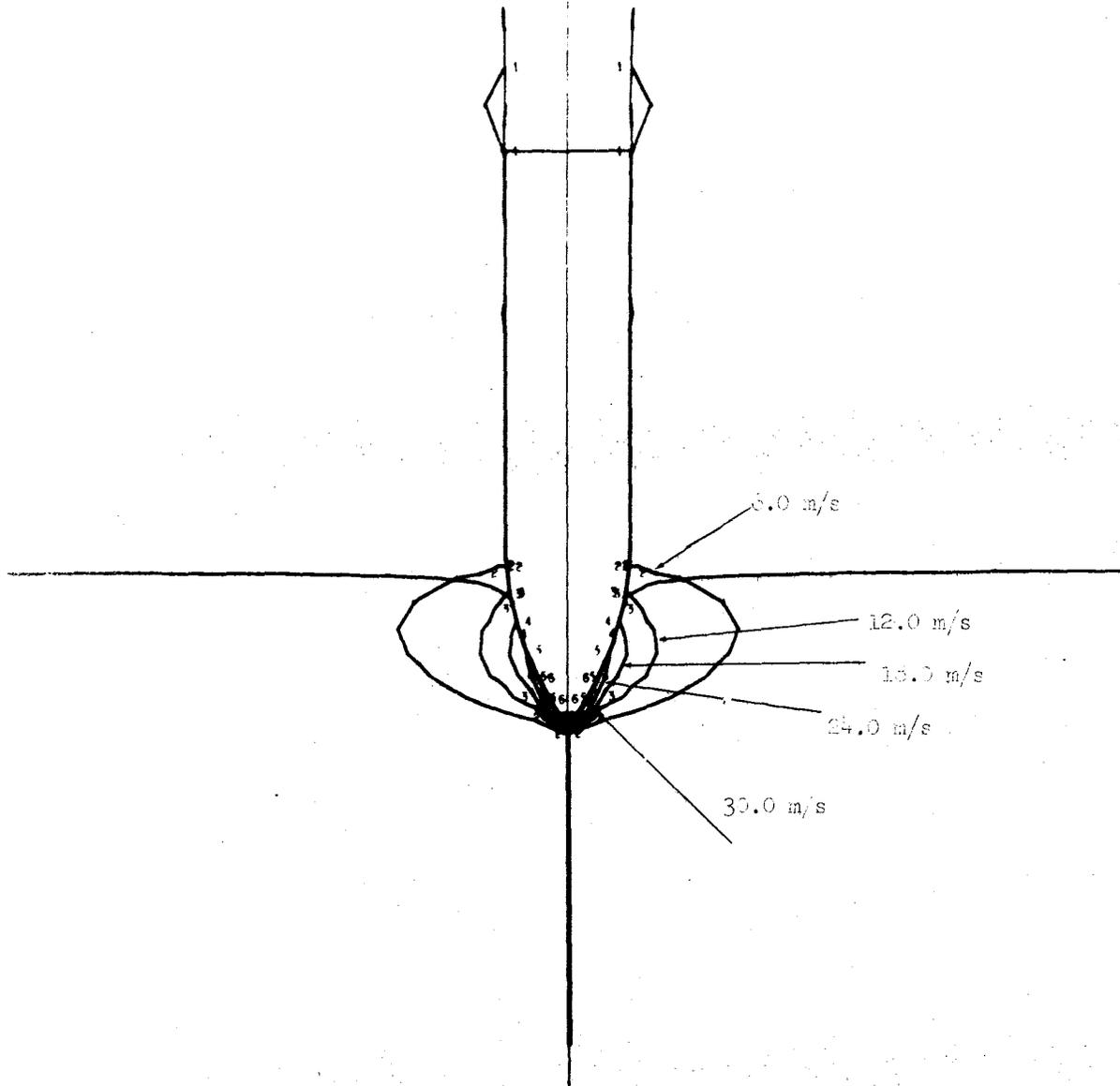


Figure A-114  
Contours of Radial Velocity in Target. Projectile at 2.8 m Depth.

4.4 m  
30.3 msec

LAGRANGIAN COORDINATES  
OF A PARTICLE IN A CAVITY

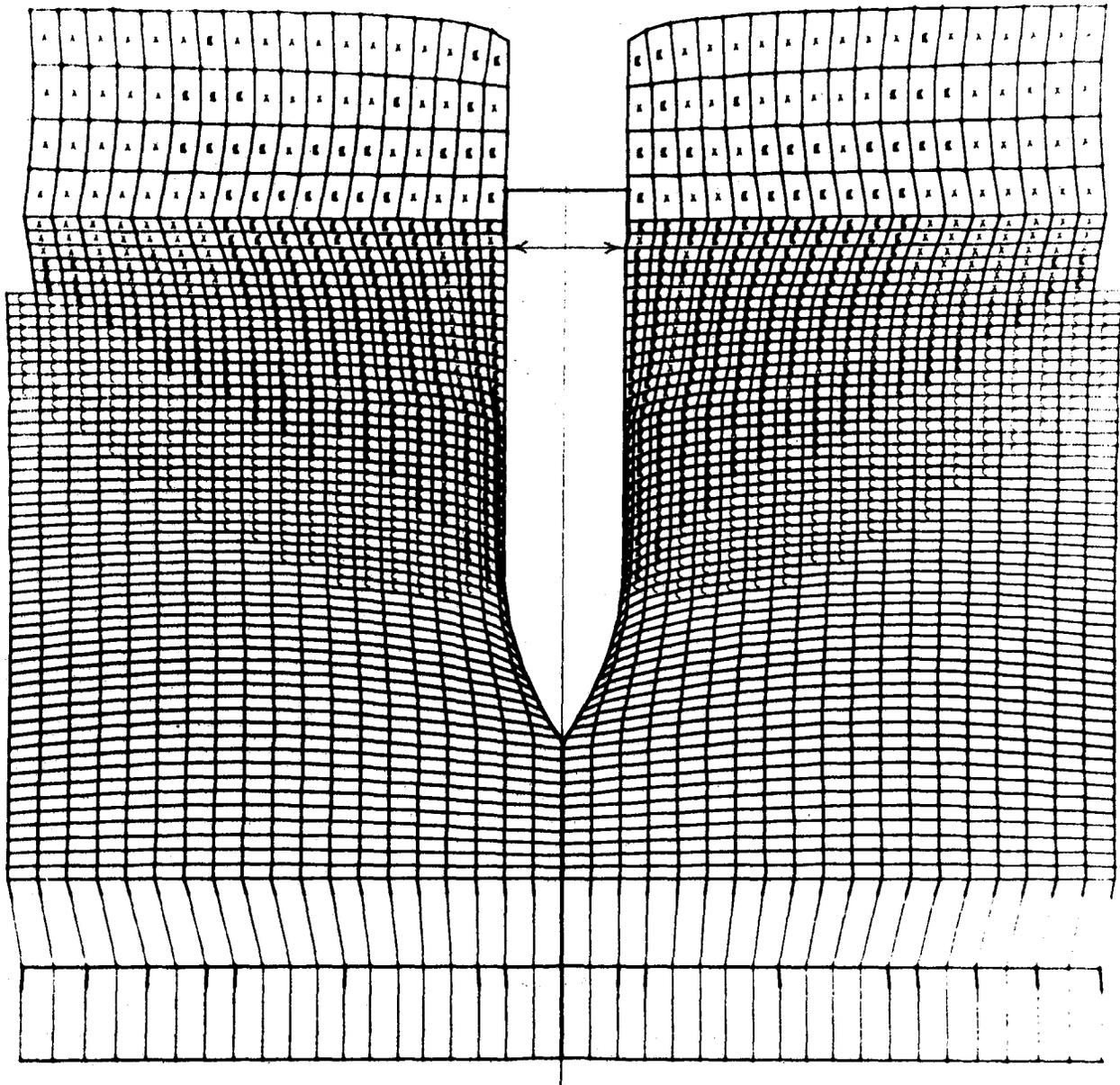


Figure A-115

Lagrangian Coordinates When Projectile has Penetrated to Depth of 4.4 m. Radial Dimensions Doubled for Clarity.

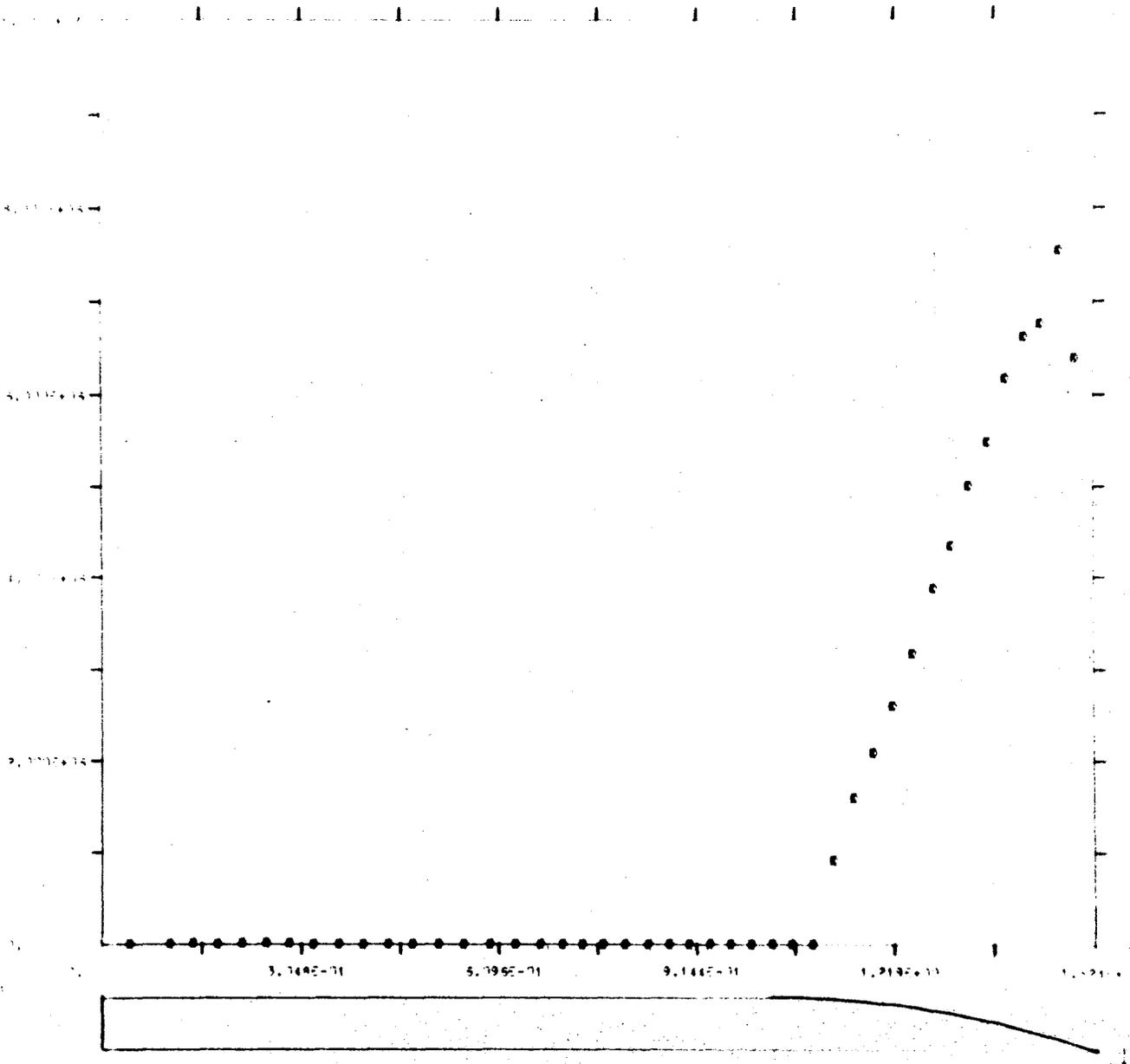
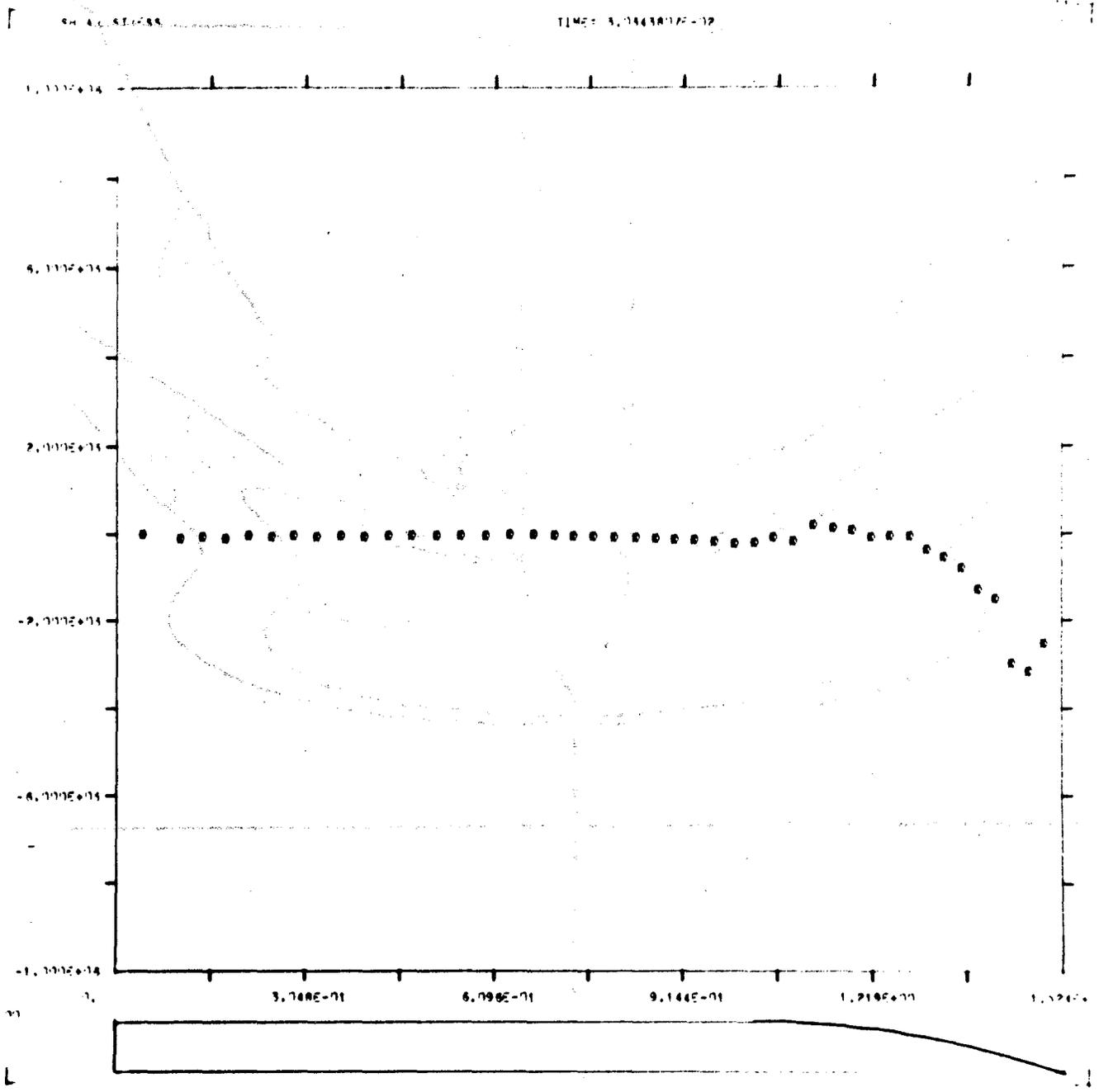


Figure A-116

Normal Stress (Pa) Along Surface of Projectile When Projectile is at 4.4 m Depth.



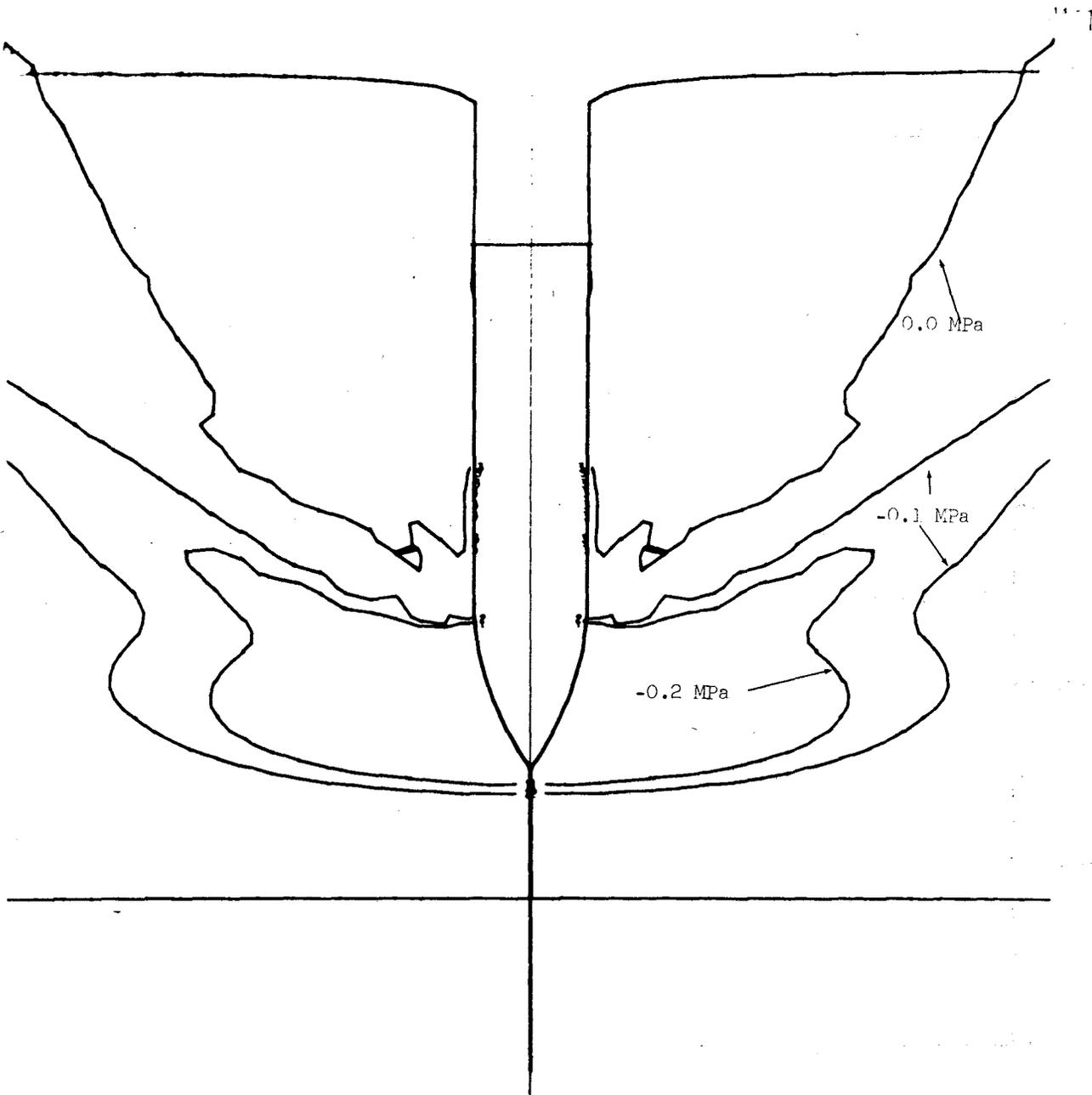


Figure A-118  
Contours of Axial Stress in Target. Projectile at 4.4 m Depth.

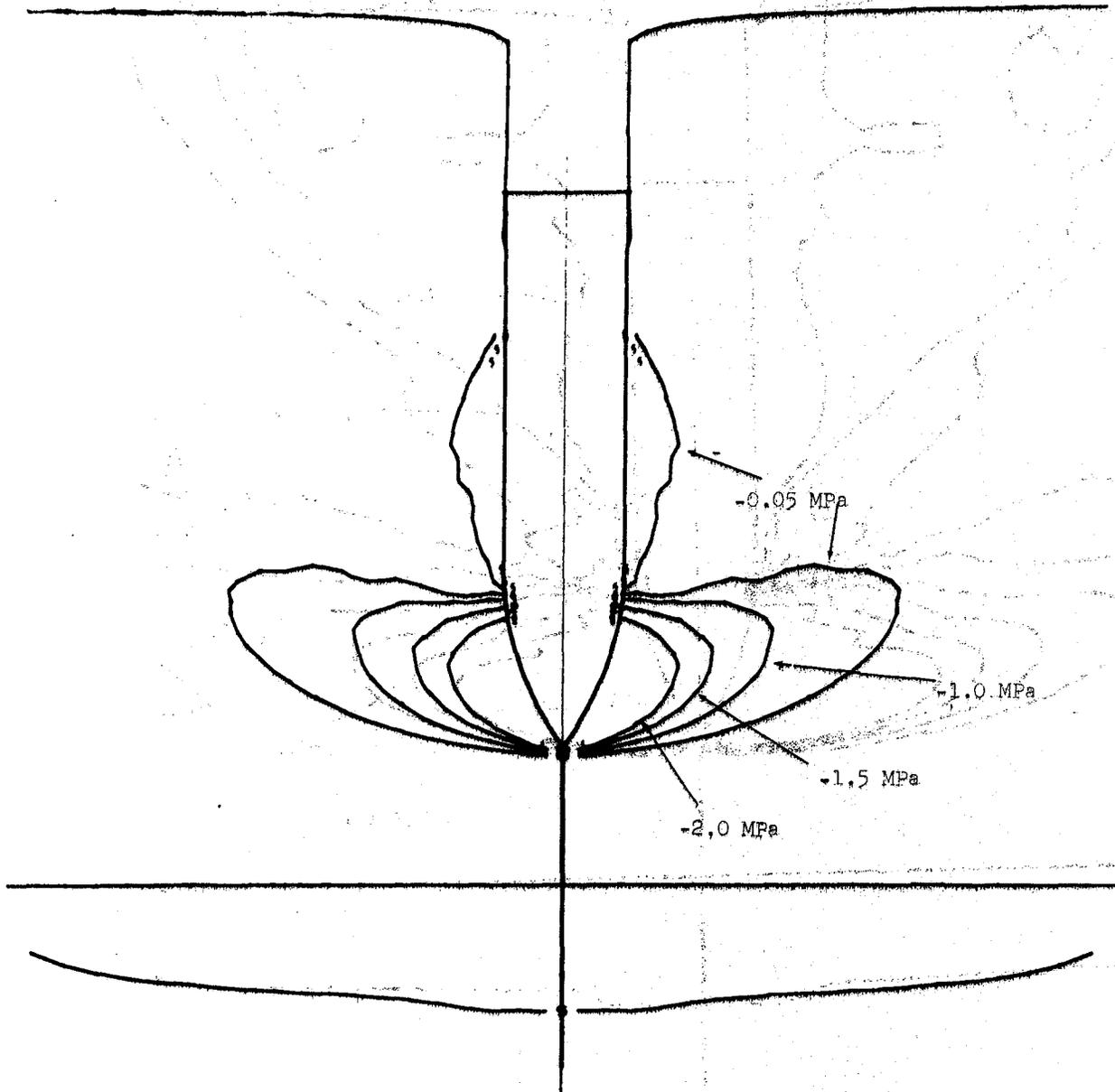


Figure A-119  
Contours of Radial Stress in Target, Projectile at 4.4 m Depth.

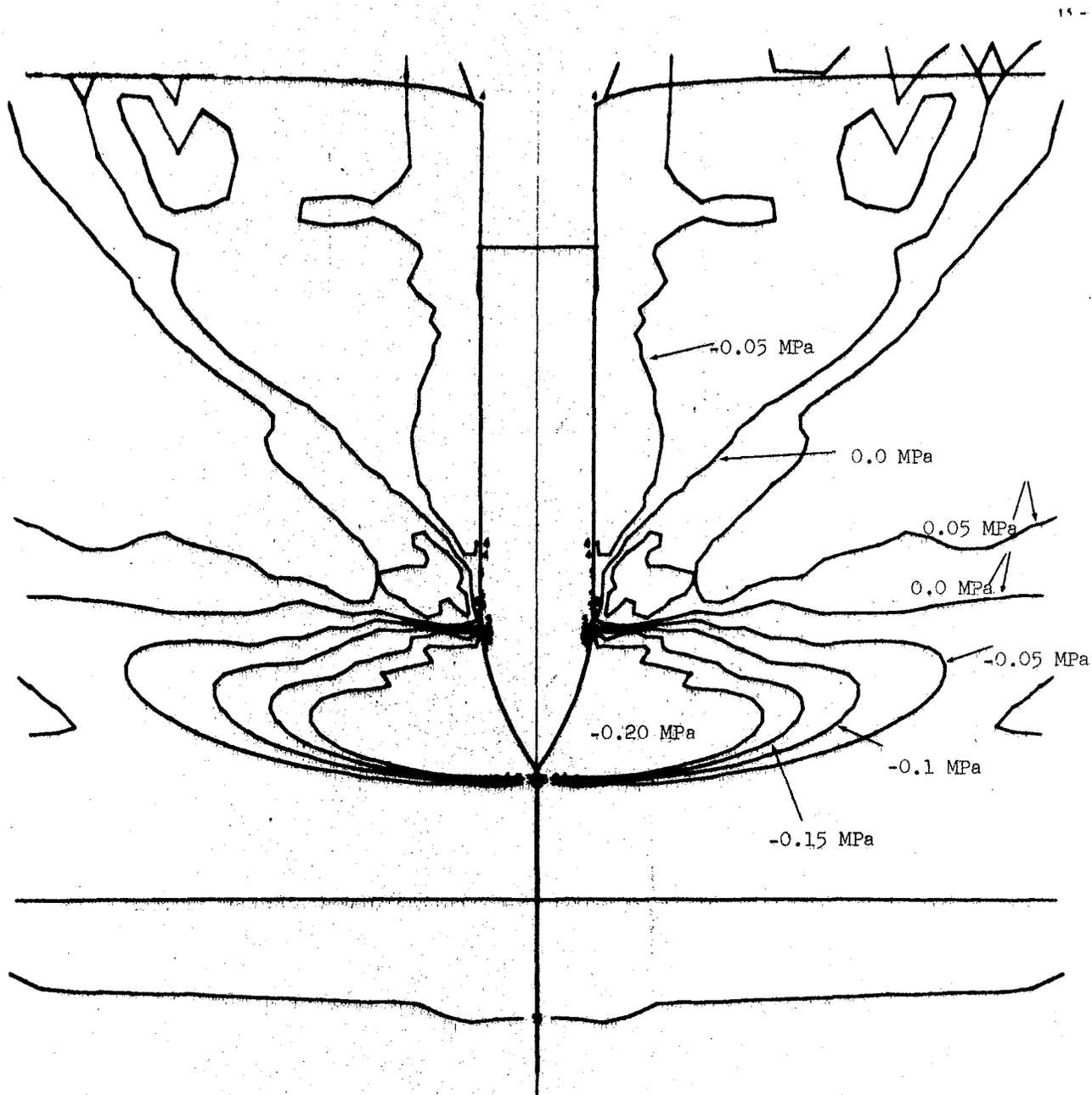


Figure A-120  
Contours of Hoop Stress in Target. Projectile at 4.4 m Depth.

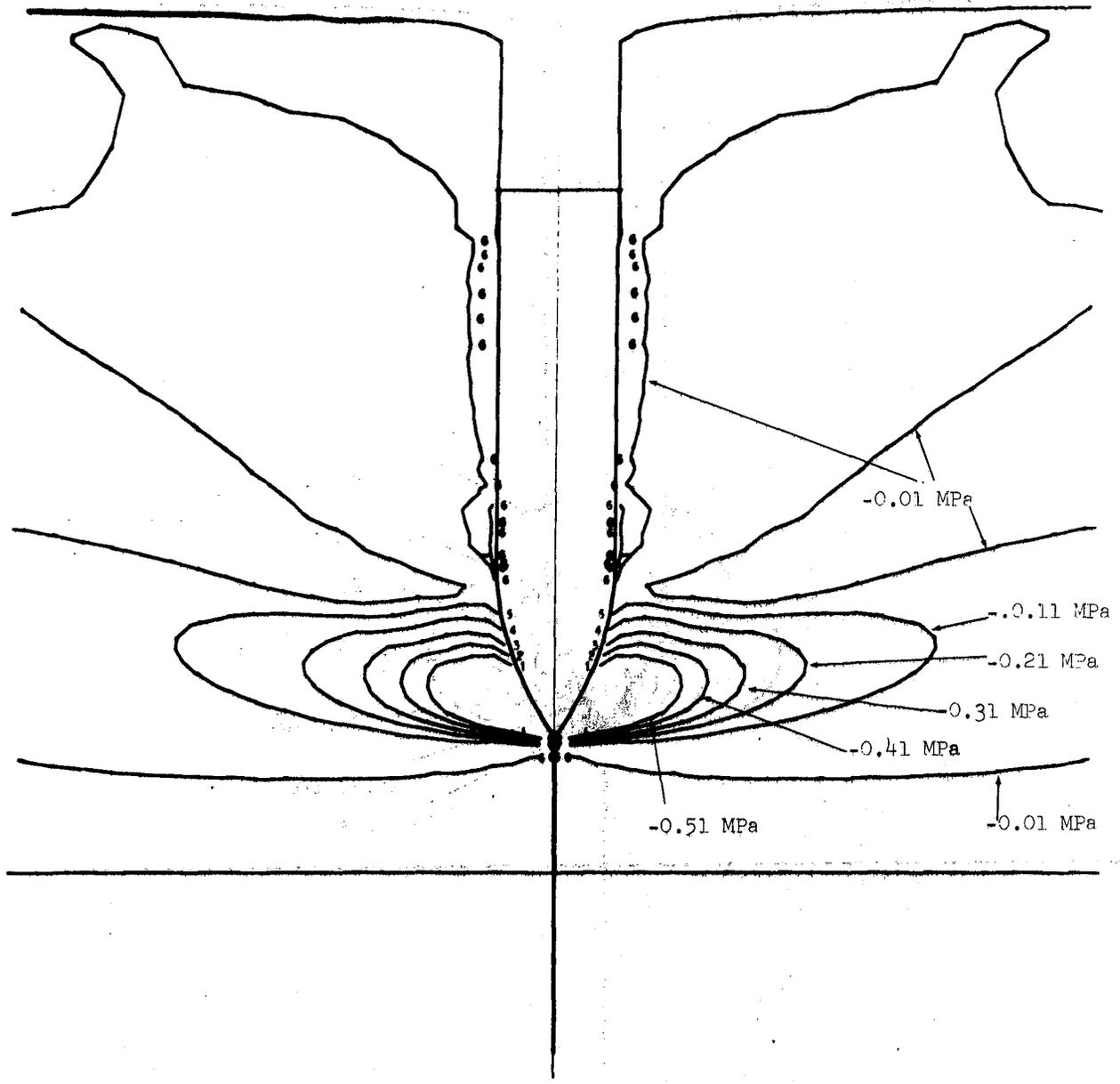


Figure A-121  
 Contours of Radial-Vertical Shear Stress in Target. Projectile at 4.4 m Depth.

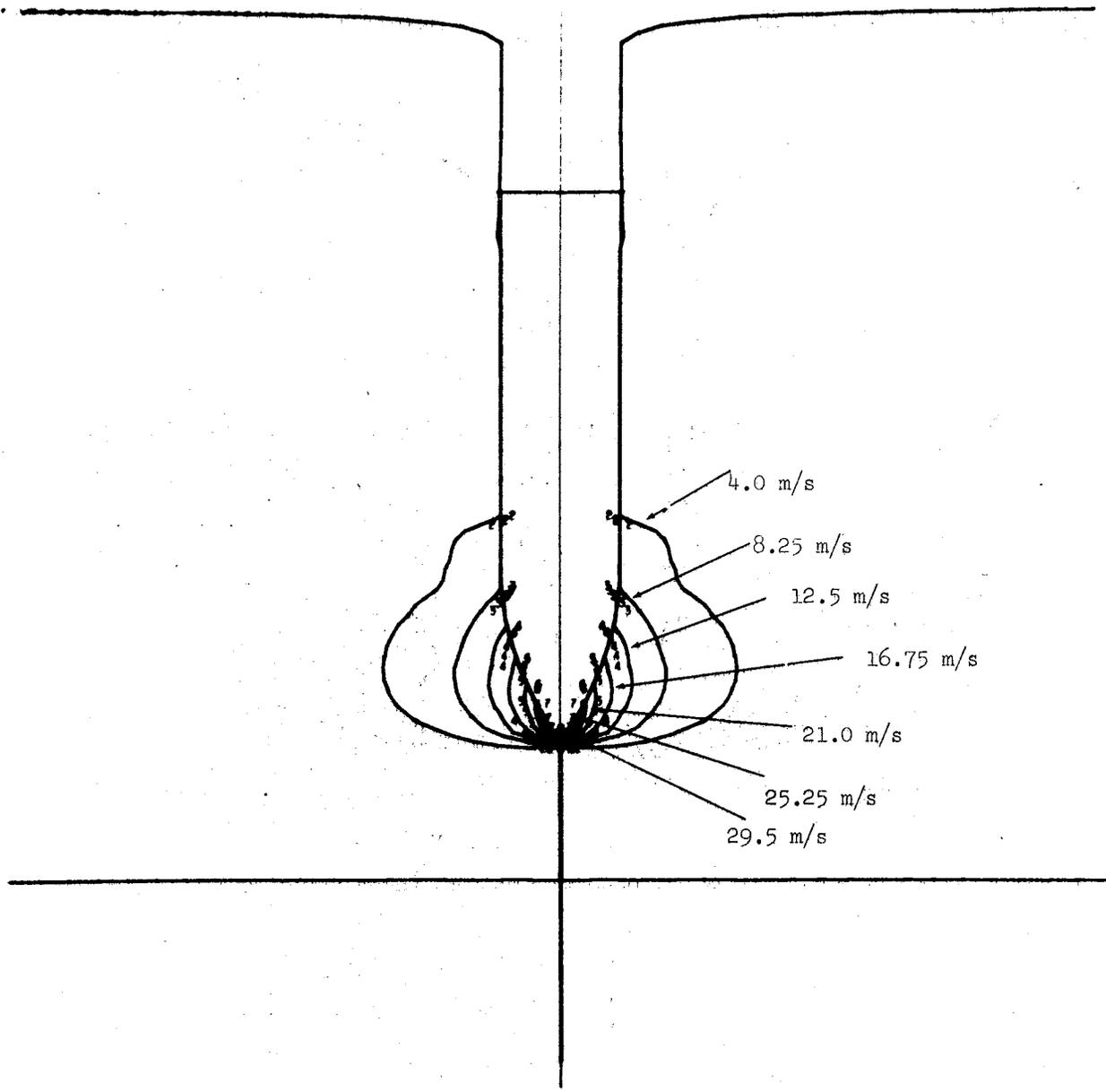


Figure A-122  
Contours of Vertical Velocity in Target. Projectile at 4.4 m Depth.

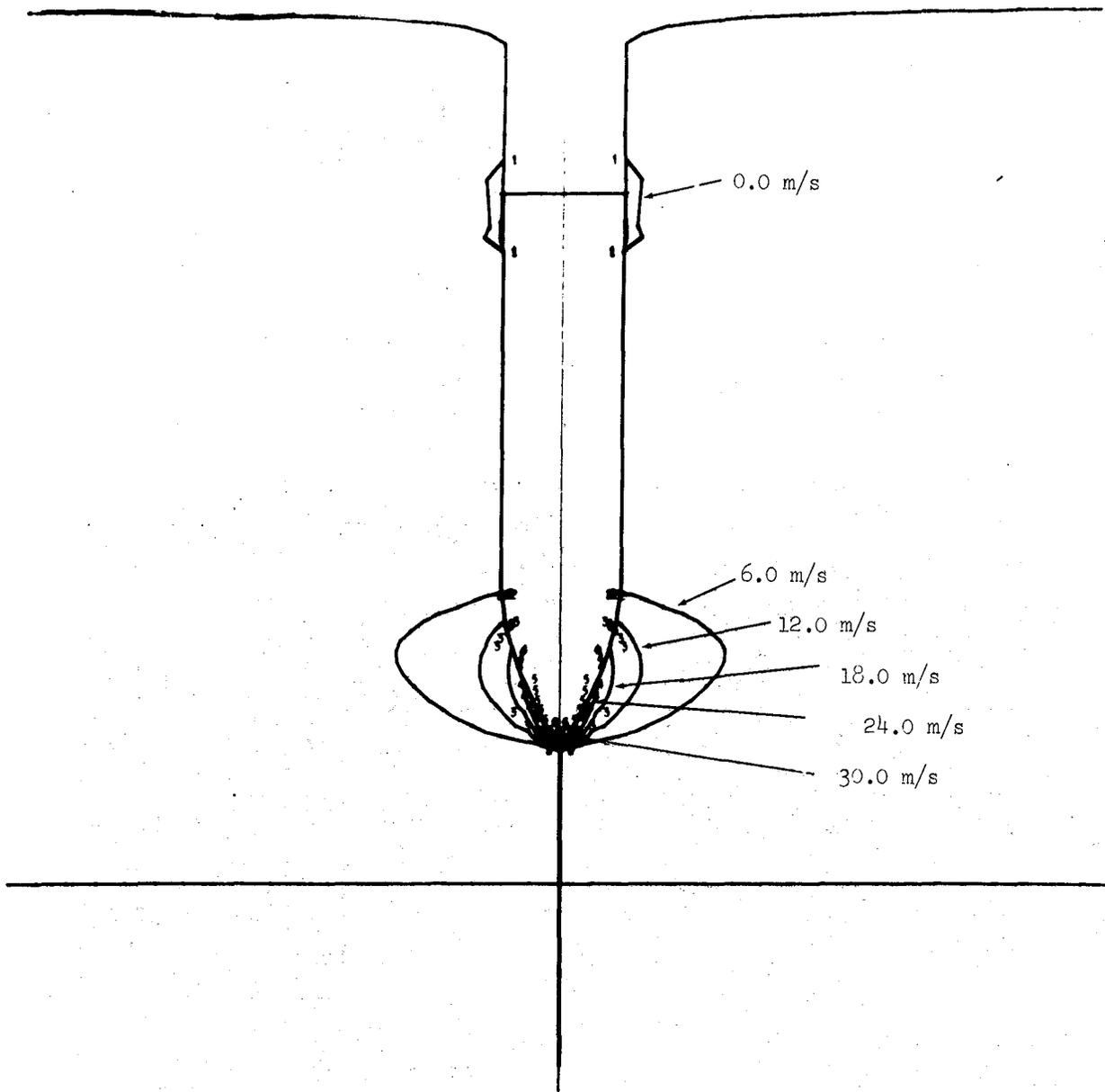


Figure A-123

Contours of Radial Velocity in Target. Projectile at 4.4 m Depth.



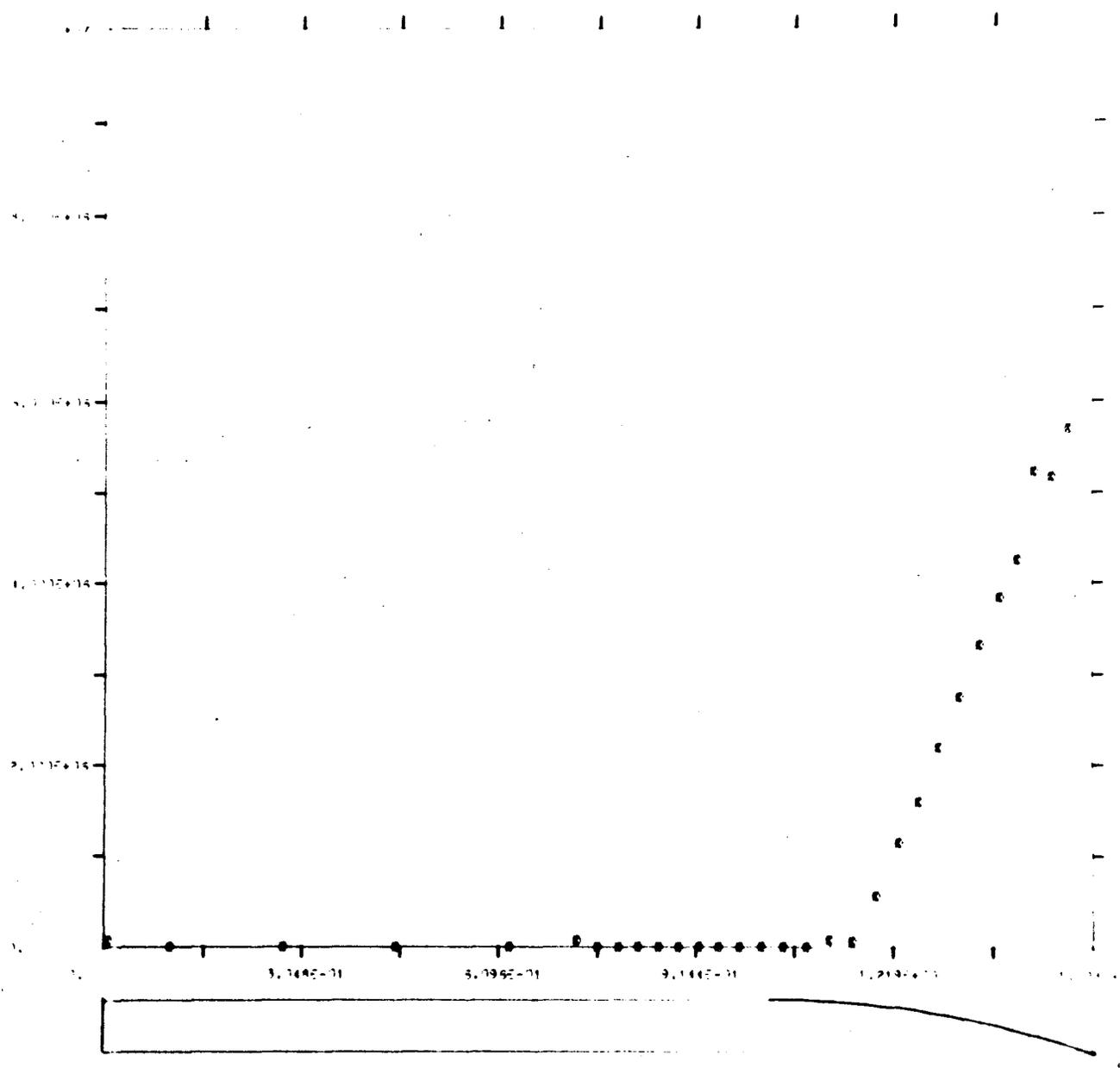


Figure A-125  
Normal Stress (Pa) Along Surface of Projectile When Projectile is at 5.2 m Depth.

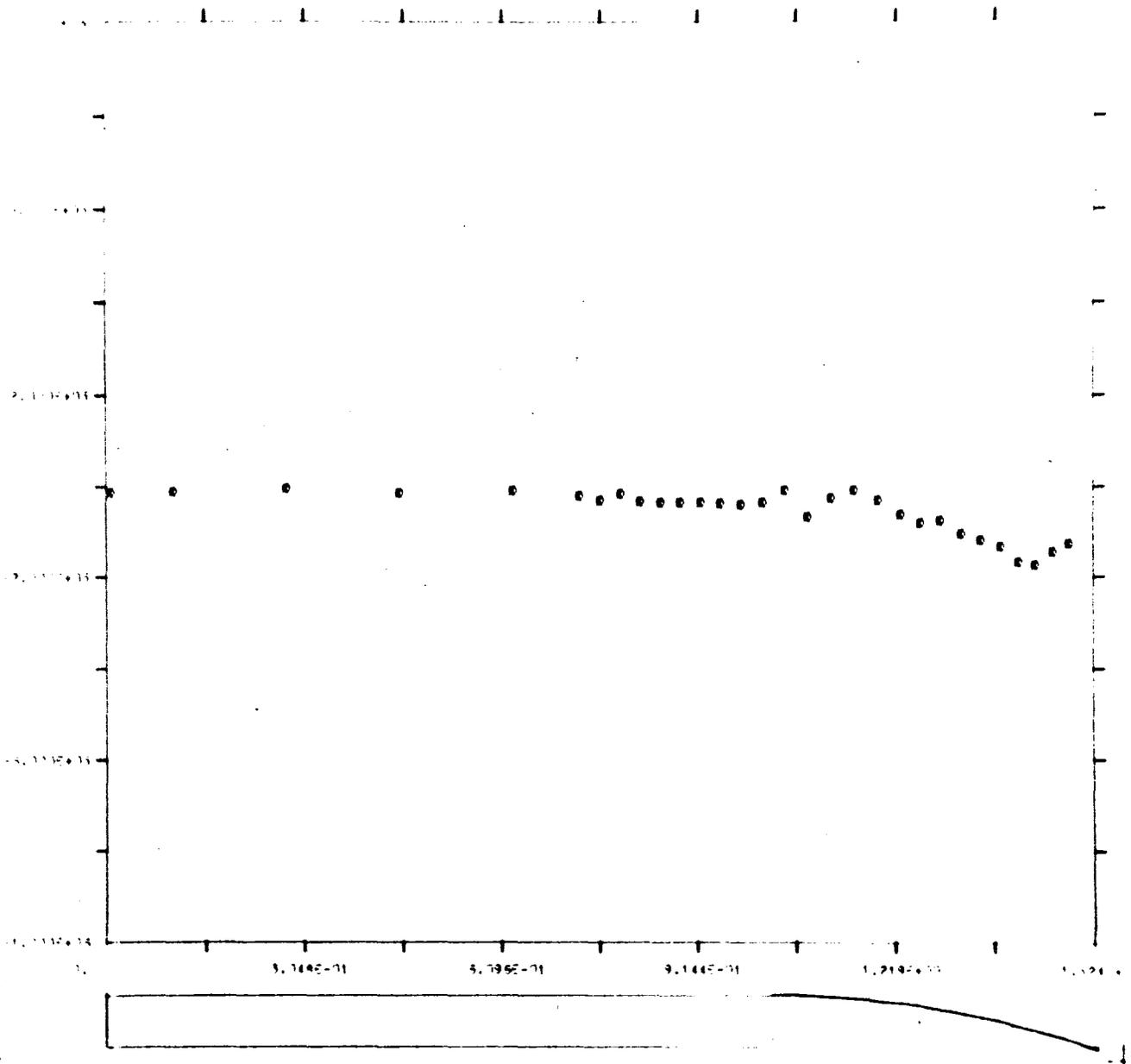


Figure A-126

Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 5.2 m Depth.

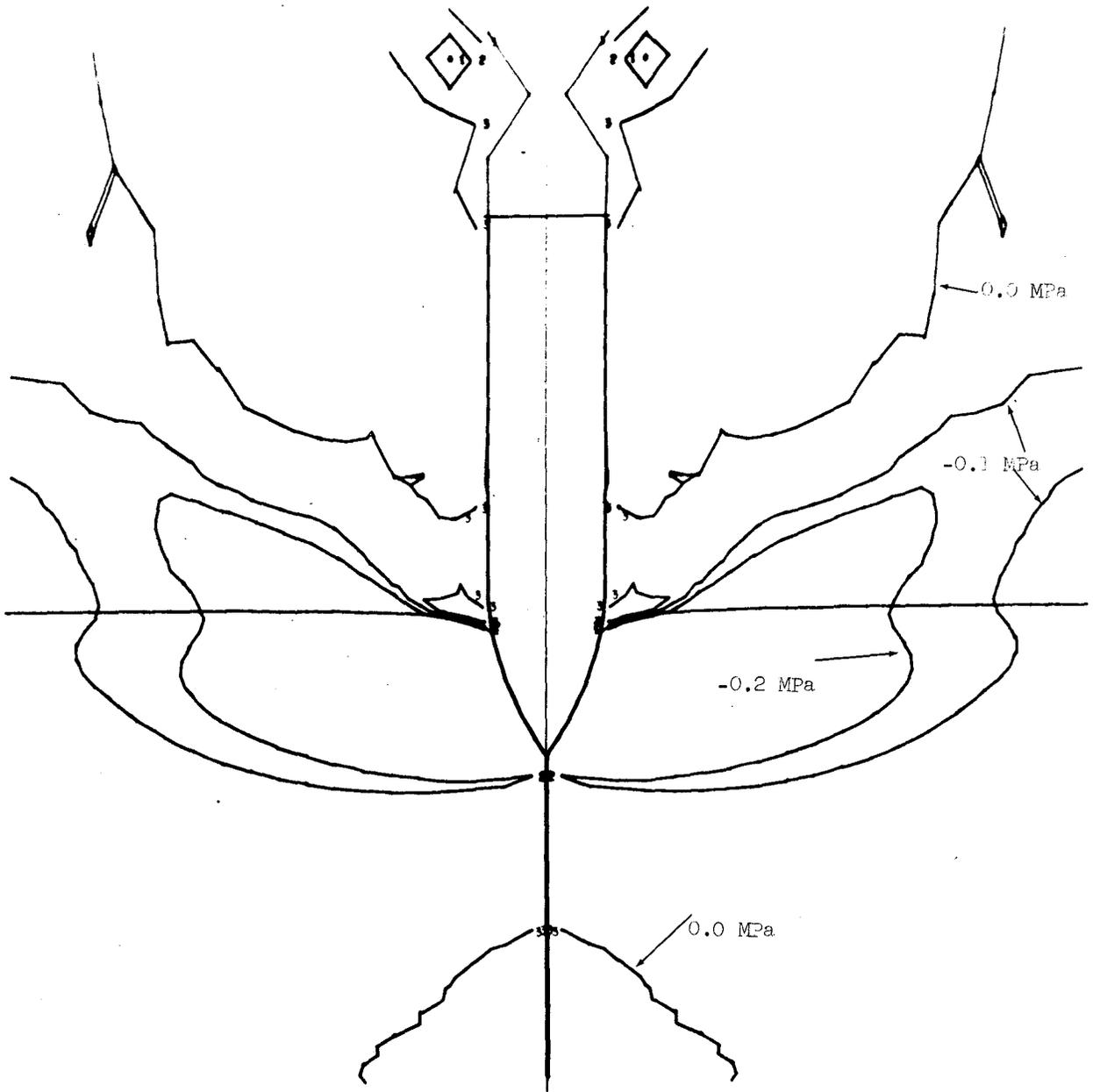


Figure A-127  
Contours of Axial Stress in Target. Projectile at 5.2 m Depth.

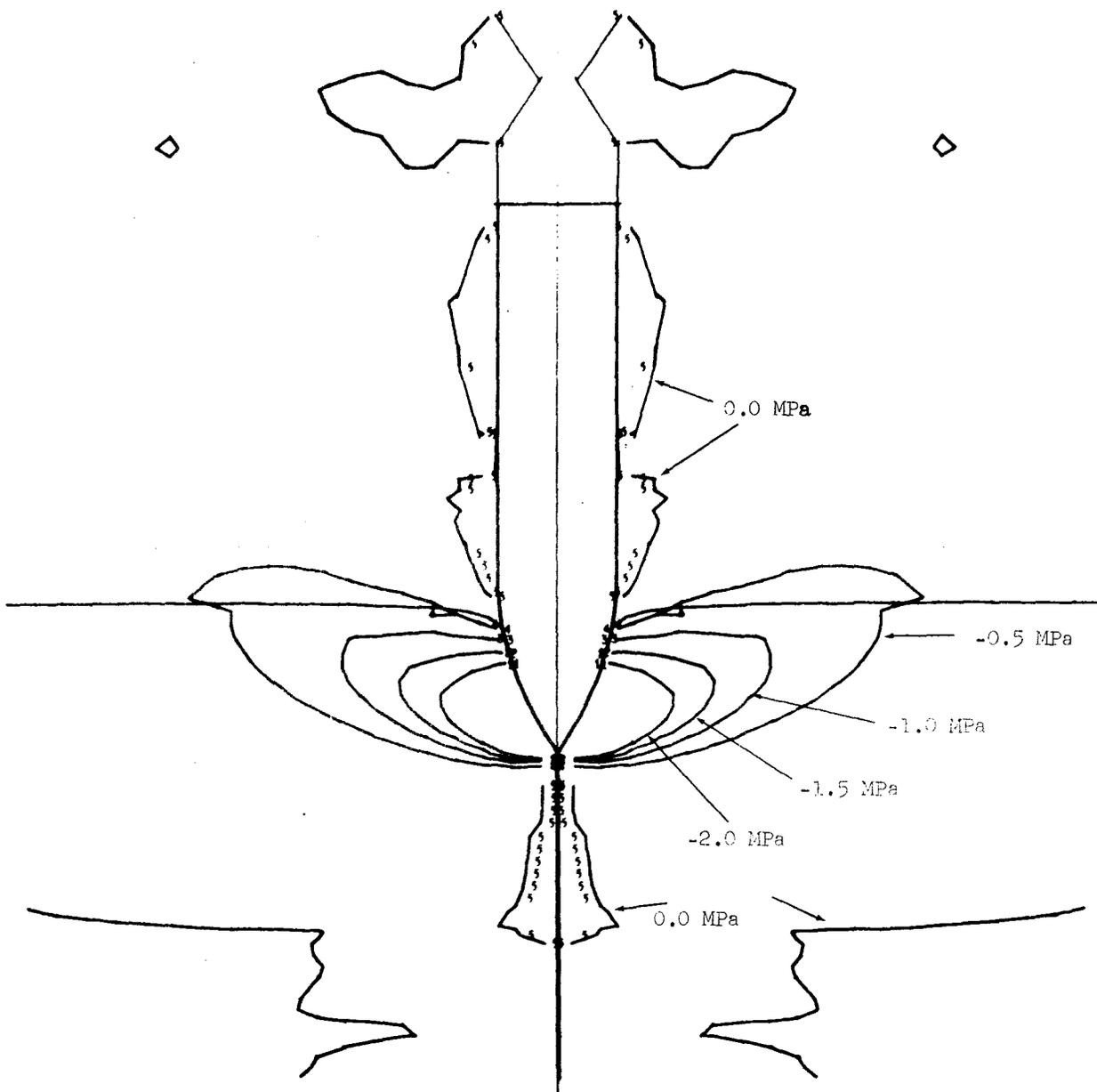


Figure A-128  
Contours of Radial Stress in Target. Projectile at 5.2 m Depth.

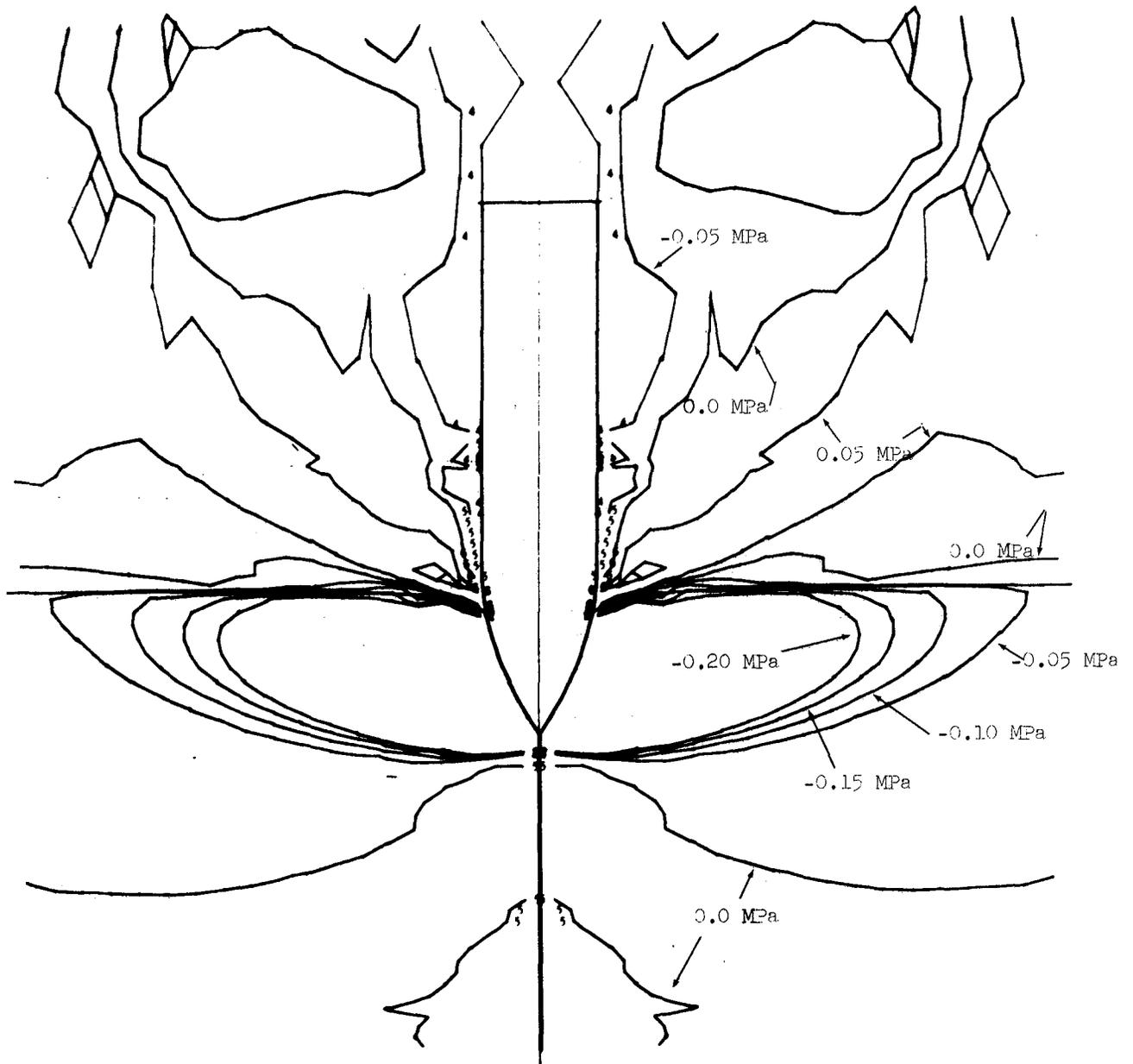


Figure A-129  
Contours of Hoop Stress in Target. Projectile at 5.2 m Depth.

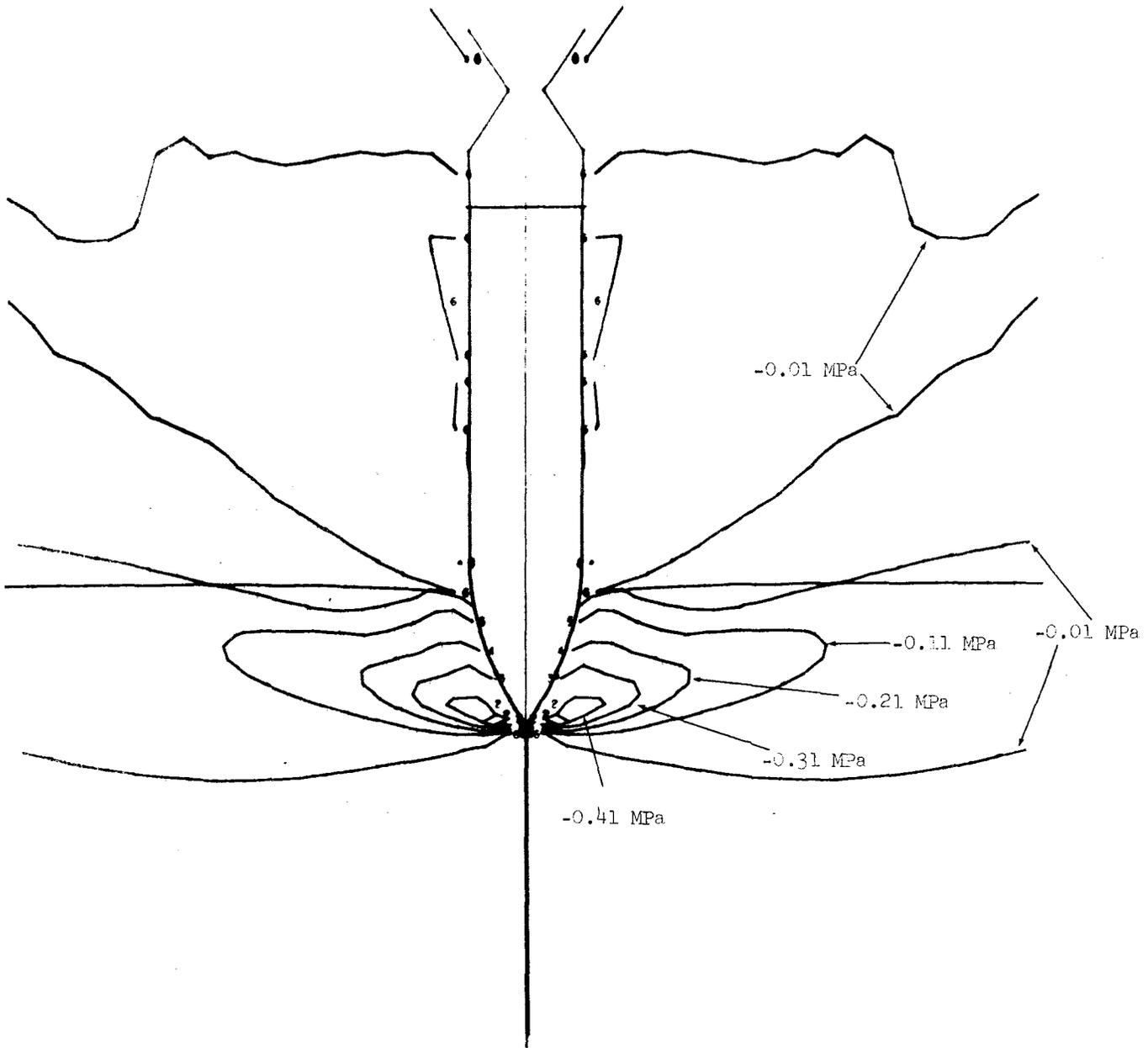


Figure A-130  
 Contours of Radial-Vertical Shear Stress in Target. Projectile at 5.2 m Depth.

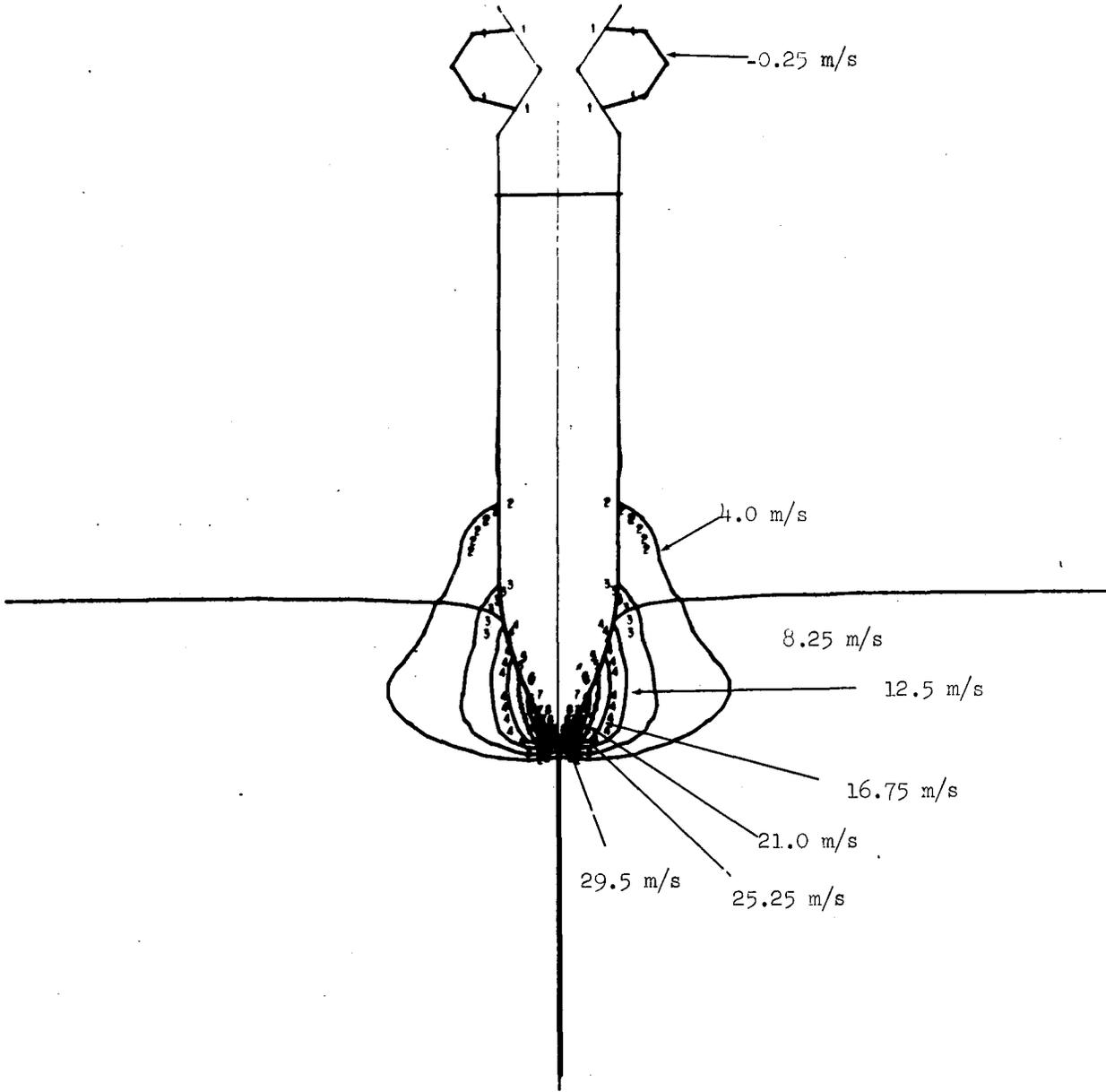


Figure A-131  
 Contours of Vertical Velocity in Target. Projectile at 5.2 m Depth.

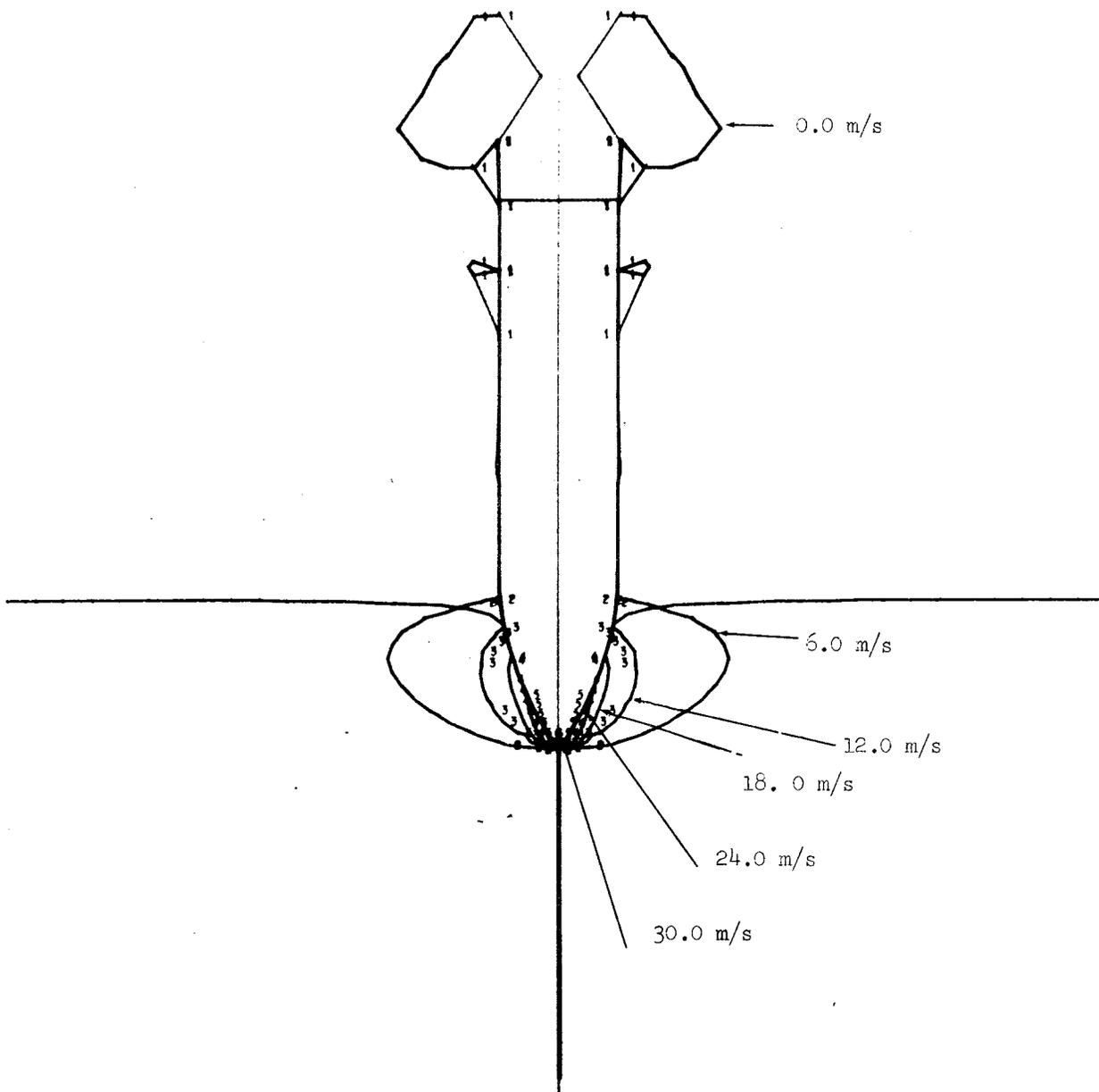


Figure A-132  
 Contours of Radial Velocity in Target. Projectile at 5.2 m Depth.

6.8 m  
48.4 msec

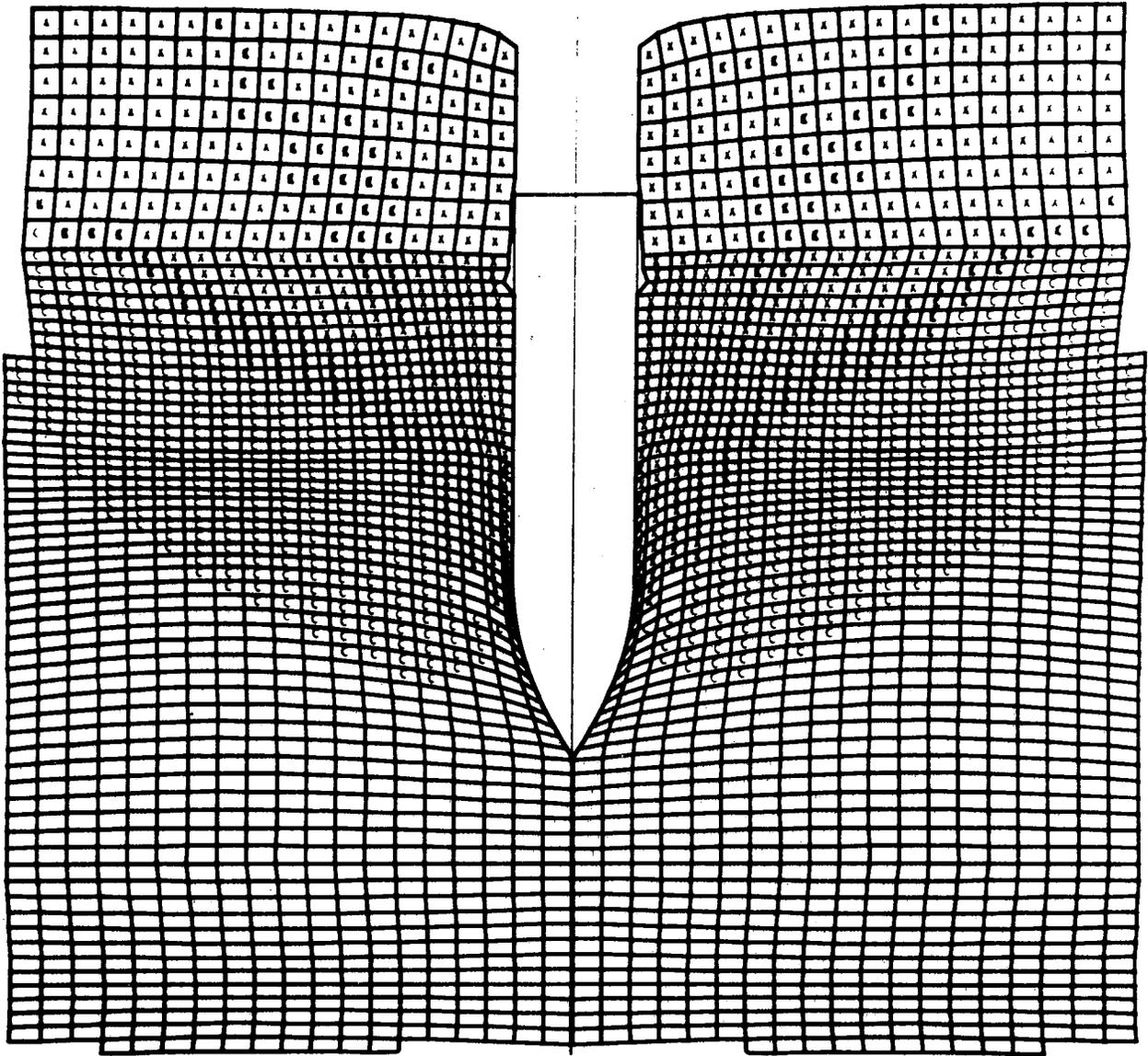


Figure A-133  
Lagrangian Coordinates When Projectile has Penetrated to Depth of 6.8 m. Radial  
Dimensions Doubled for Clarity.

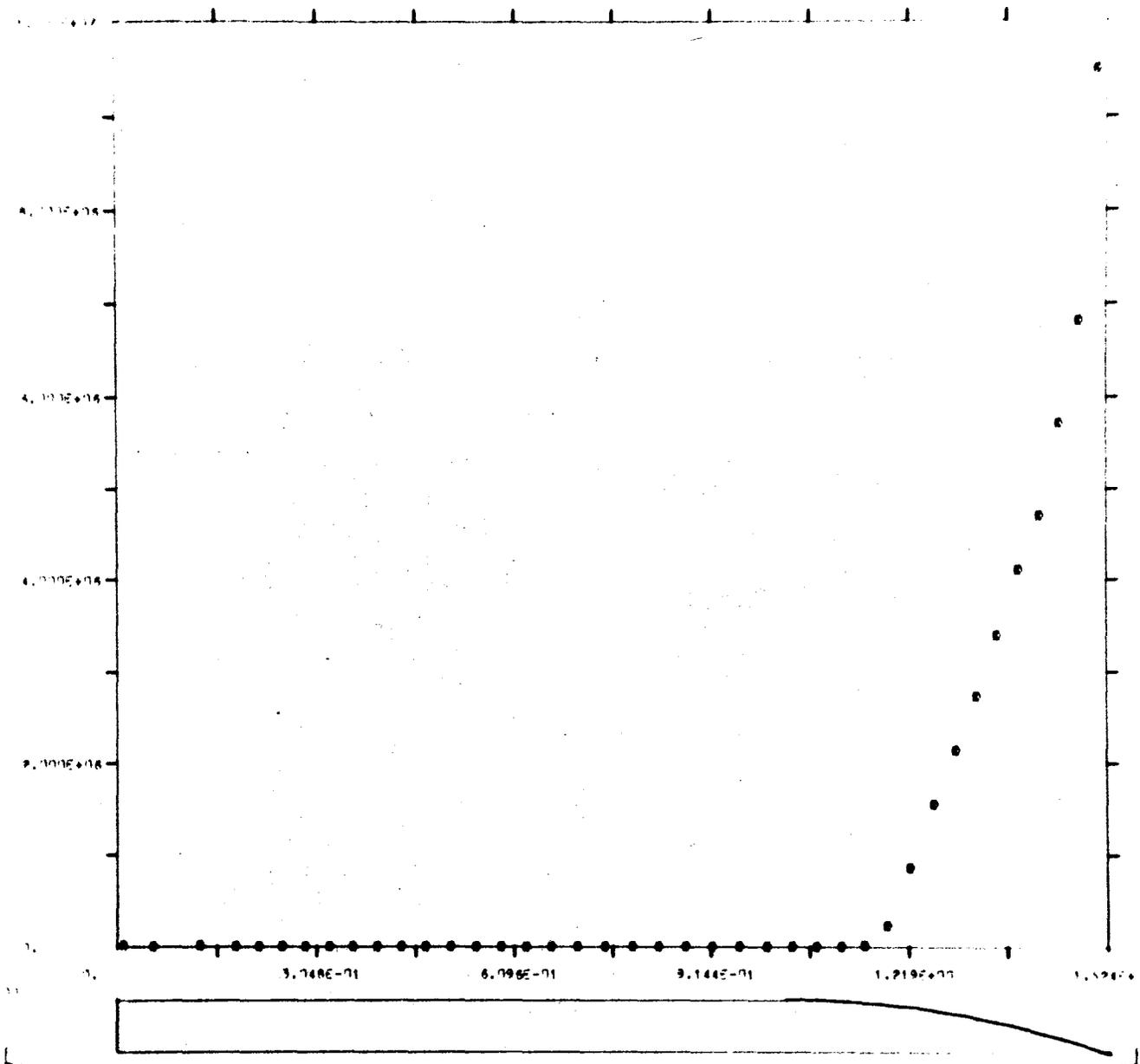


Figure A-134

Normal Stress (Pa) Along Surface of Projectile When Projectile is at 6.8 m Depth.

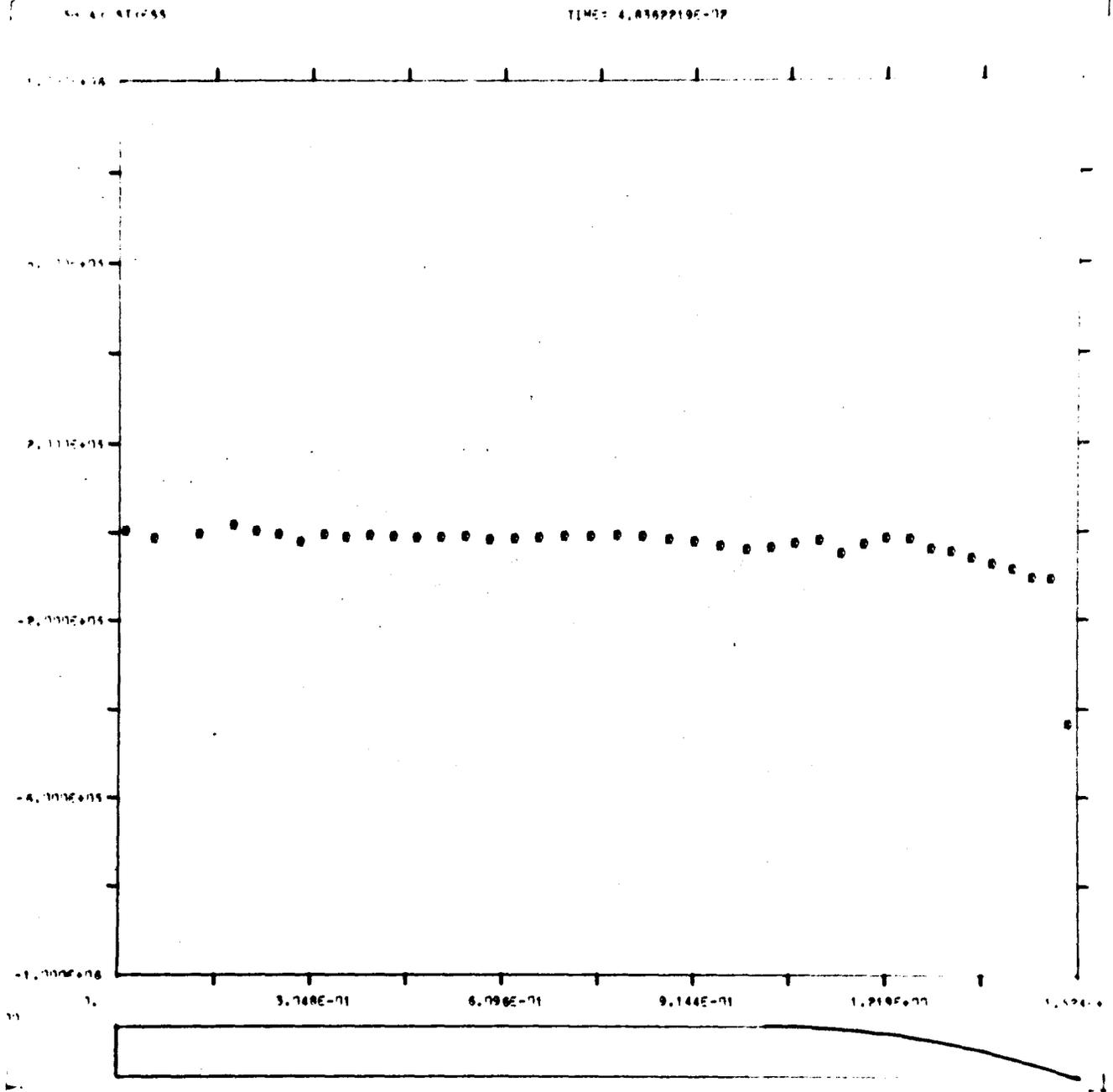


Figure A-135  
 Tangential Stress (Pa) Along Surface of Projectile When Projectile is at 6.8 m Depth.

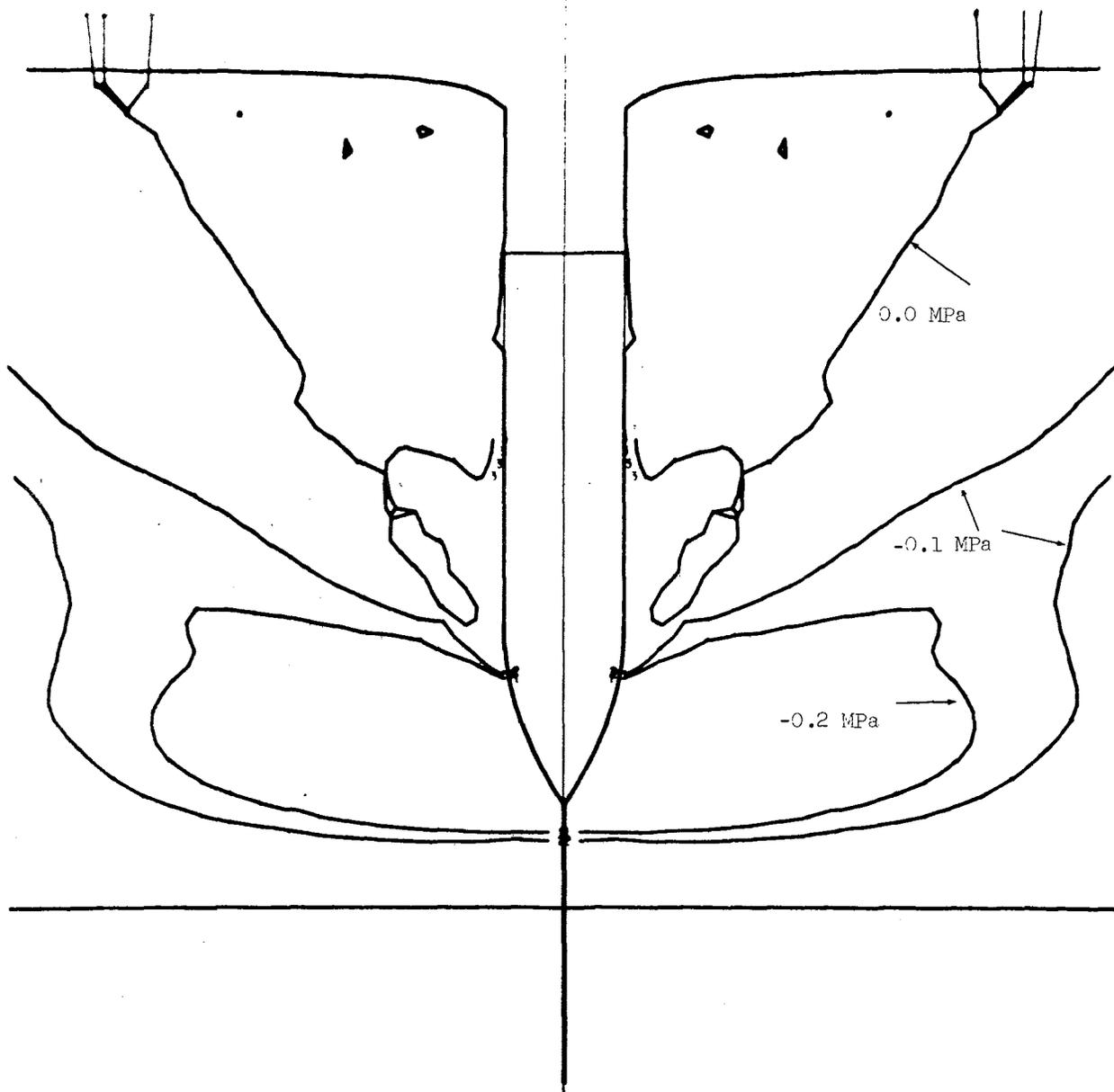


Figure A-136  
Contours of Axial Stress in Target. Projectile at 6.8 m Depth.

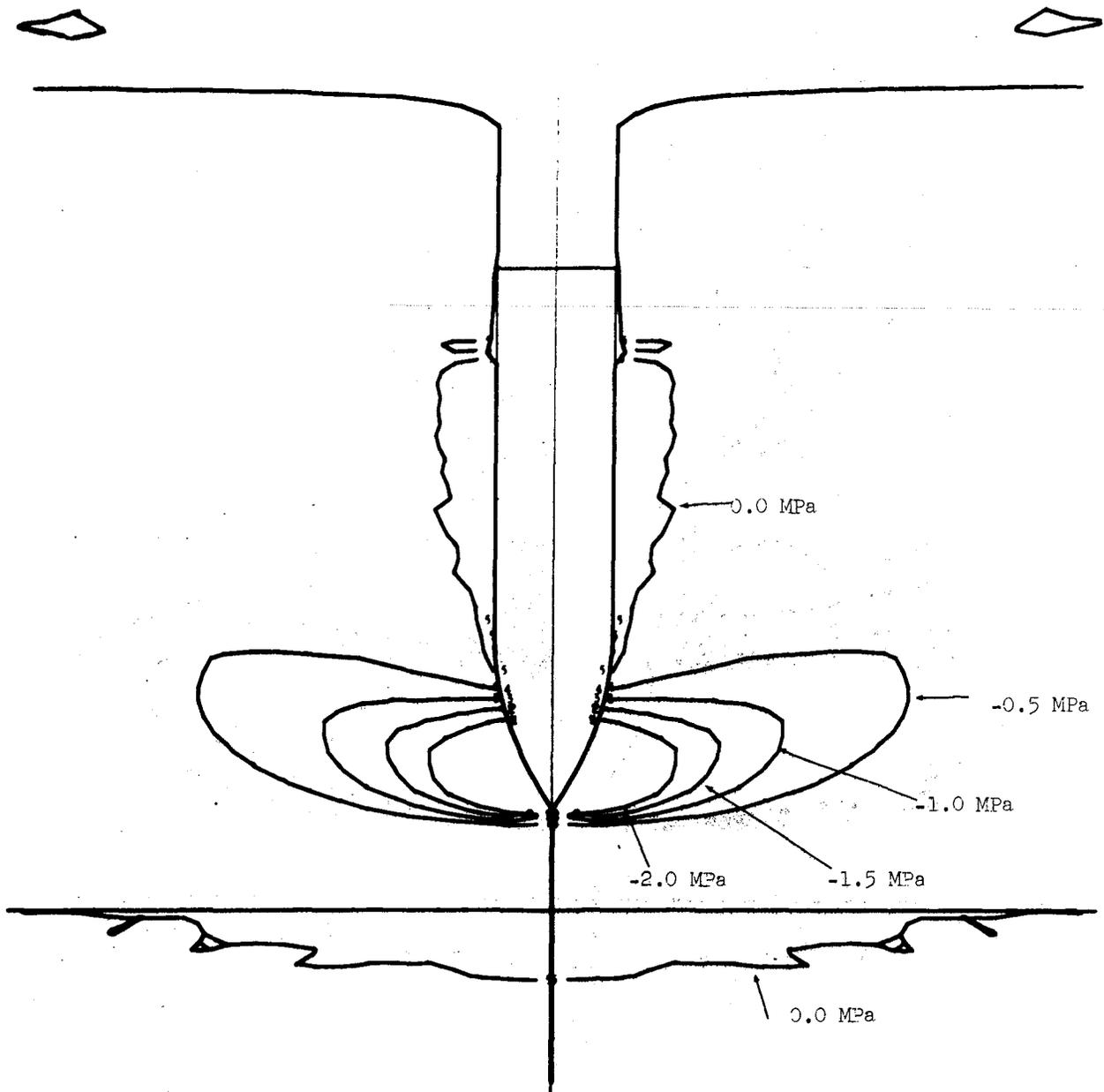


Figure A-137  
Contours of Radial Stress in Target. Projectile at 6.8 m Depth.

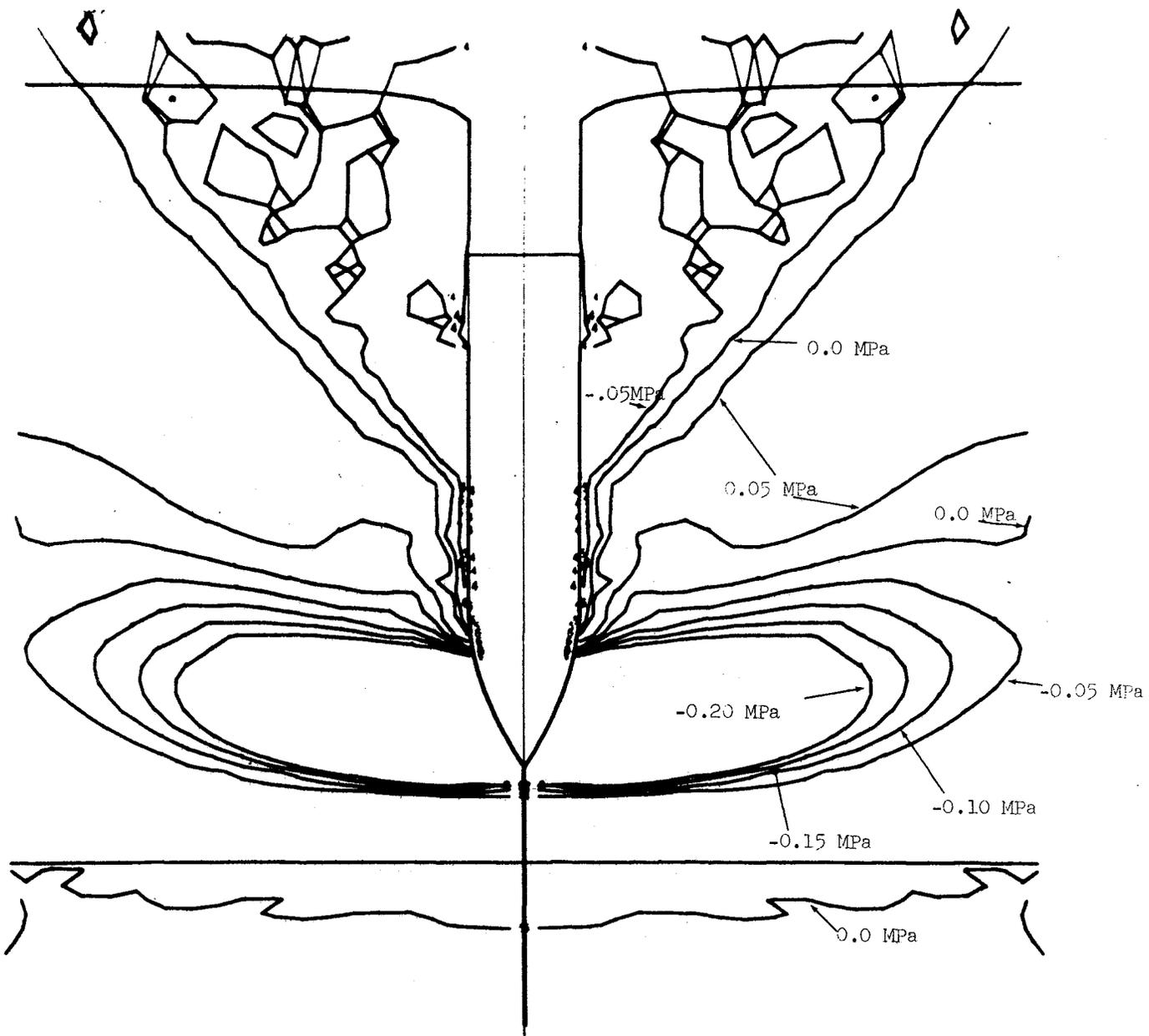


Figure A-138  
Contours of Hoop Stress in Target. Projectile at 6.8 m Depth.

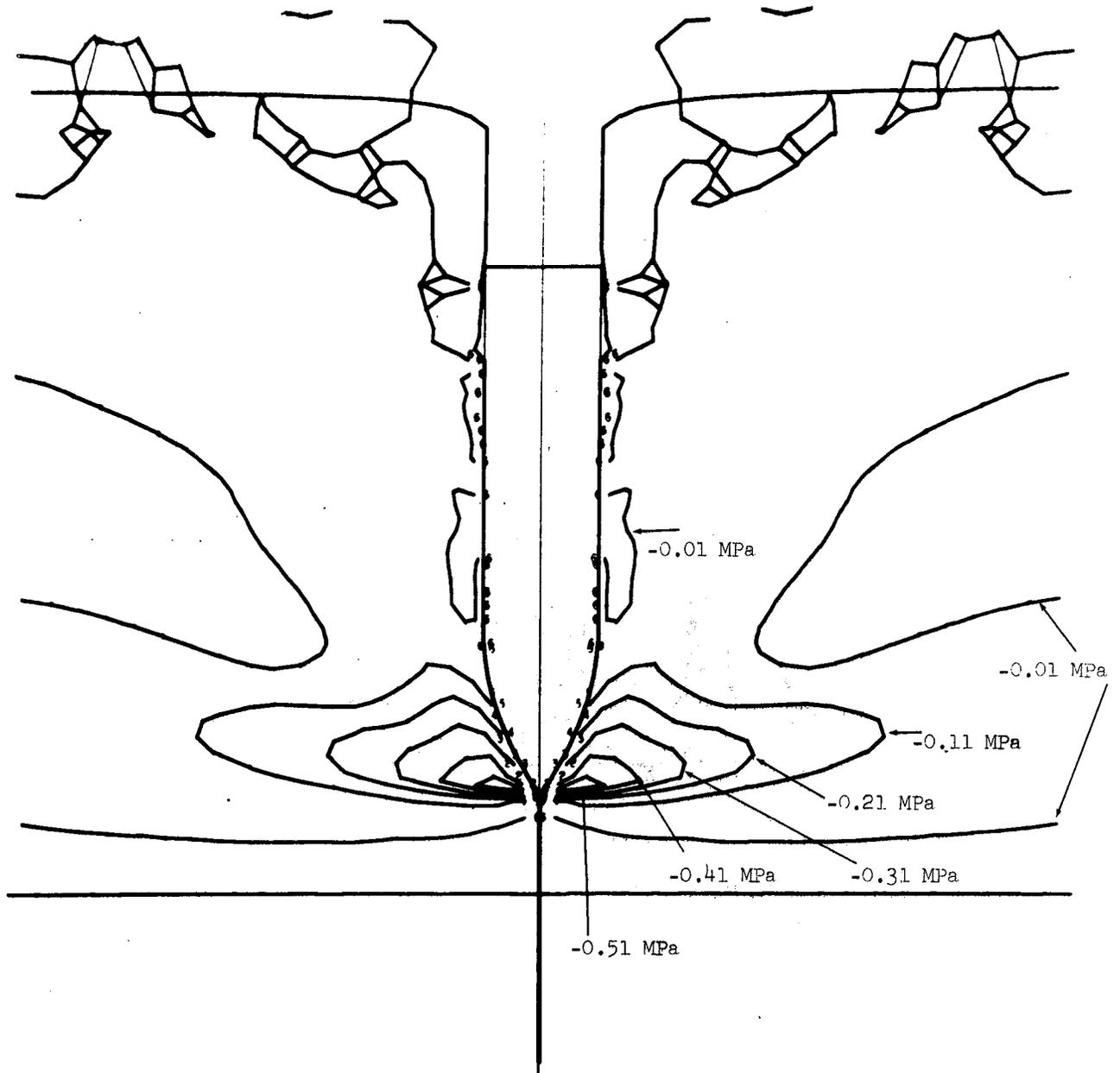


Figure A-139  
 Contours of Radial-Vertical Shear Stress in Target. Projectile at 6.8 m Depth.

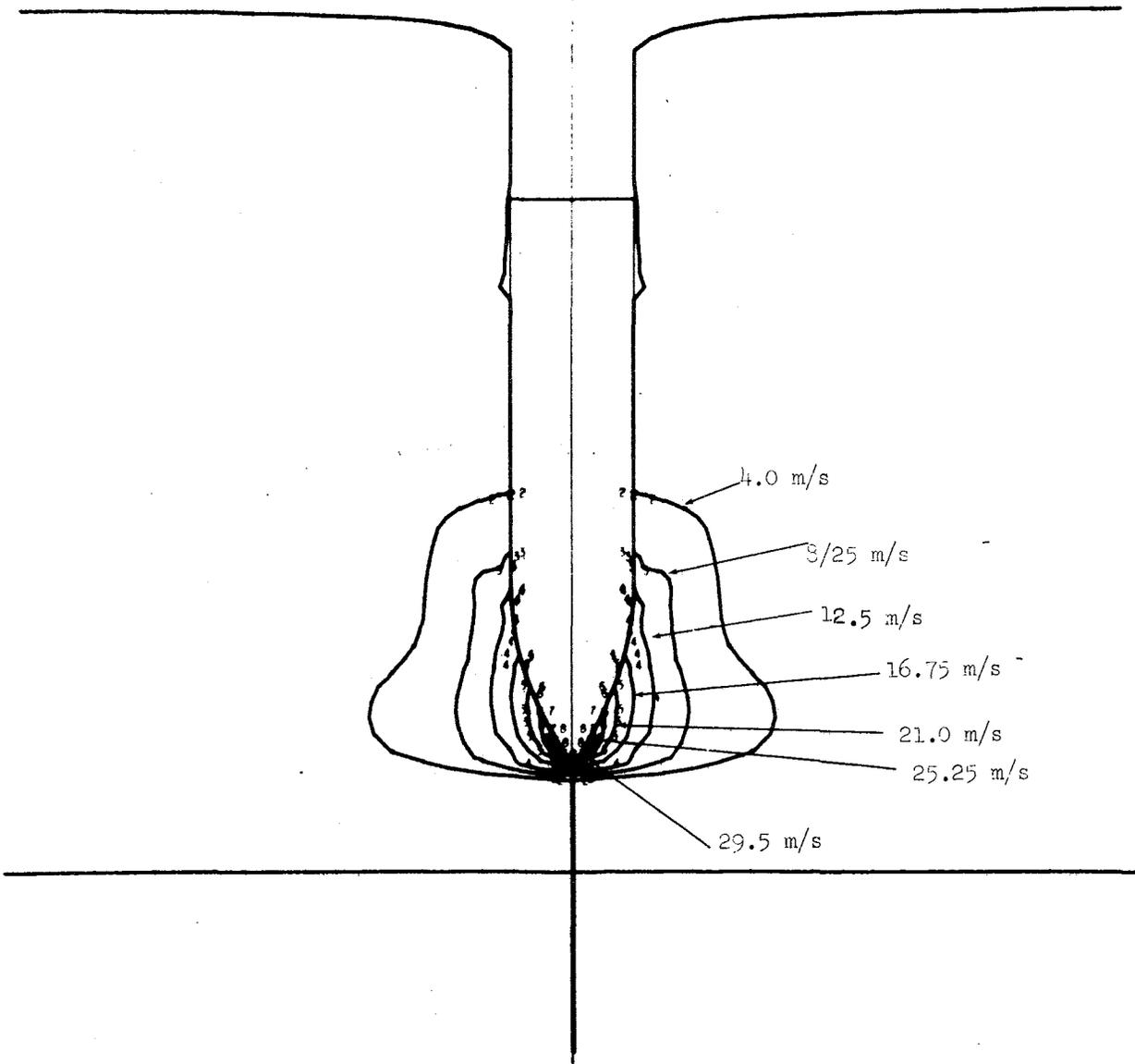


Figure A-140  
 Contours of Vertical Velocity in Target. Projectile at 6.8 m Depth.

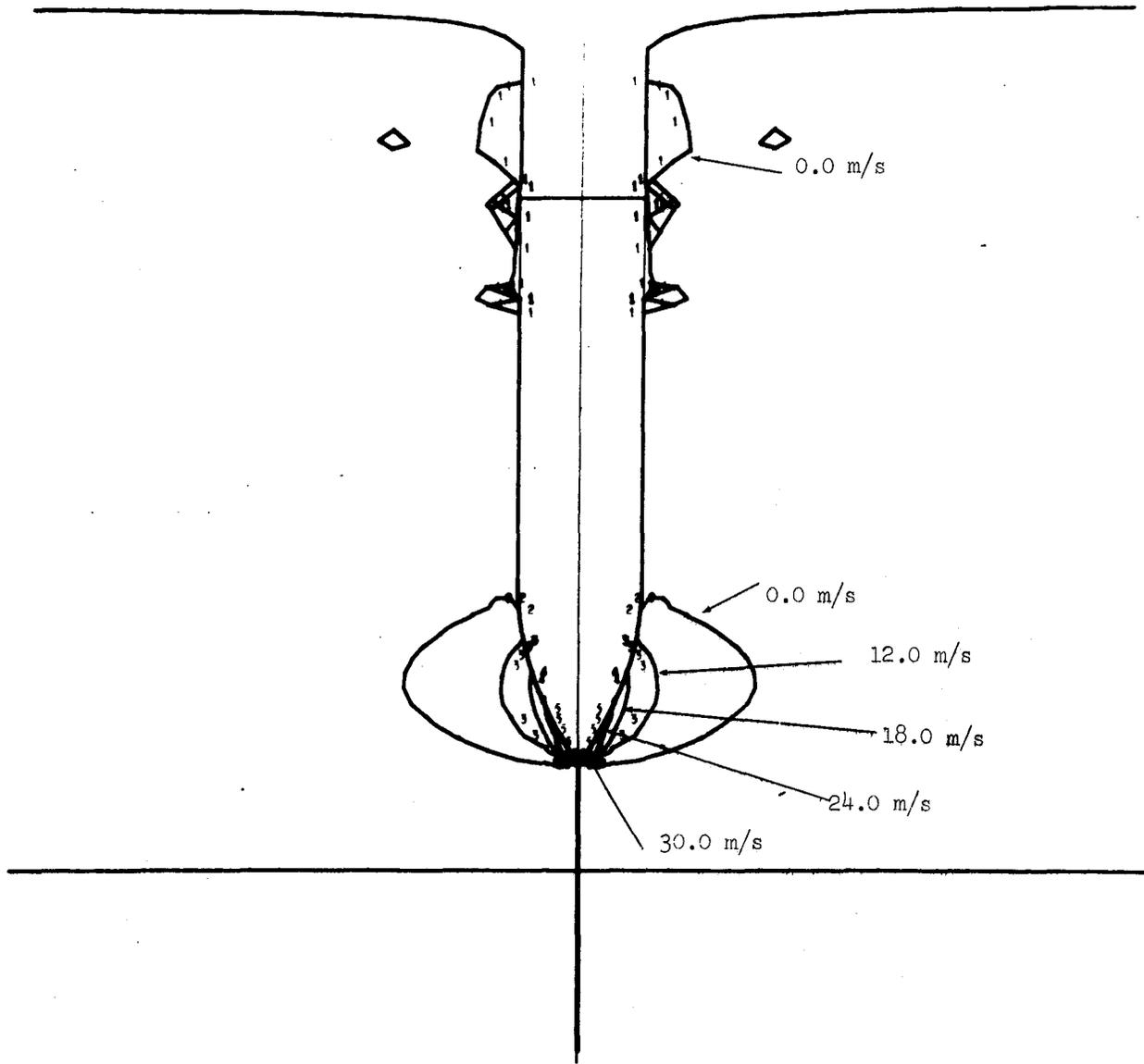


Figure A-141  
Contours of Radial Velocity in Target. Projectile at 6.8 m Depth.

APPENDIX B

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- B-67. Radial Displacement History (m) in Soil at Range 0.14 m, Depth 0.2 m (Deformable Penetrator).
- B-68. Vertical Displacement History (m) in Soil at Range 0.14 m, Depth 0.2 m (Deformable Penetrator).
- B-69. Pressure History (Pa) in Soil at Range 0.14 m, Depth 0.2 m (Deformable Penetrator).
- B-70. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.14 m, Depth 0.2 m (Deformable Penetrator).

- B-71. Radial Velocity History (m/s) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-72. Vertical Velocity History (m/s) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-73. Radial Displacement History (m) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-74. Vertical Displacement History (m) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-75. Pressure History (Pa) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-76. Deviator Stress, J2, History (Pa) in Soil at Range 0.14 m, Depth 0.4 m (Deformable Penetrator).
- B-77. Radial Velocity History (m/s) in Soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-78. Vertical Velocity History (m/s) in Soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-79. Radial Displacement History (m) in Soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-80. Vertical Displacement History (m) in soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-81. Pressure History (Pa) in Soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-82. Deviator Stress, J2, History (Pa) in Soil at Range 0.28 m, Depth 0.1 m (Deformable Penetrator).
- B-83. Radial Velocity History (m/s) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).

- B-84. Vertical Velocity History (m/s) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).
- B-85. Radial Displacement History (m) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).
- B-86. Vertical Displacement History (m) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).
- B-87. Pressure History (Pa) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).
- B-88. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.28 m, Depth 0.2 m (Deformable Penetrator).
- B-89. Radial Velocity History (m/s) in Soil at Range 0.28 m, Depth 0.4 m (Deformable Penetrator).
- B-90. Vertical Velocity History (m/s) in Soil at Range 2.28 m, Depth 0.4 m (Deformable Penetrator).
- B-91. Radial Displacement History (m) in Soil at Range 0.28 m, Depth 0.4 m (Deformable Penetrator).
- B-92. Vertical Displacement History (m) in Soil at Range 0.28 m, Depth 0.4 m (Deformable Penetrator).
- B-93. Pressure History (Pa) in Soil at Range 0.28 m, Depth 0.4 m (Deformable Penetrator).
- B-94. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.28 m, Depth 0.4 m (Deformable Penetrator).
- B-95. Radial Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-96. Vertical Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).

- B-97. Radial Displacement History (m) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-98. Vertical Displacement History (m) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-99. Pressure History (Pa) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-100. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-101. Radial Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.2 m (Deformable Penetrator).
- B-102. Vertical Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.2 m (Deformable Penetrator).
- B-103. Radial Displacement History (m) in Soil at Range 0.44 m, Depth 0.2 m (Deformable Penetrator).
- B-104. Vertical Displacement History (m) in Soil at Range 0.44 m, Depth 0.2 m (Deformable Penetrator).
- B-105. Pressure History (Pa) in Soil at Range 0.44 m, Depth 0.2 m (Deformable Penetrator).
- B-106. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.44 m, Depth 0.1 m (Deformable Penetrator).
- B-107. Radial Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator).
- B-108. Vertical Velocity History (m/s) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator).
- B-109. Radial Displacement History (m) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator).

- B-110. Vertical Displacement History (m) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator).
- B-111. Pressure History (Pa) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator).
- B-112. Deviator Stress,  $J_2$ , History (Pa) in Soil at Range 0.44 m, Depth 0.4 m (Deformable Penetrator), (Octahedral Shear Stress =  $\sqrt{2/3}(J_2)$ ).

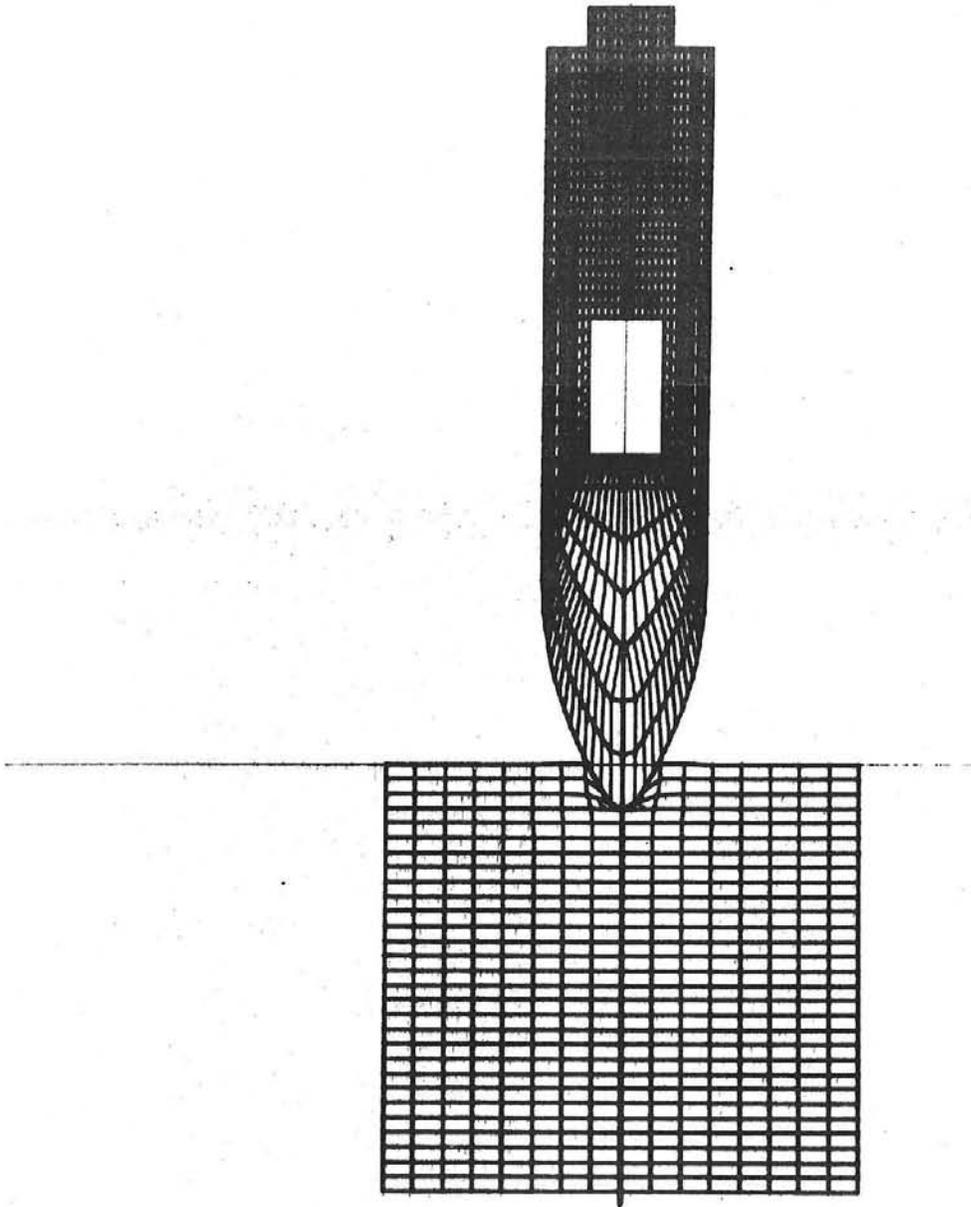


Figure B-1

Lagrangian coordinates at 0.4 ms (radial dimensions doubled to show deformable penetrator).

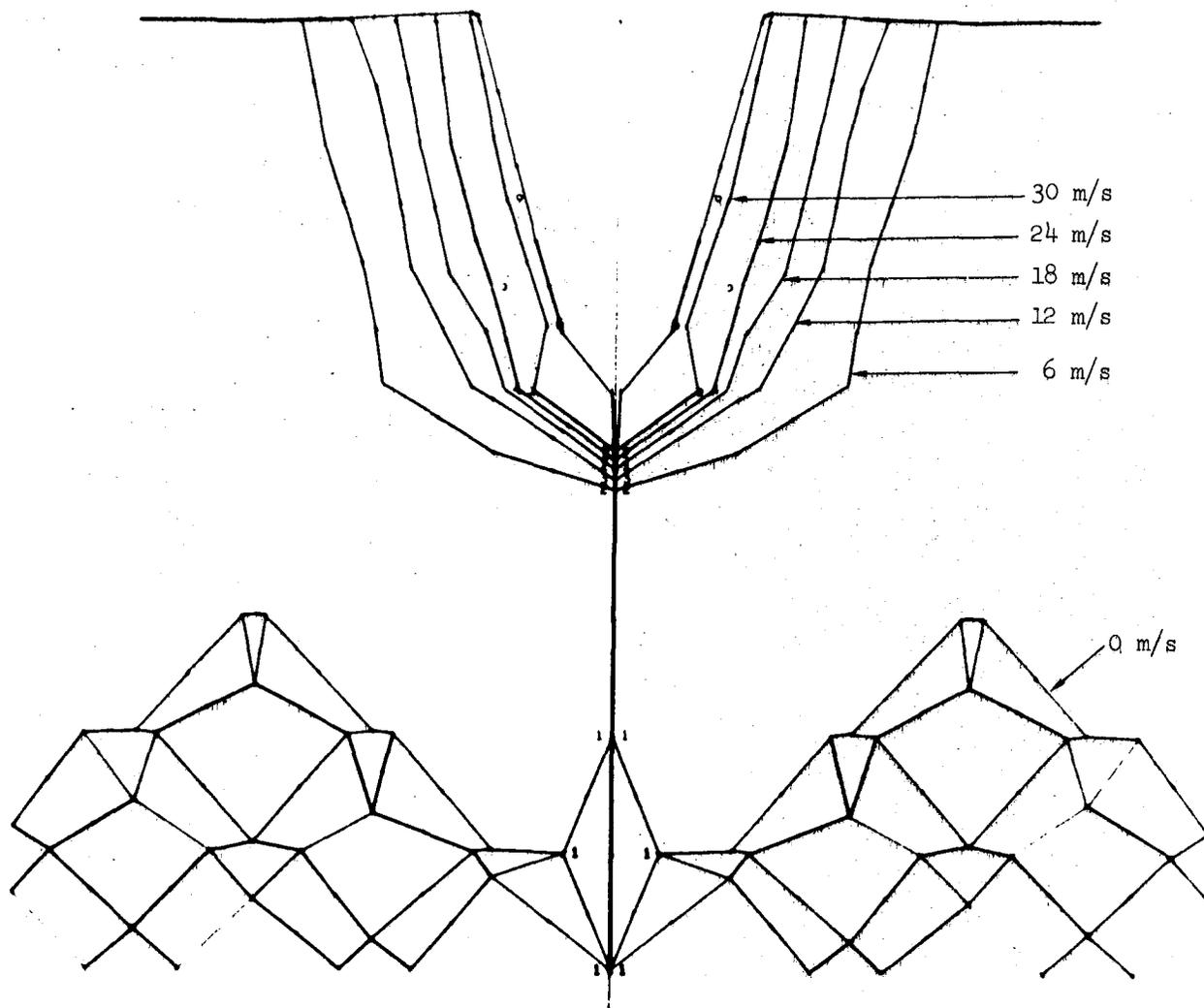


Figure B-2

Contours of radial velocity at 0.4 ms (deformable penetrator not shown).

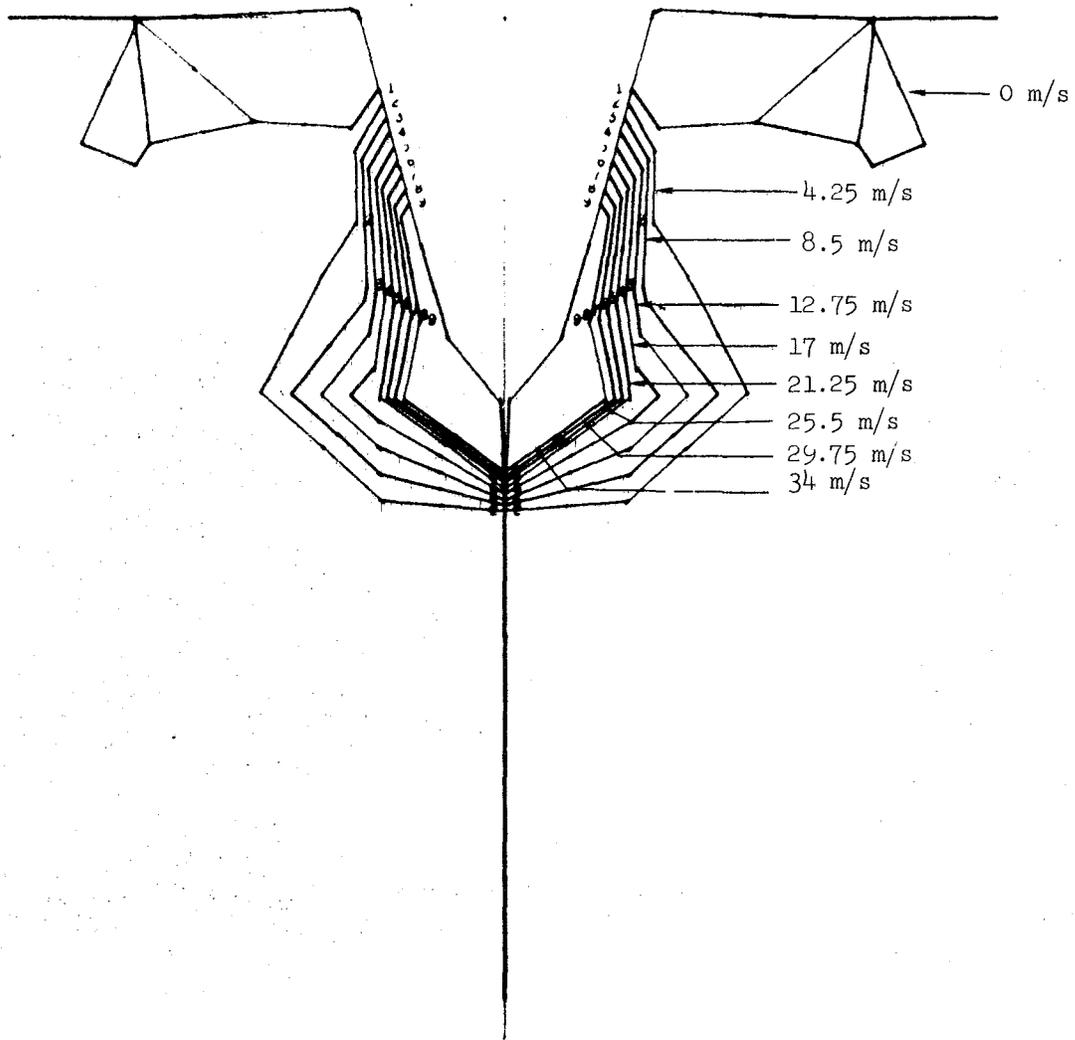


Figure B-3

Contours of vertical velocity at 0.4 ms (deformable penetrator now shown).

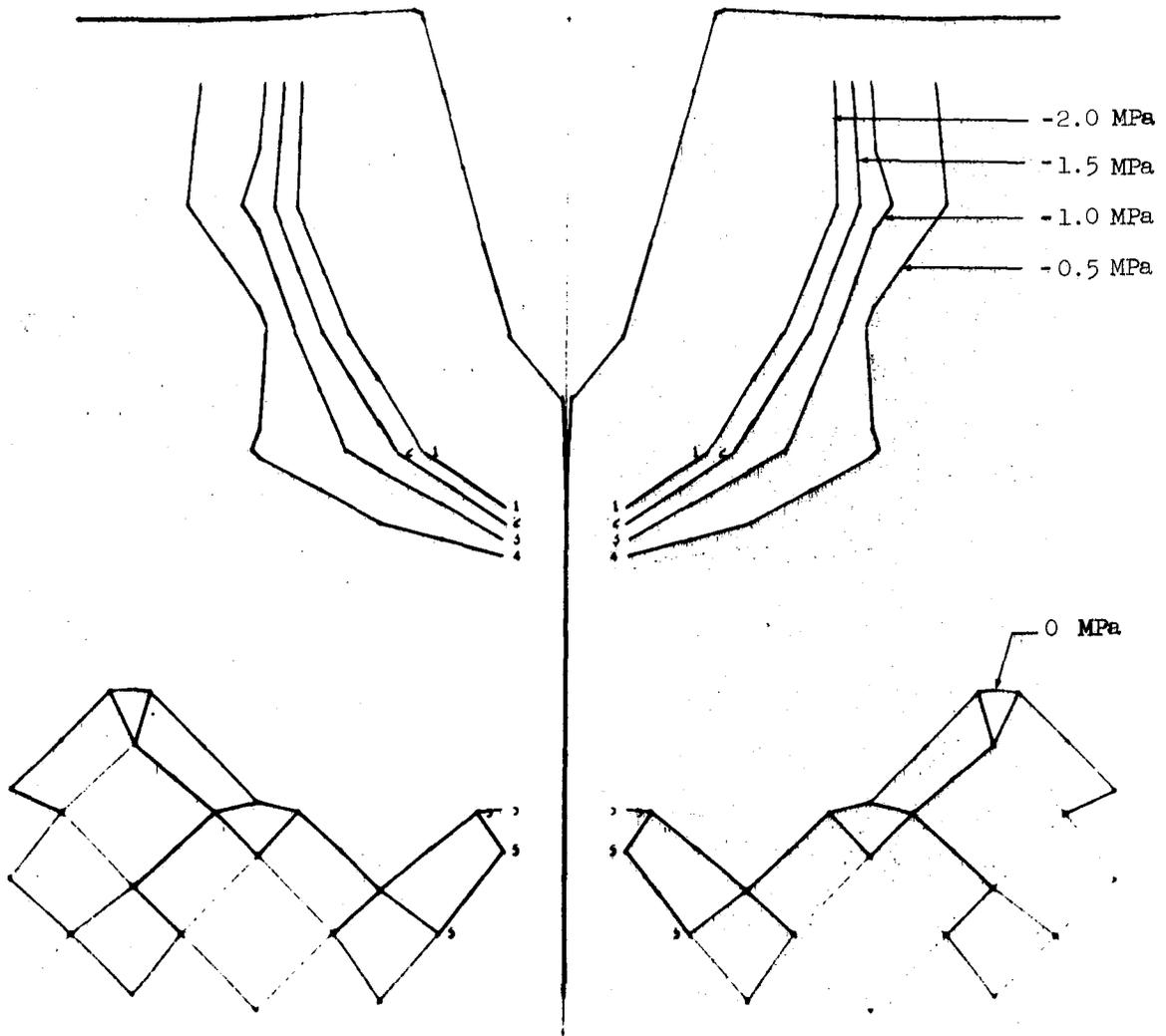


Figure B-4

Contours of radial stress at 0.4 ms (deformable penetrator not shown).

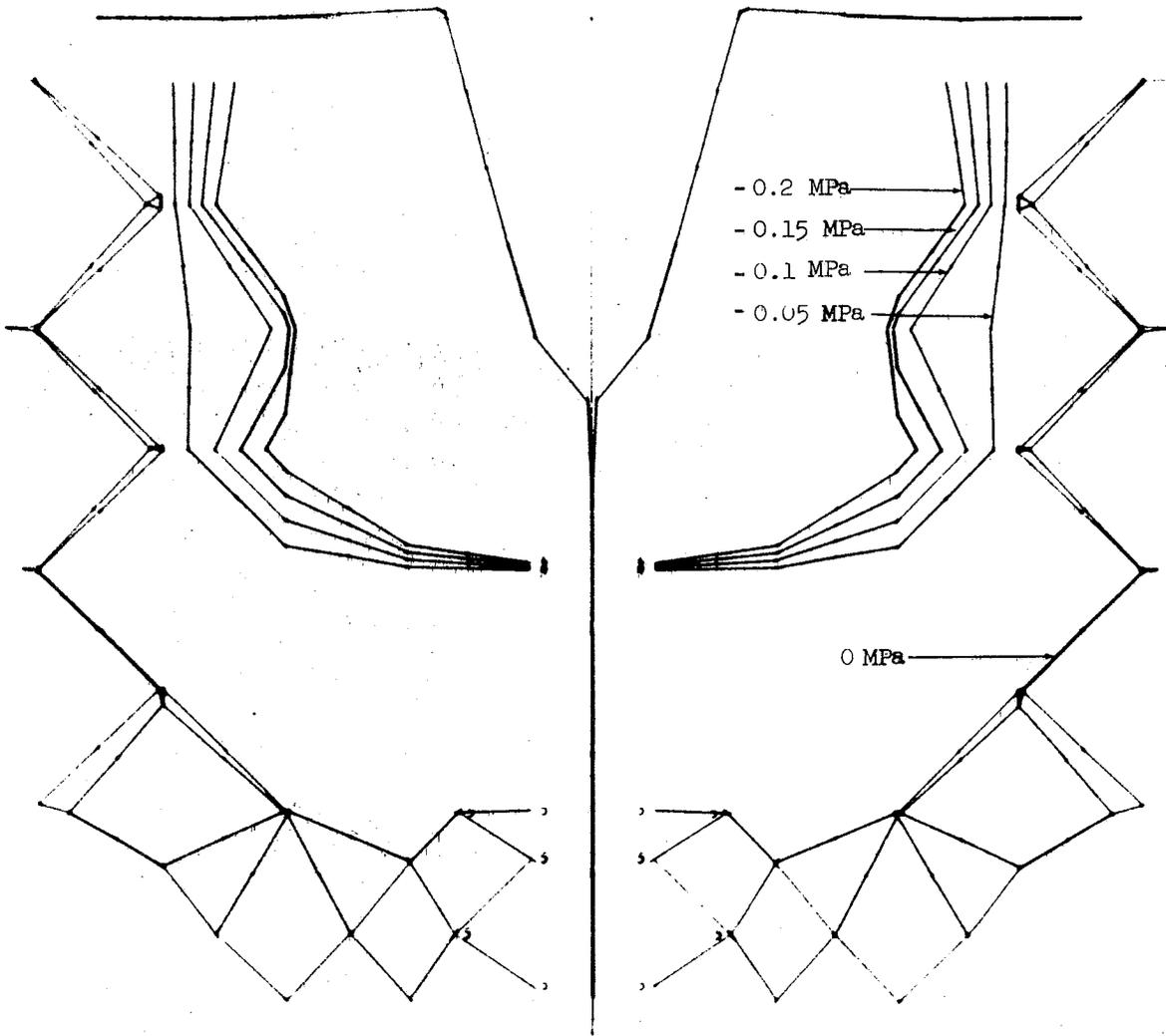


Figure B-5

Contours of hoop stress at 0.4 ms (deformable penetrator not shown).

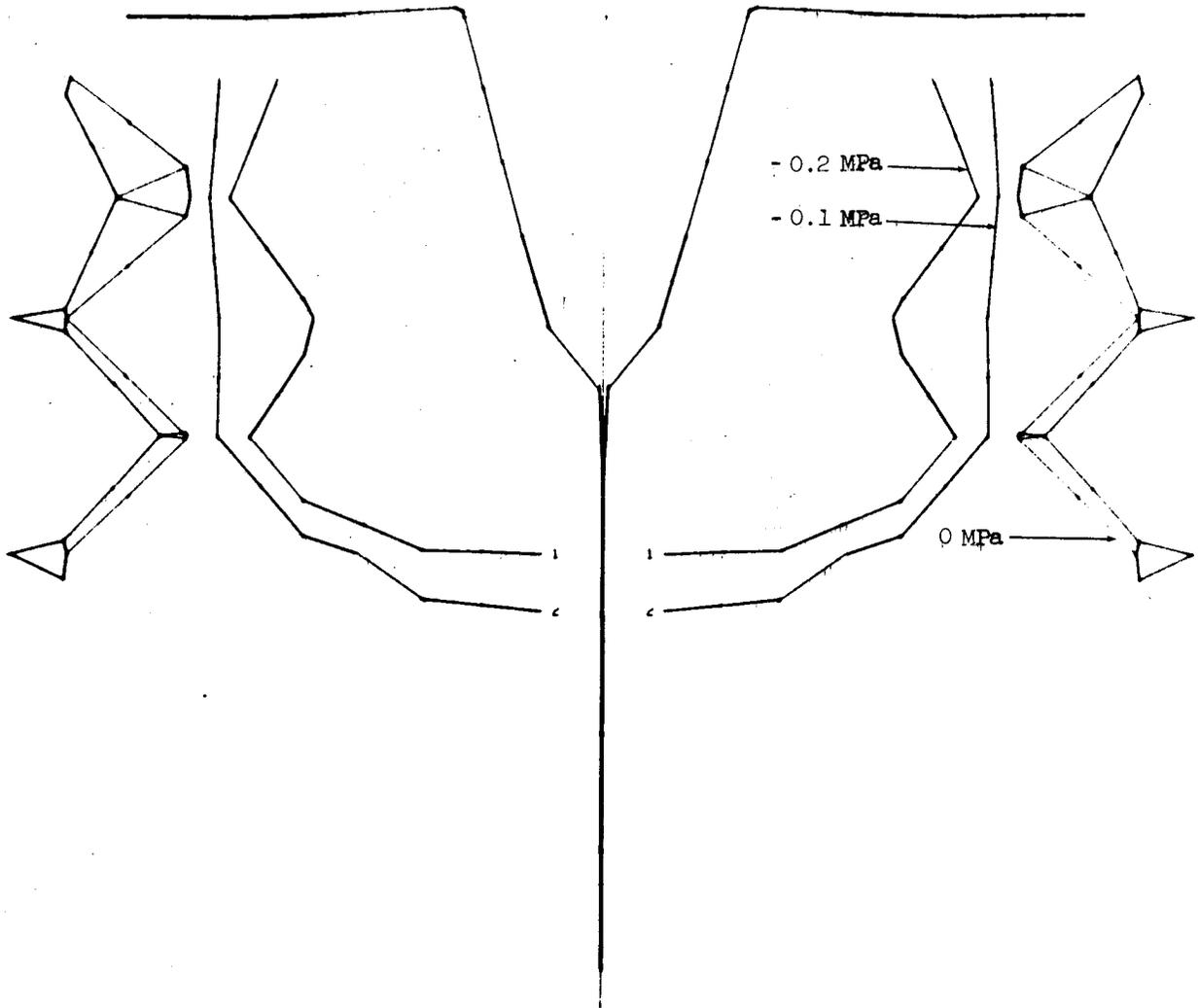


Figure B-6

Contours of vertical stress at 0.4 ms (deformable penetrator not shown).

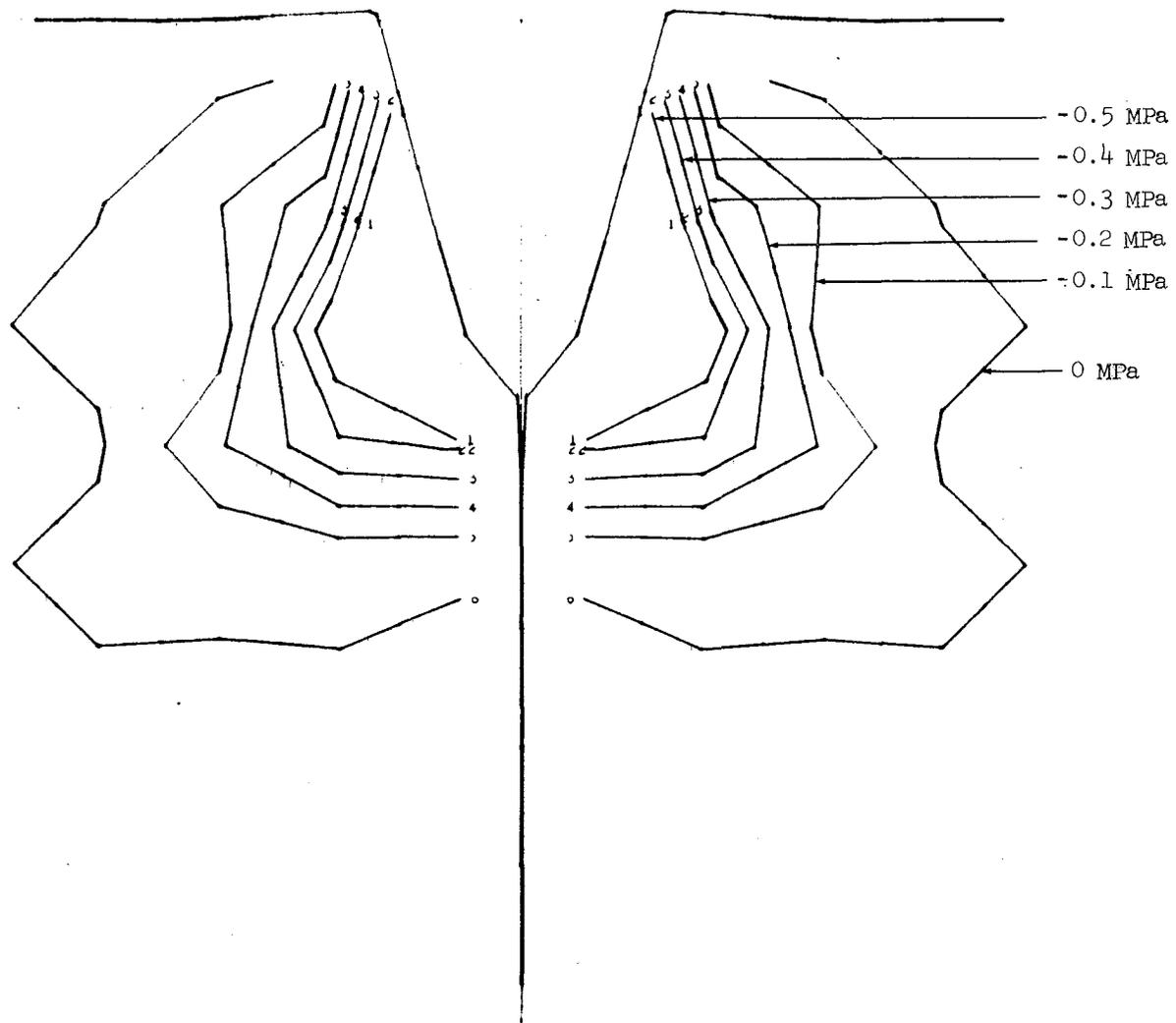


Figure B-7

Contours of radial-vertical shear stress at 0.4 ms (deformable penetrator now shown).

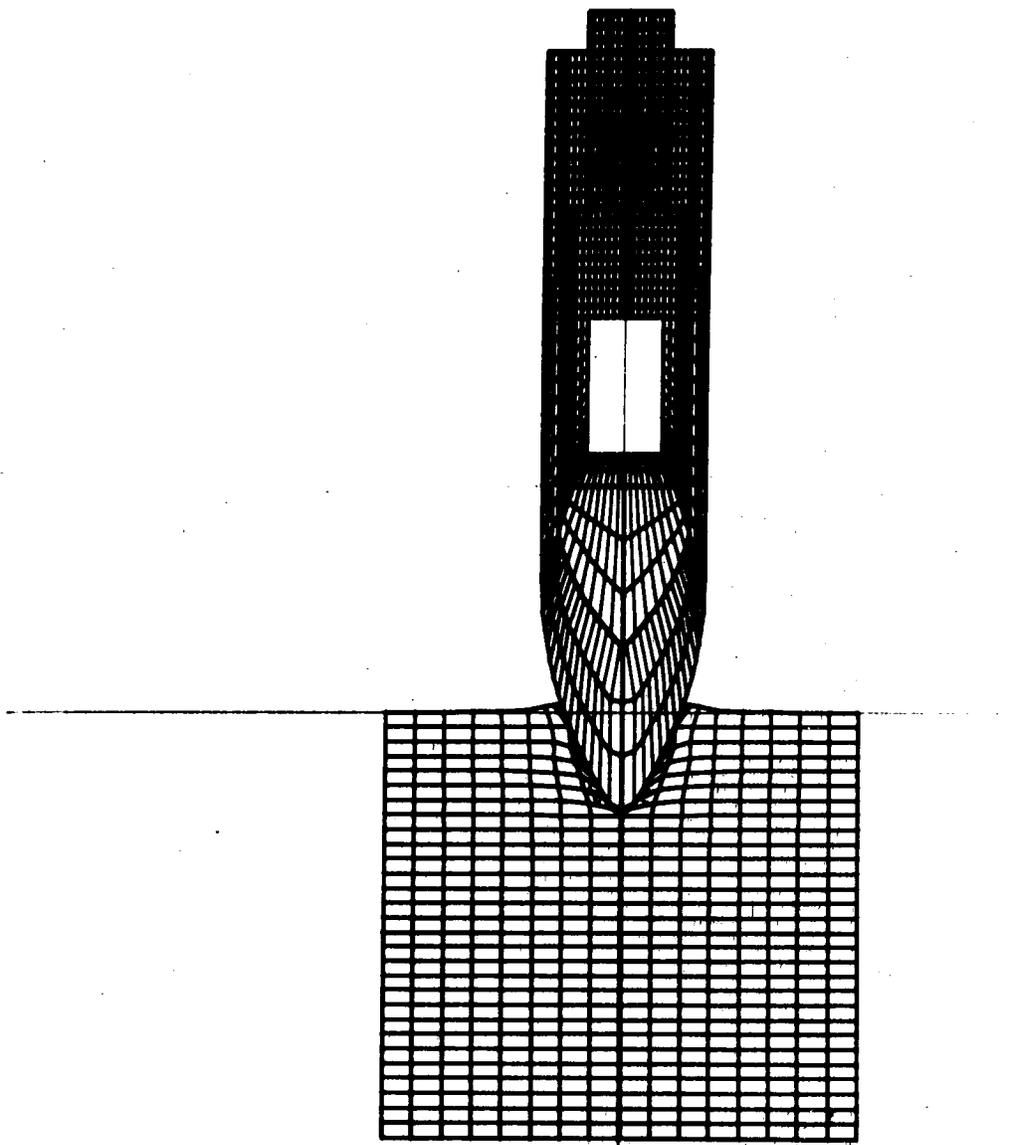


Figure B-8  
Lagrangian coordinates at 1.1 ms (radial dimensions doubled to show deformable penetrator).

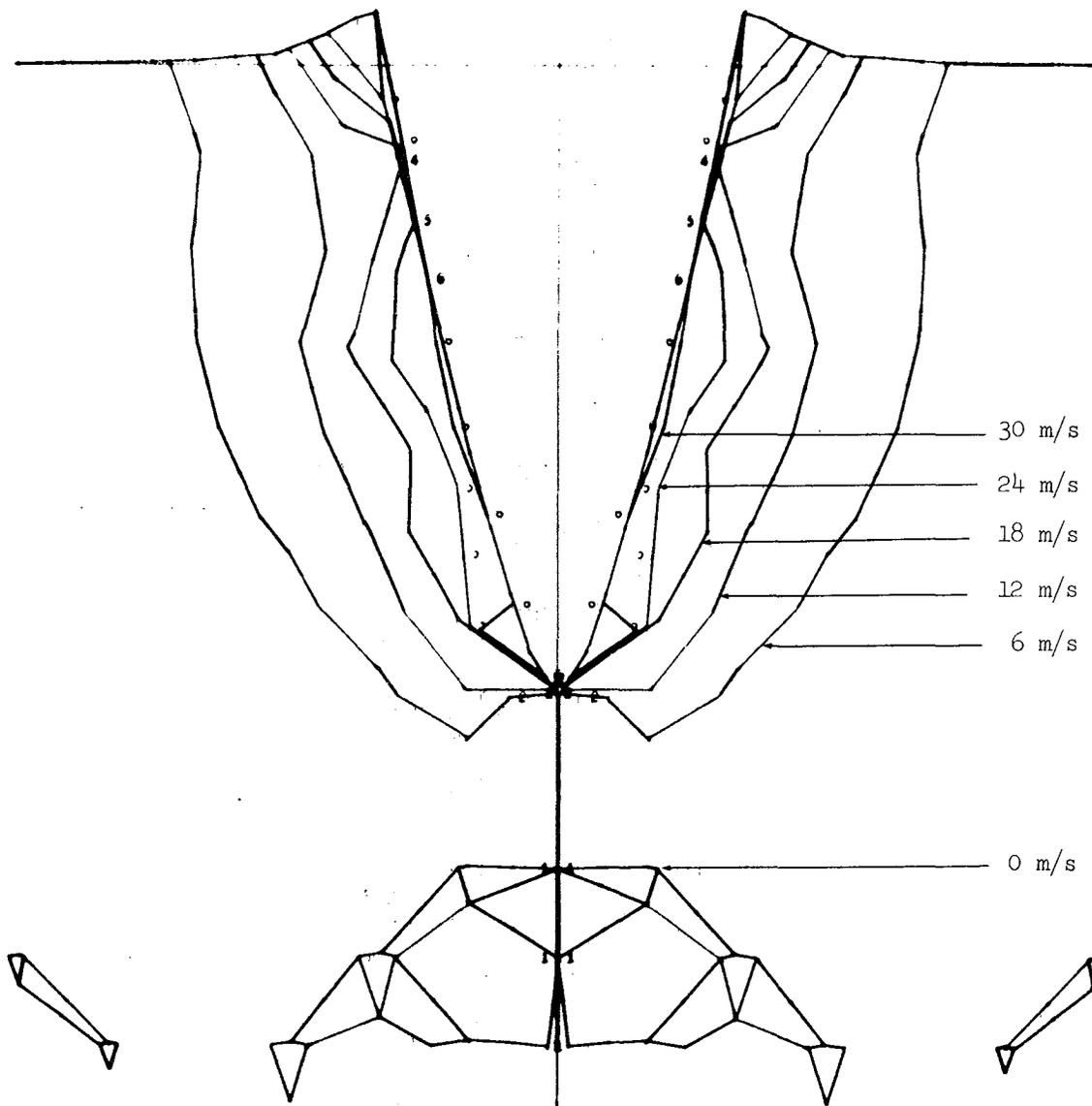


Figure B-9

Contours of radial velocity at 1.1 ms (deformable penetrator now shown).

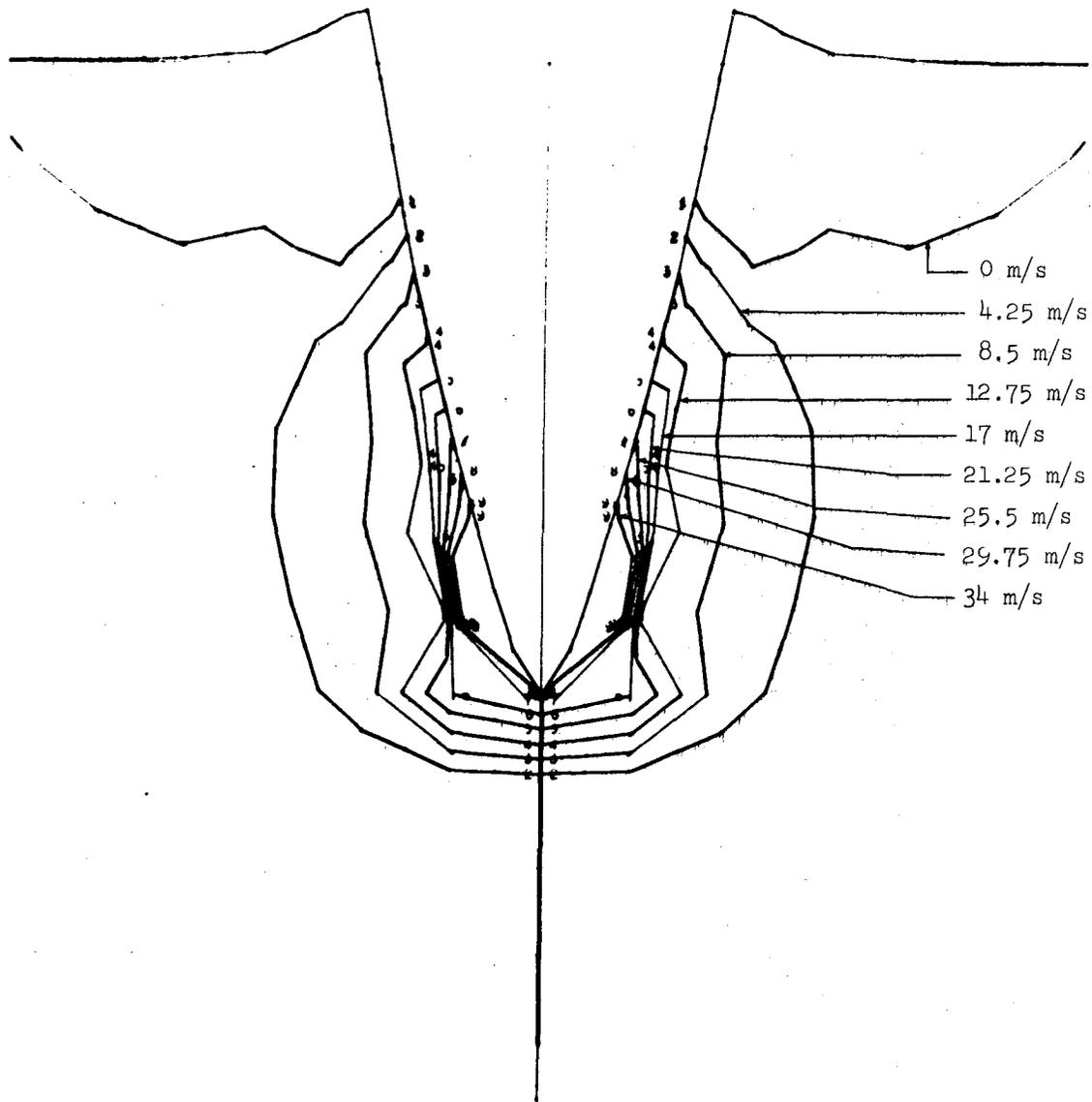


Figure B-10  
Contours of vertical velocity at 1.1 ms (deformable penetrator not shown).

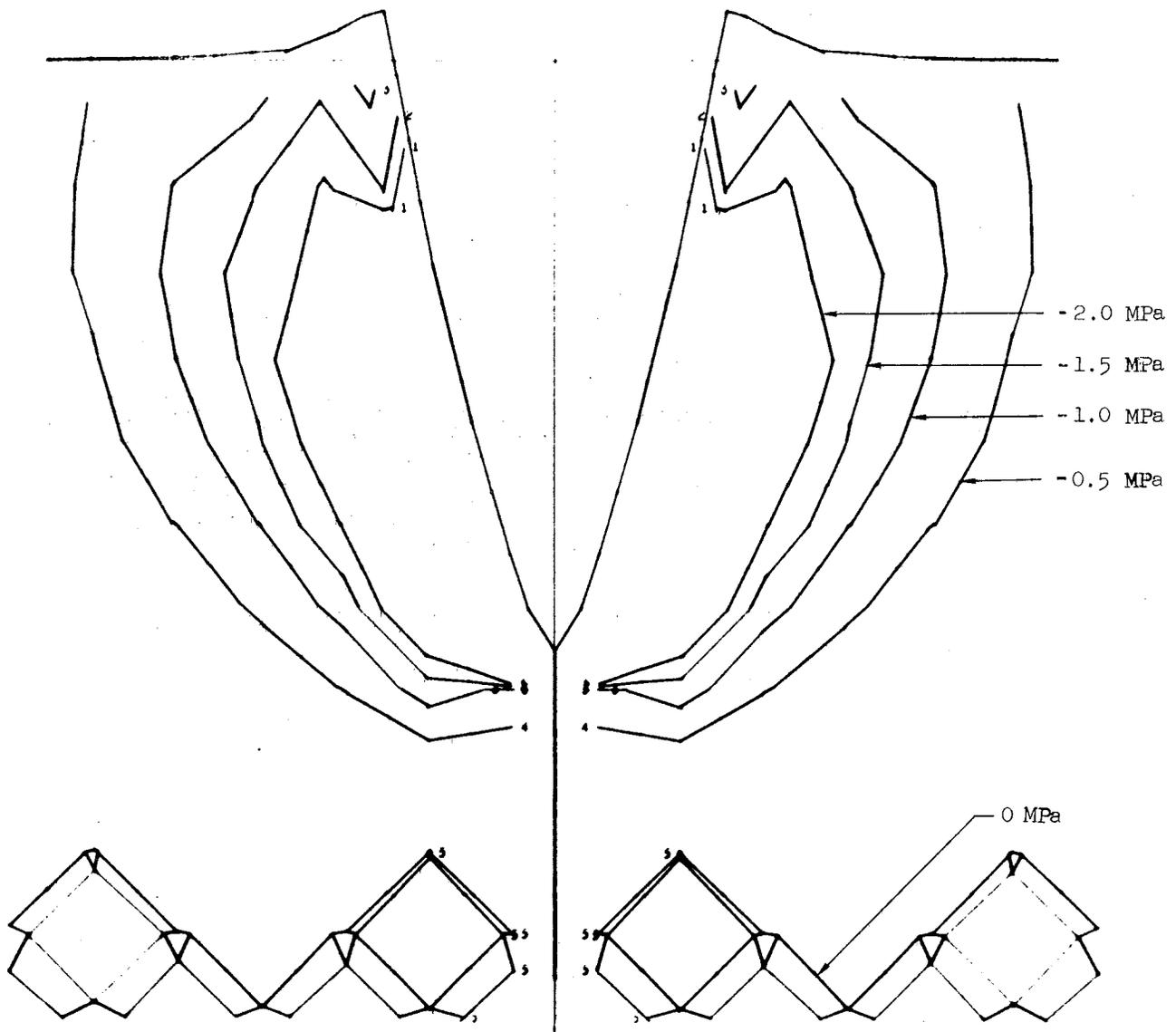


Figure B-11

Contours of radial stress at 1.1 ms (deformable penetrator not shown).

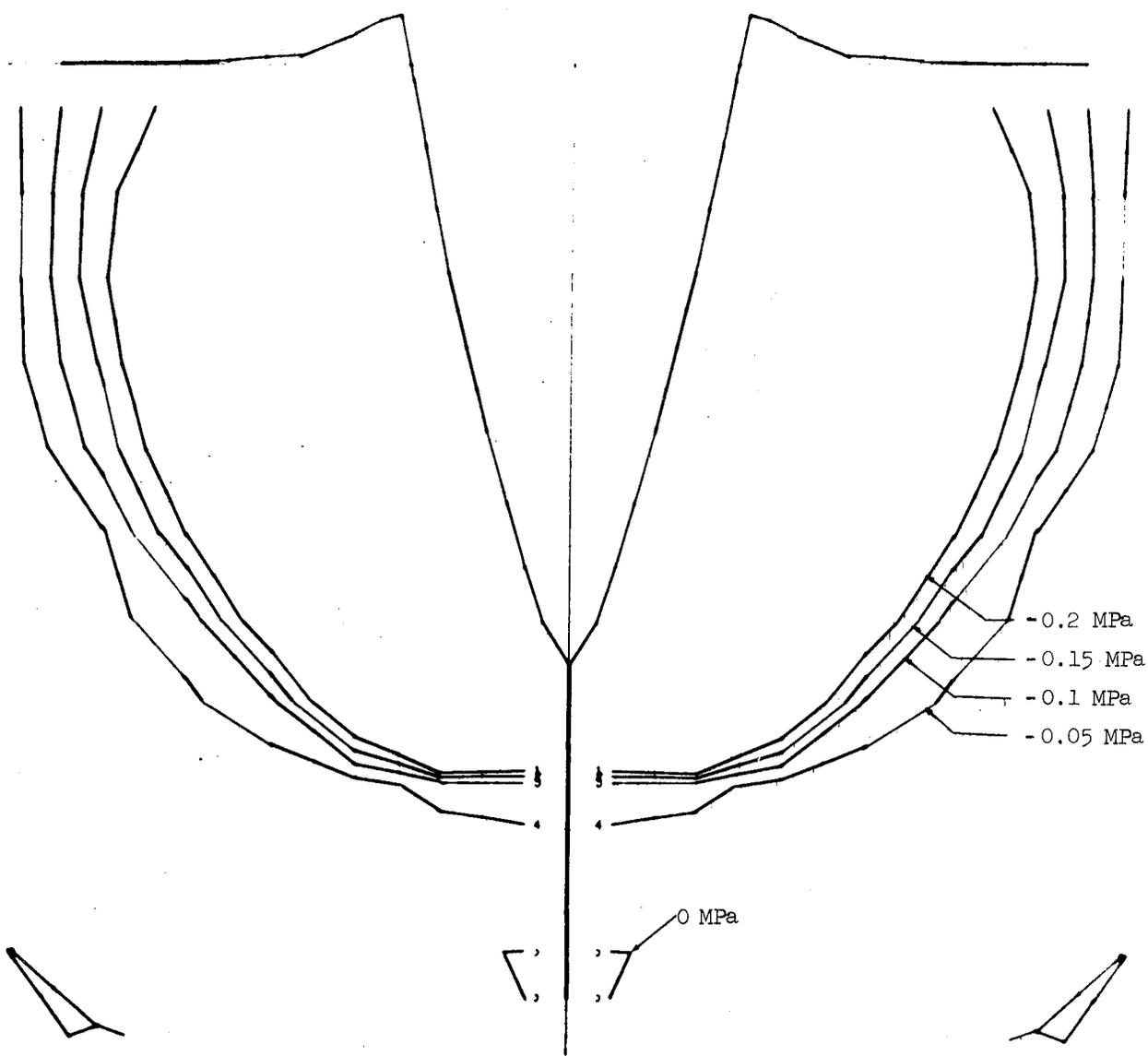


Figure B-12

Contours of hoop stress at 1.1 ms (deformable penetrator not shown).

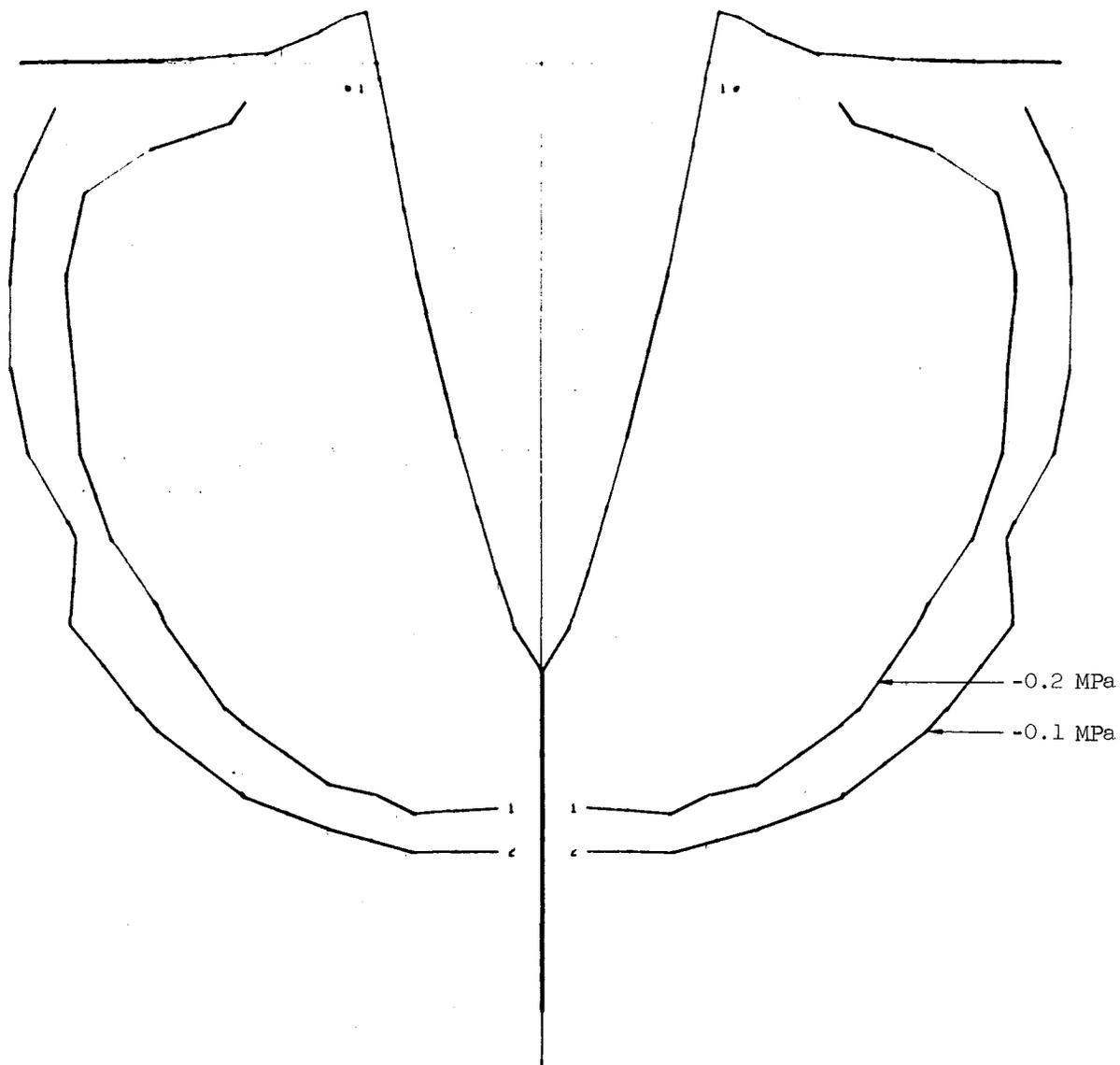


Figure B-13

Contours of vertical stress at 1.1 ms (deformable penetrator not shown).

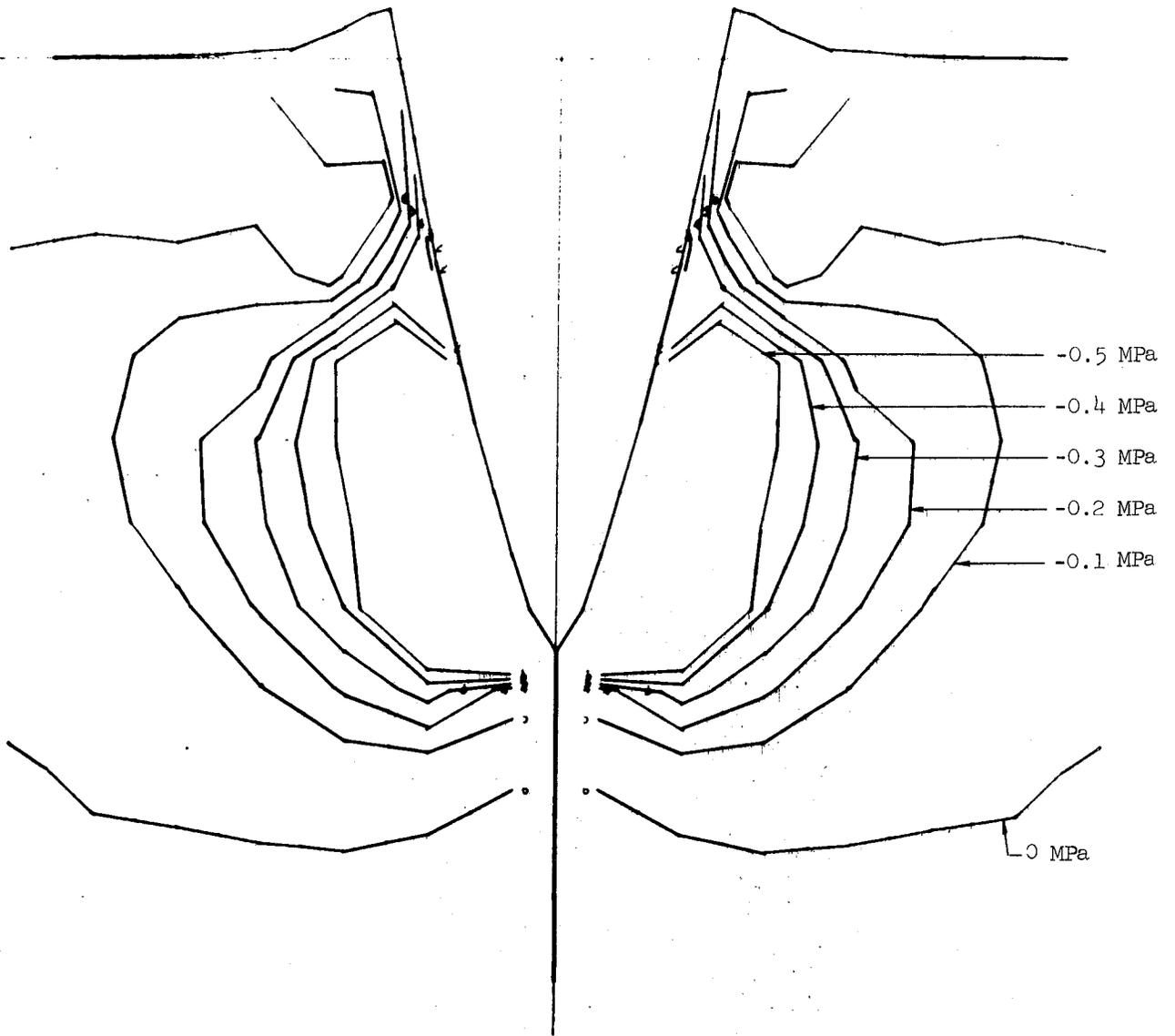


Figure B-14

Contours of radial-vertical shear stress at 1.1 ms (deformable penetrator not shown).

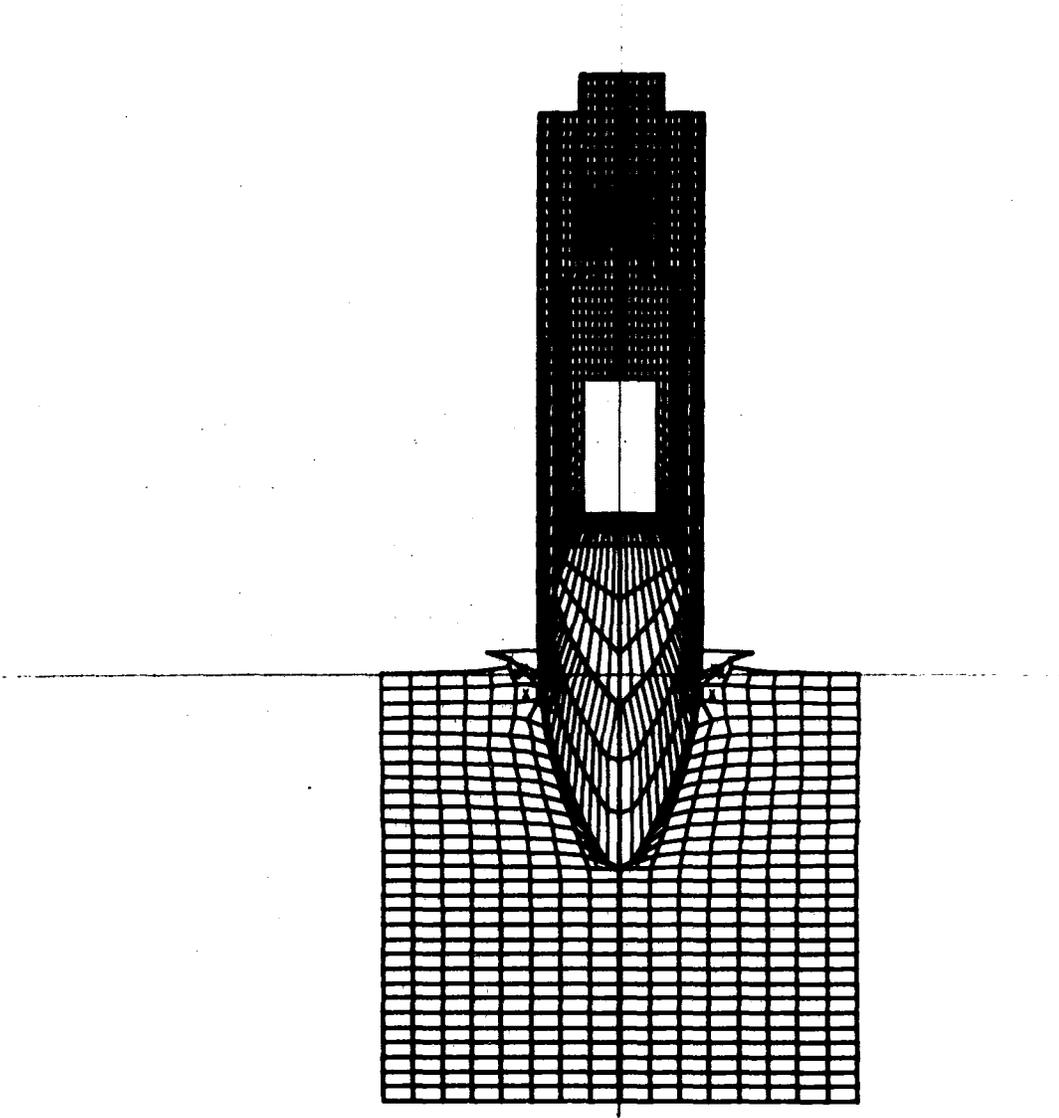


Figure B-15

Lagrangian coordinates at 2.4 ms (radial dimensions doubled to show deformable penetrator).

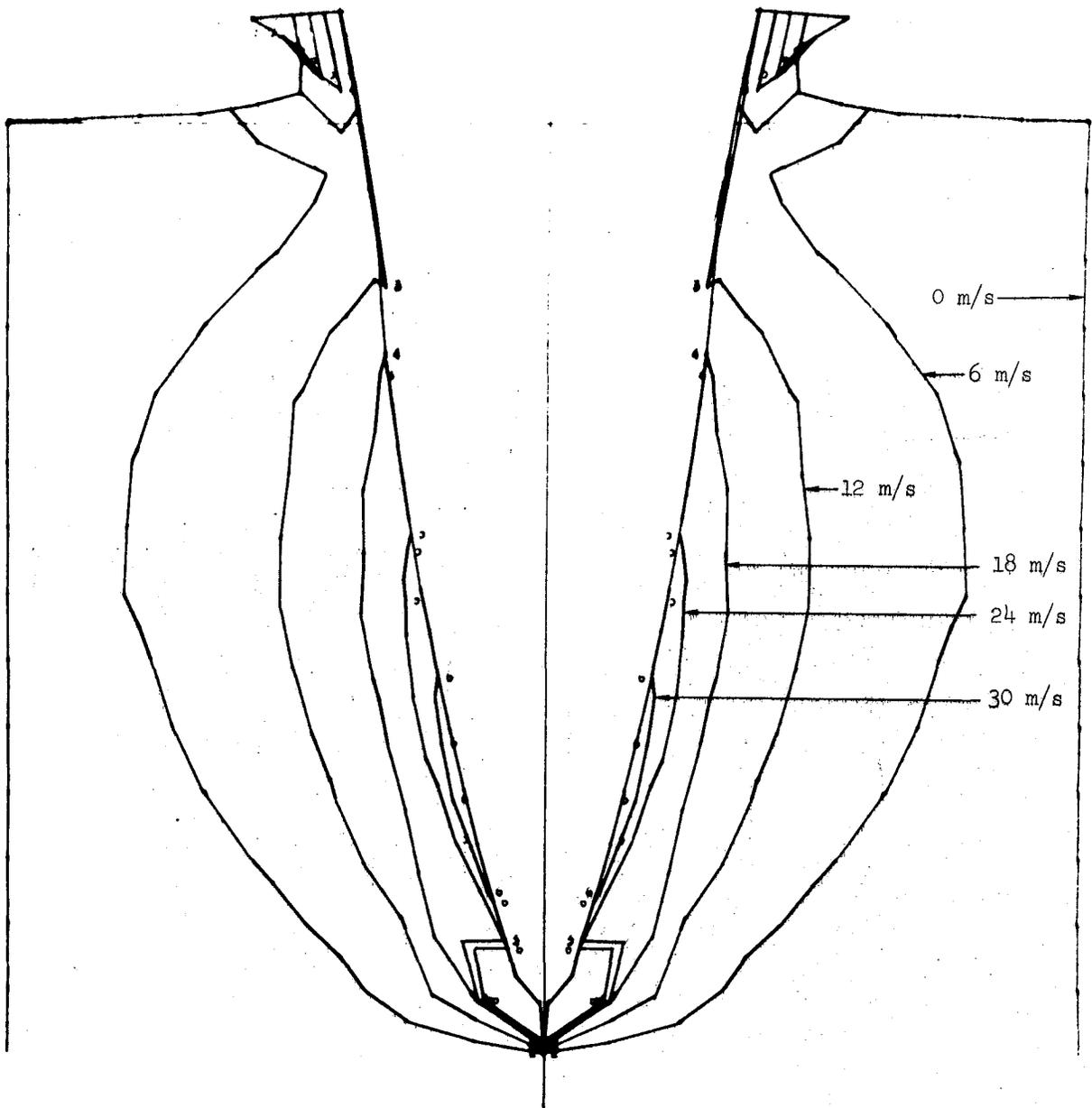


Figure B-16  
Contours of radial velocity at 2.4 ms (deformable penetrator not shown).

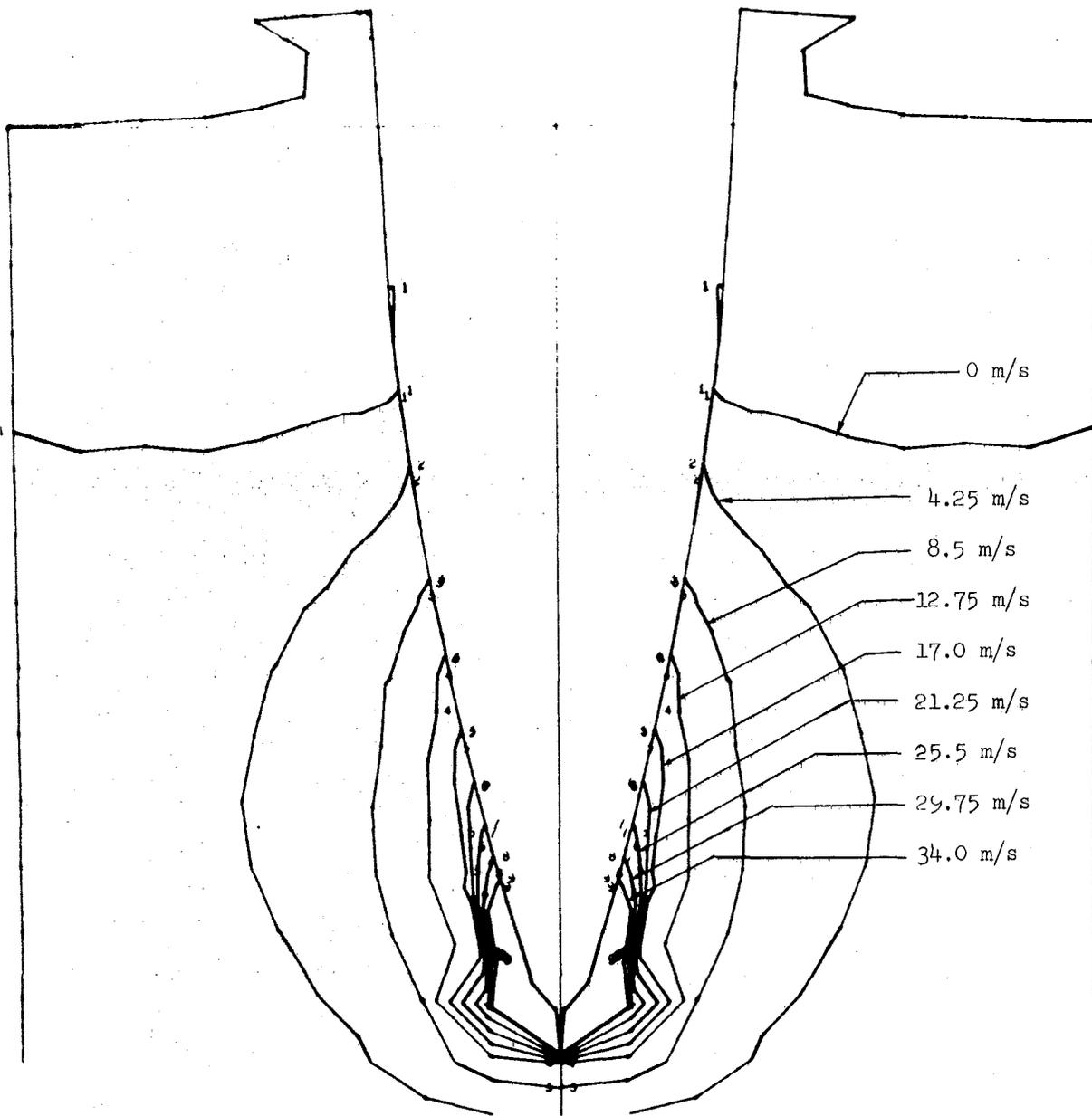


Figure B-17

Contours of vertical velocity at 2.4 ms (deformable penetrator not shown).

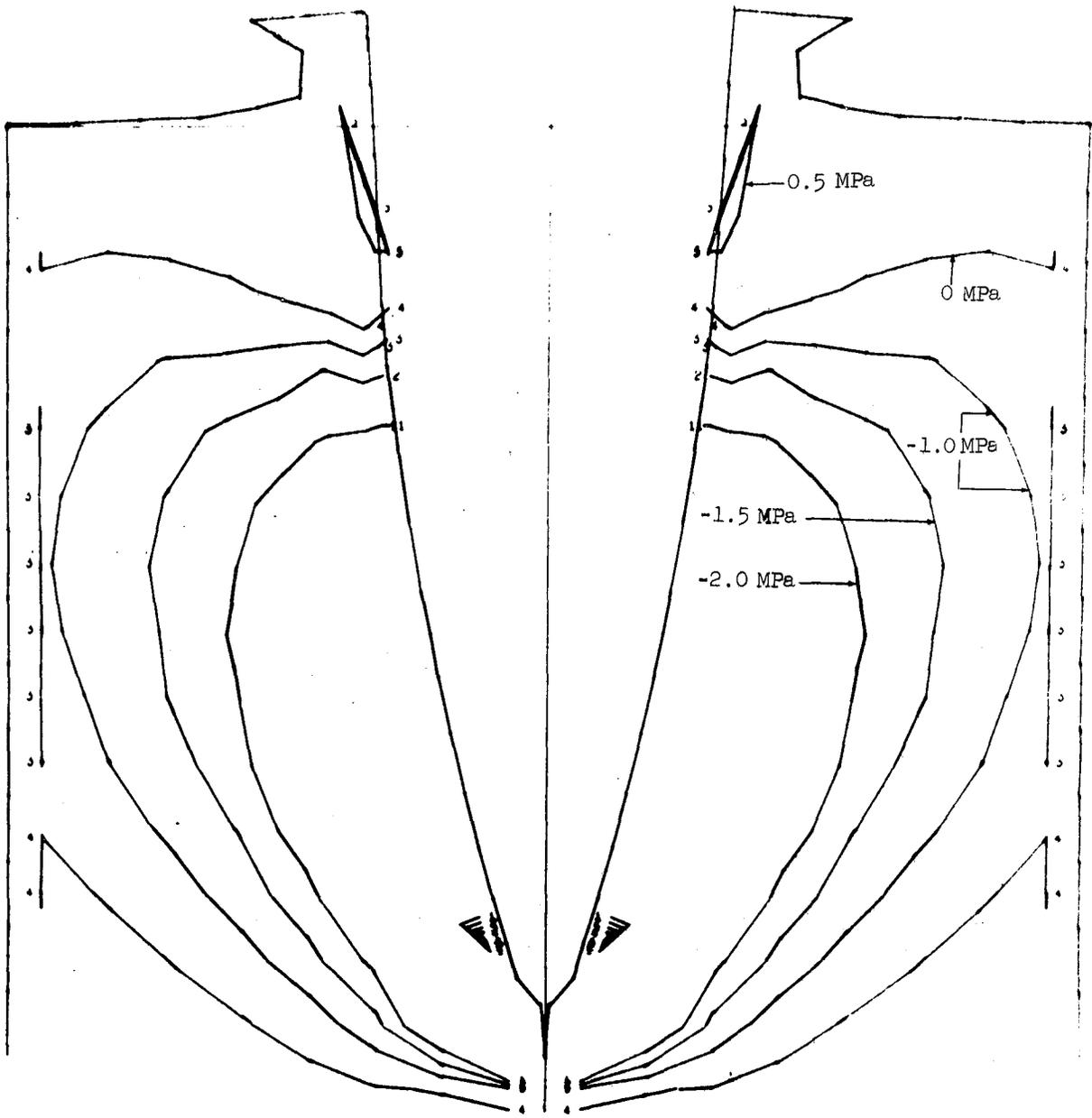


Figure B-18  
Contours of radial stress at 2.4 ms (deformable penetrator not shown).

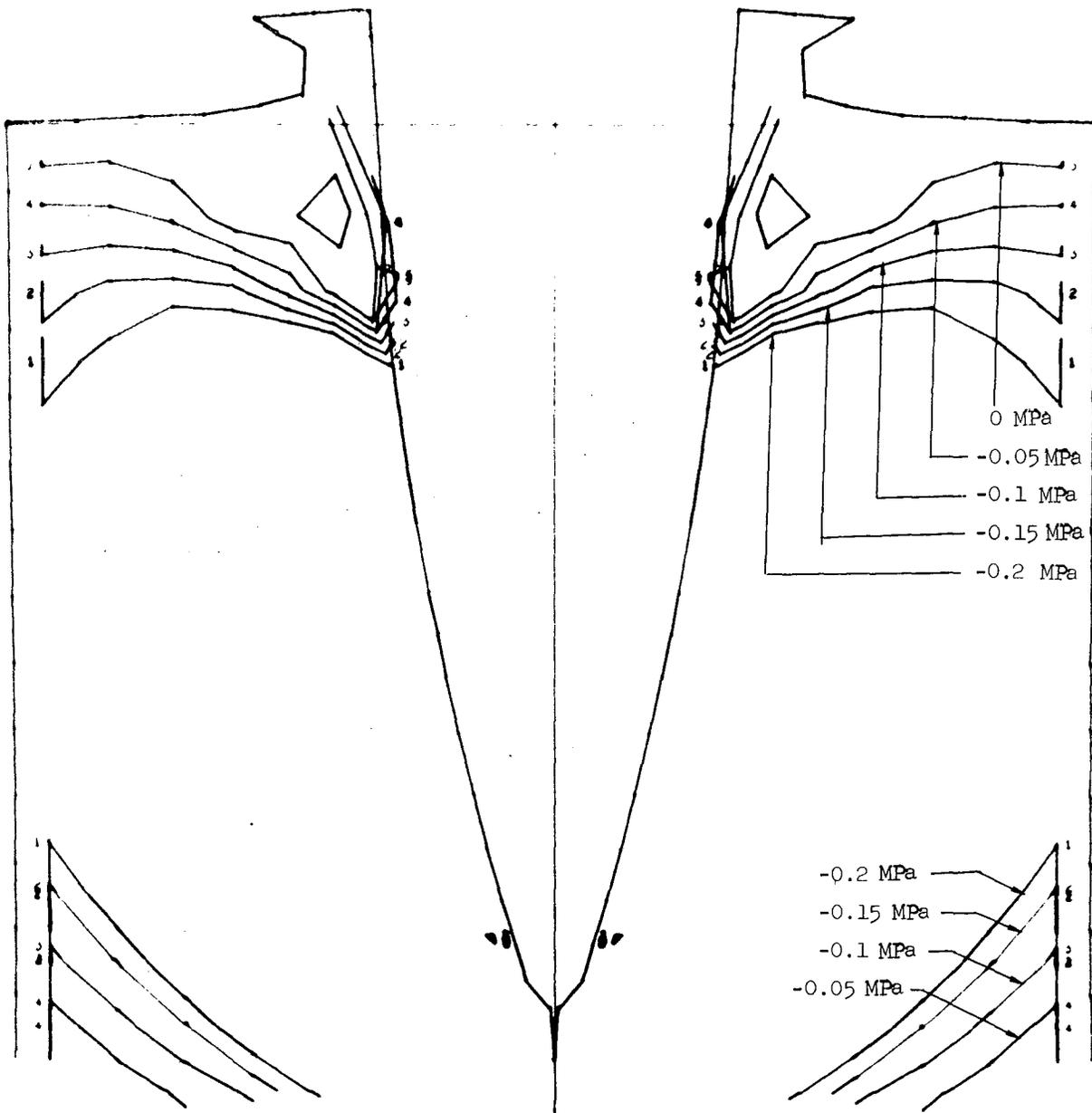


Figure B-19

Contours of hoop stress at 2.4 ms (deformable penetrator not shown).

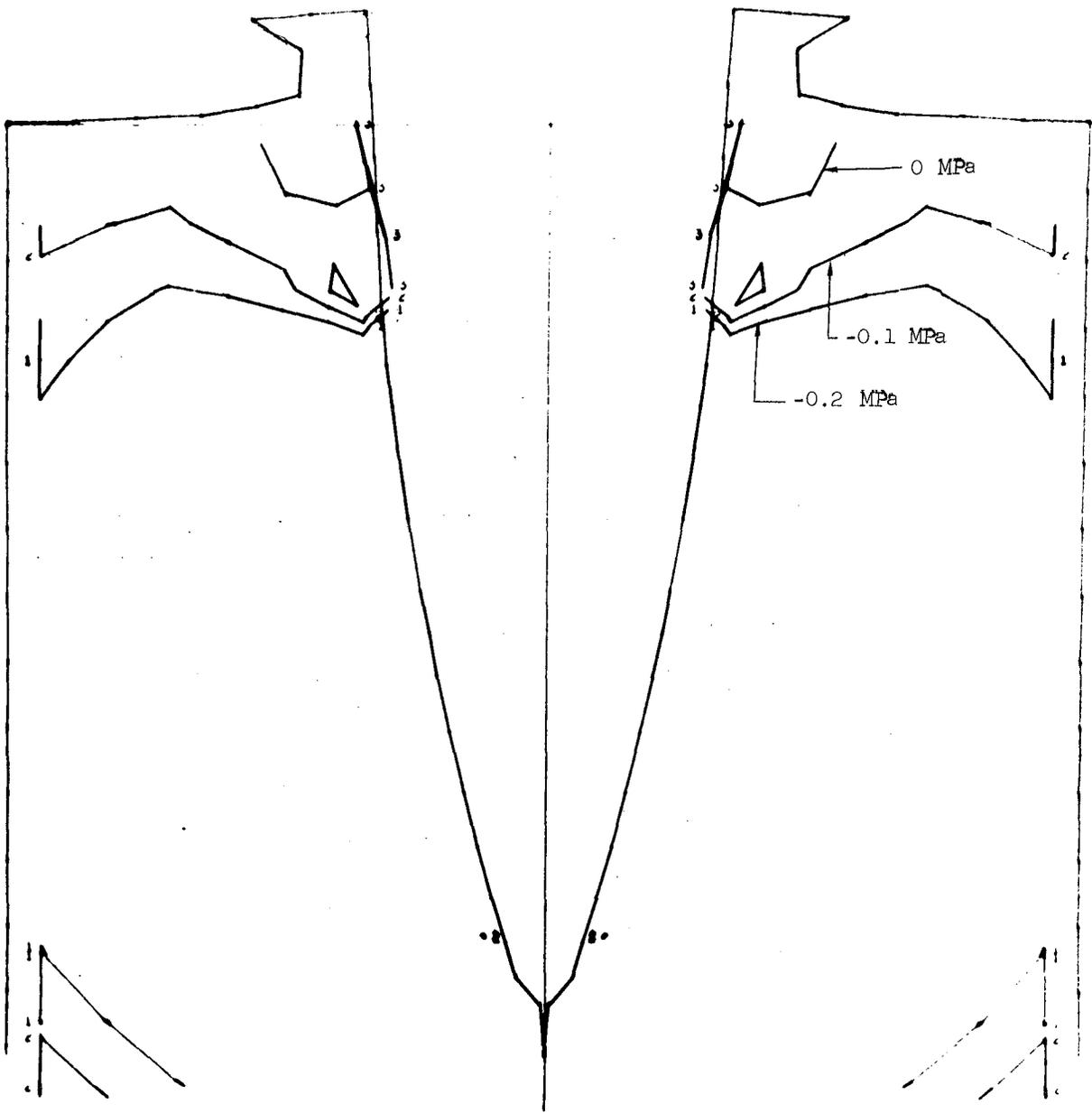


Figure B-20  
 Contours of vertical stress at 2.4 ms (deformable penetrator not shown).

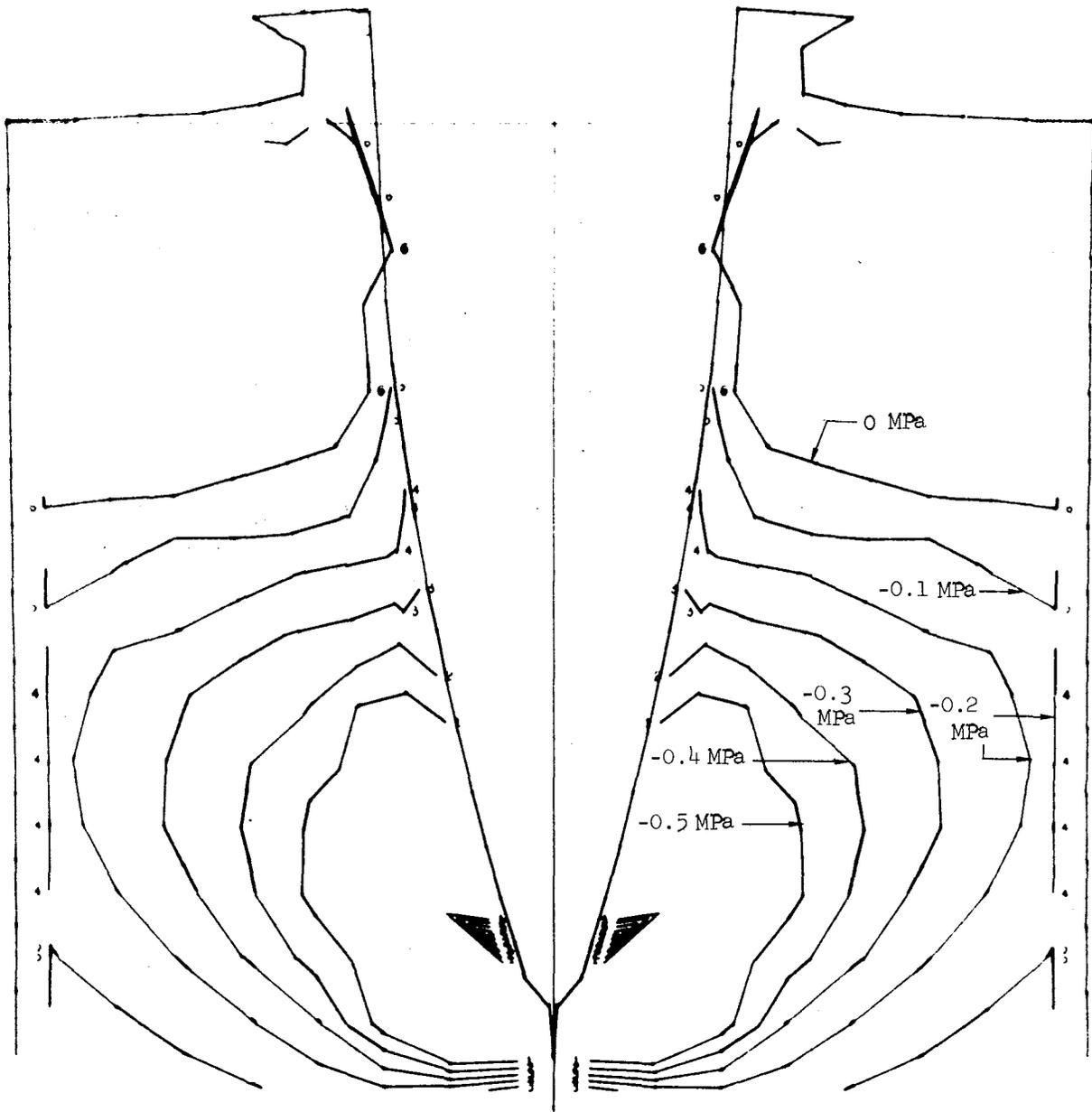


Figure B-21

Contours of radial-vertical shear stress at 2.4 ms (deformable penetrator not shown).

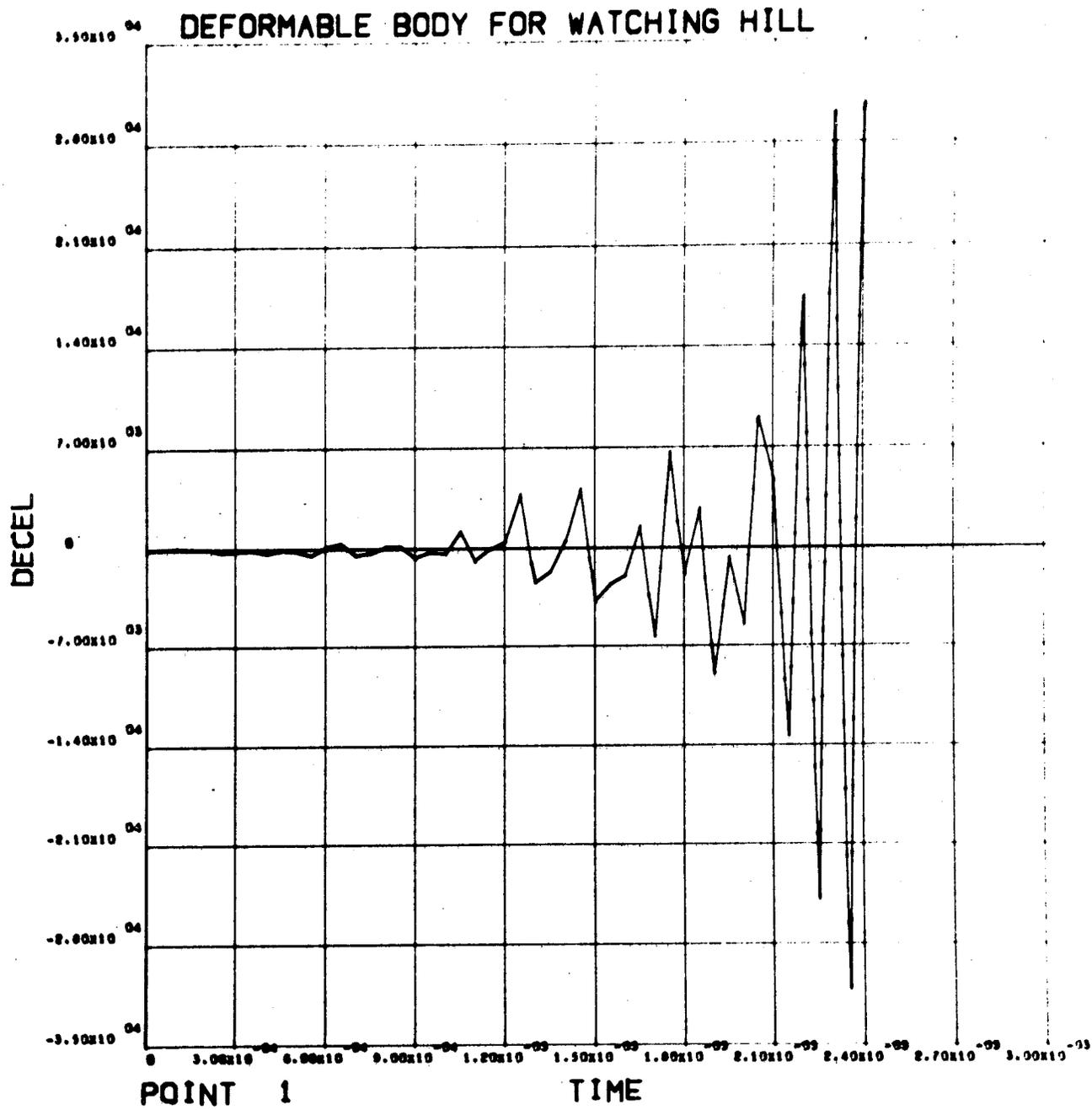


Figure B-22

Deceleration history (g) for point 1 at accelerometer (filtered above 10 kHz).

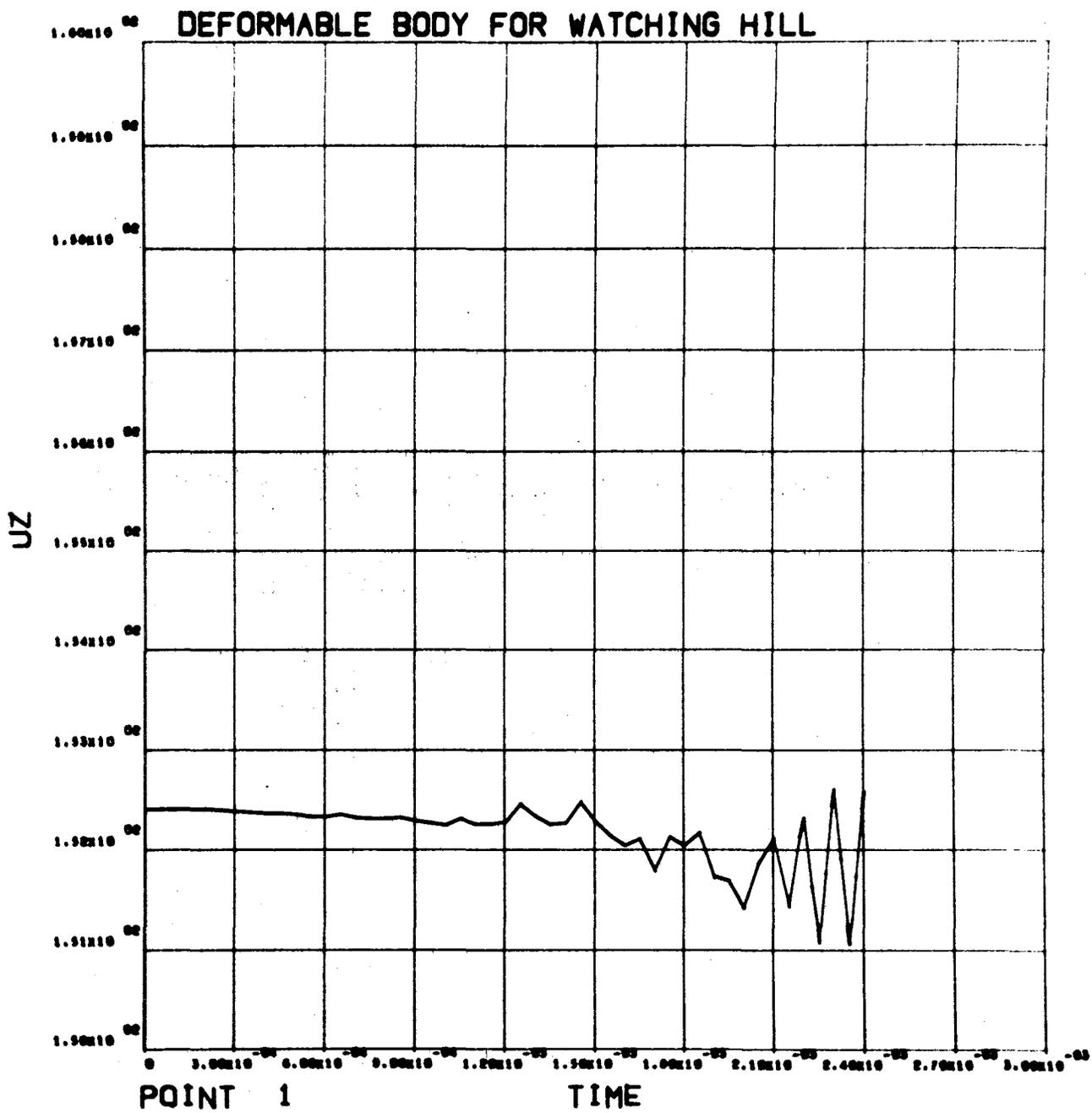


Figure B-23  
Vertical velocity history (m/s) for point 1 at accelerometer.

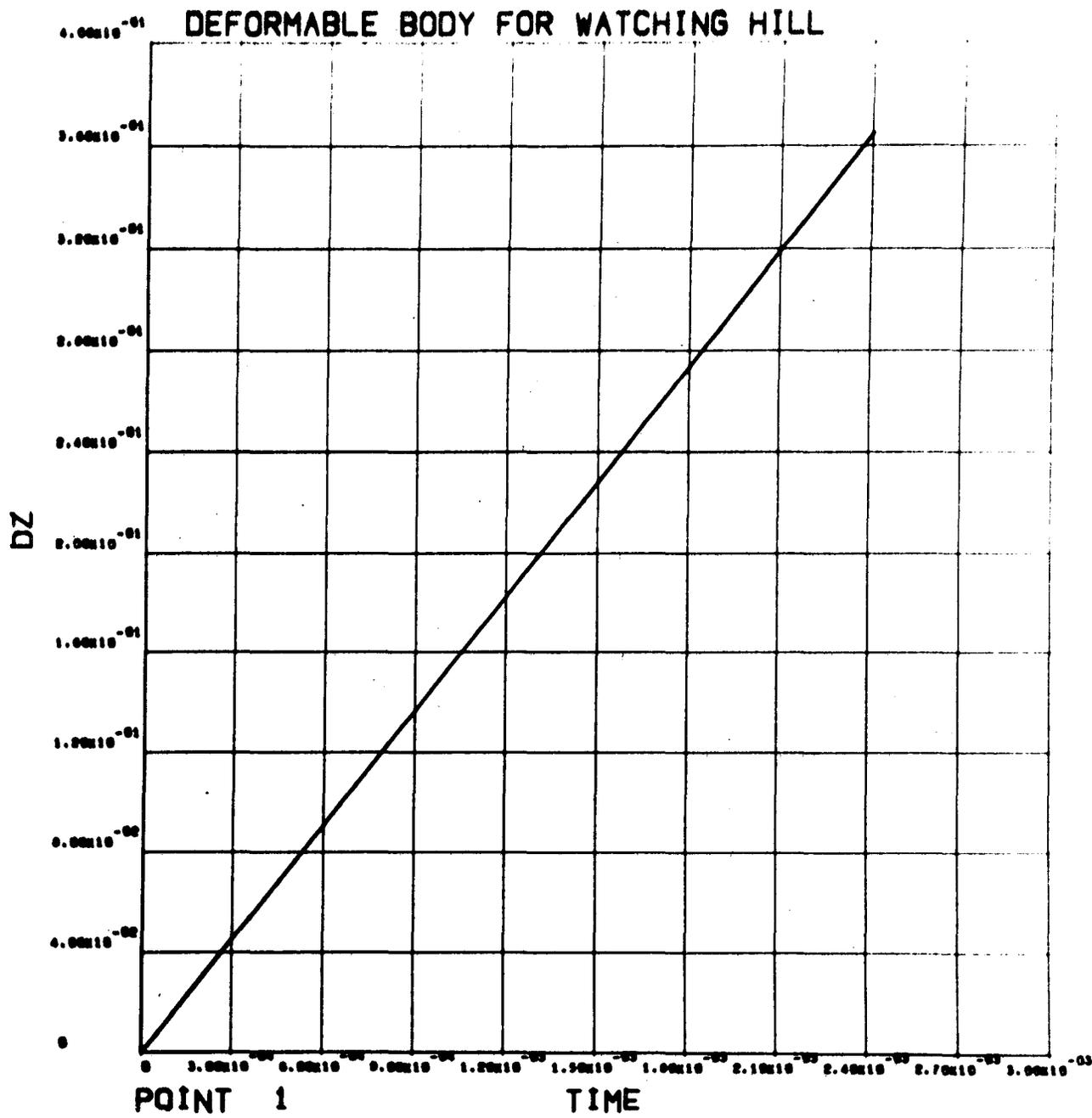


Figure B-24  
Vertical displacement history (m) for point 1 at accelerometer.

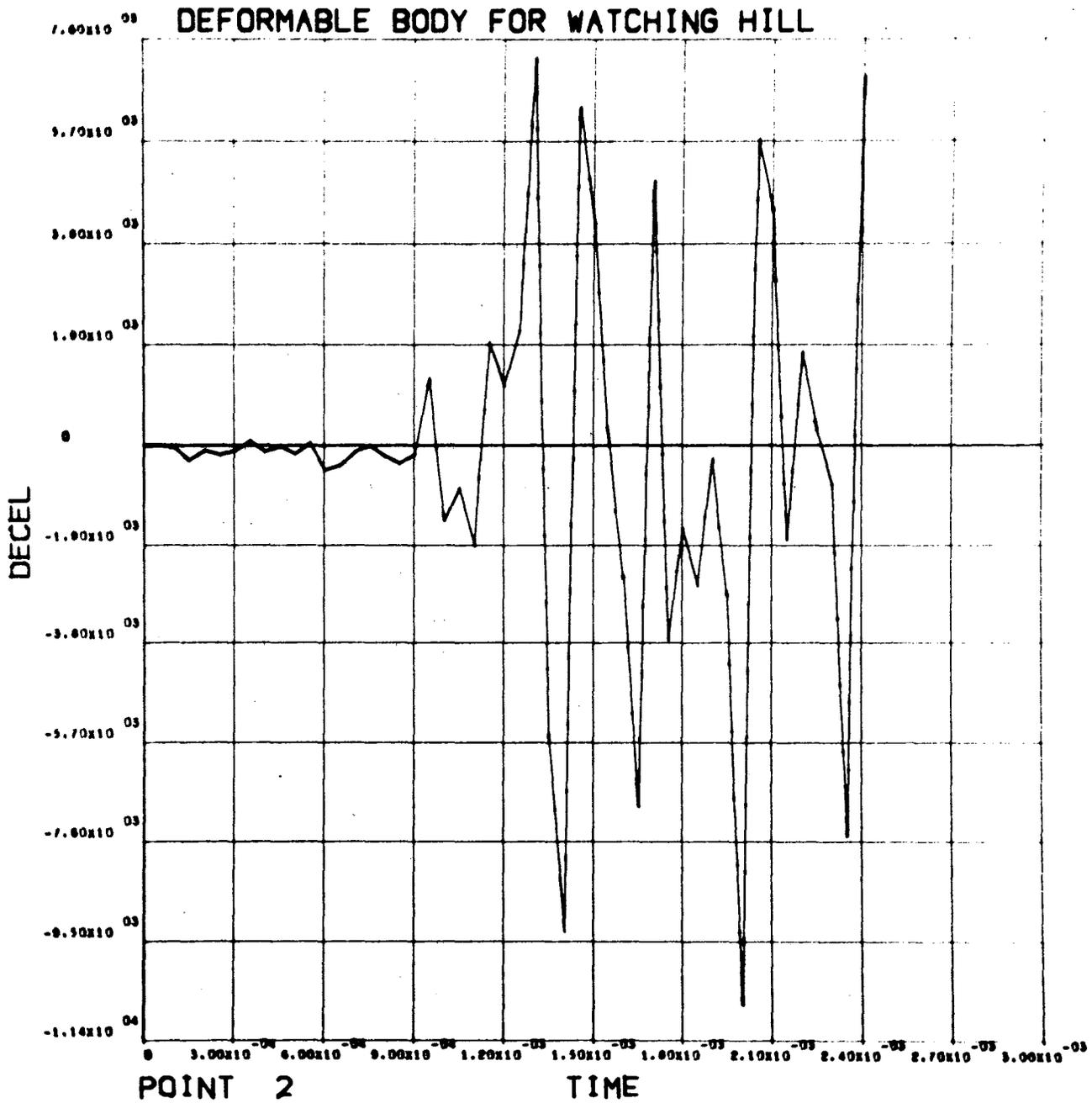


Figure B-25

Deceleration history (g) for point 2, 0.58 m behind penetrator tip and 10 mm from central axis.

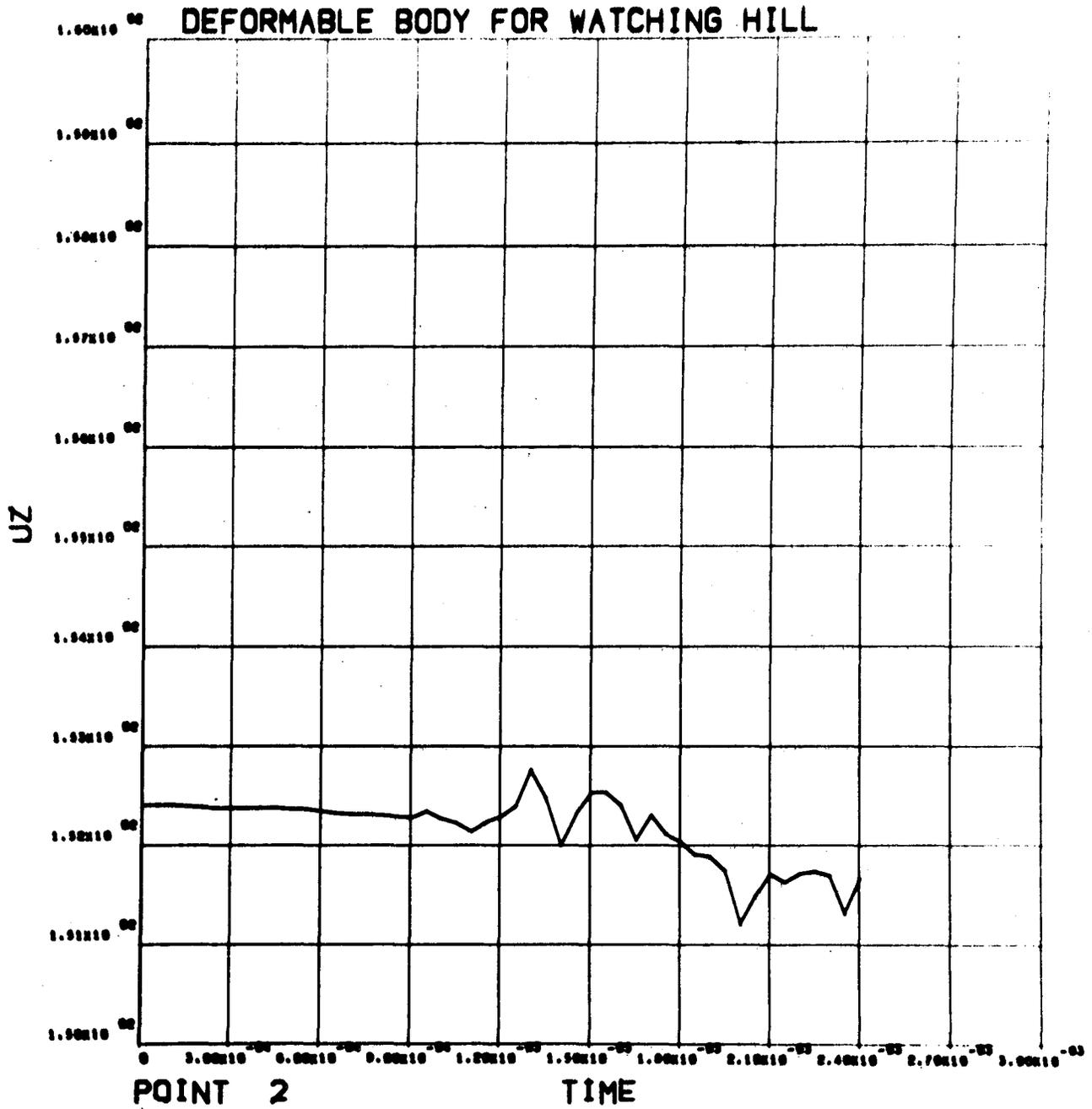


Figure B-26

Vertical velocity history (m/s) for point 2, 0.58 m behind penetrator tip and 10 mm from central axis.

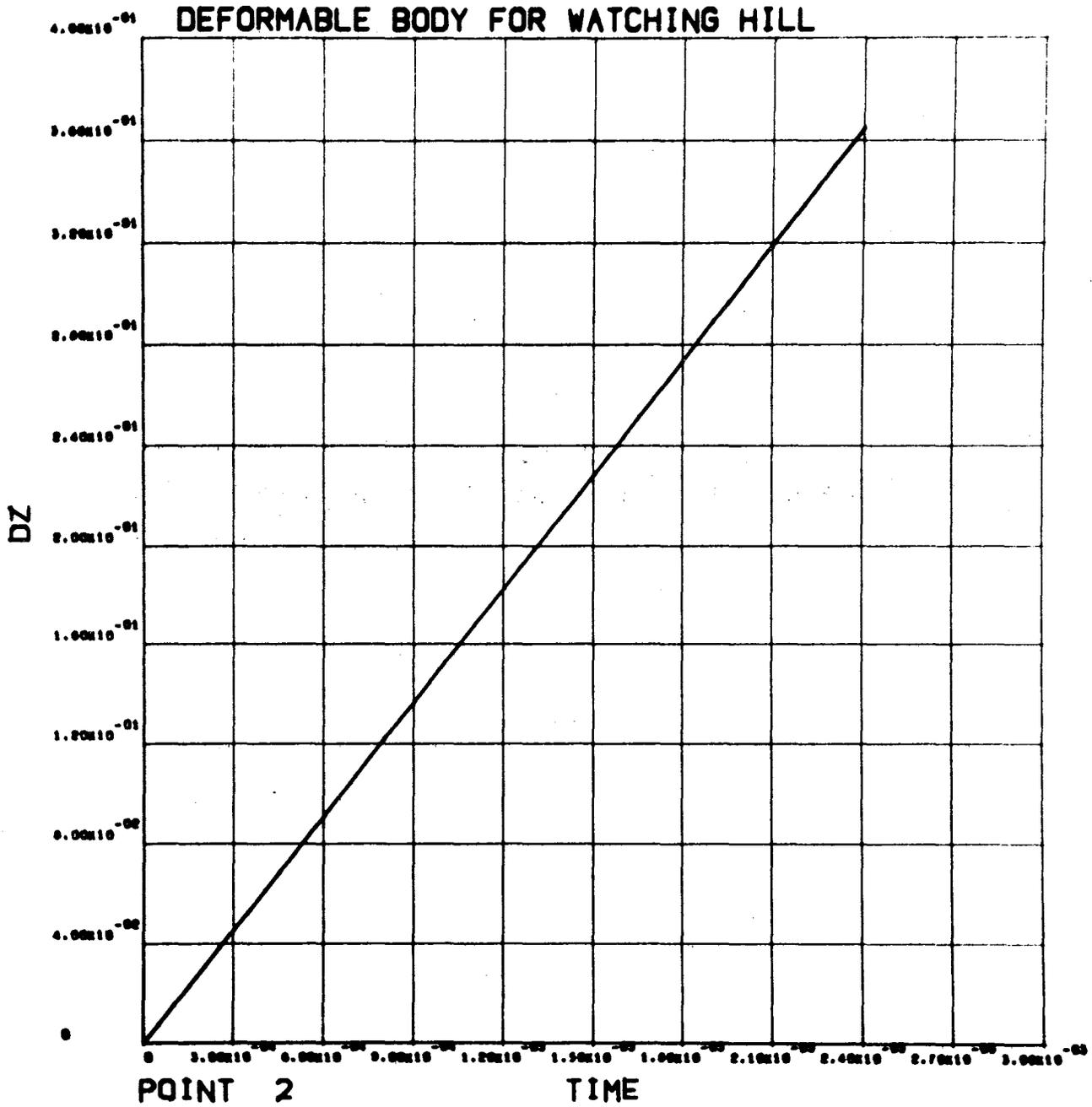


Figure B-27

Vertical displacement history (m) for point 2.0,58 m behind penetrator tip and 10 mm from central axis.

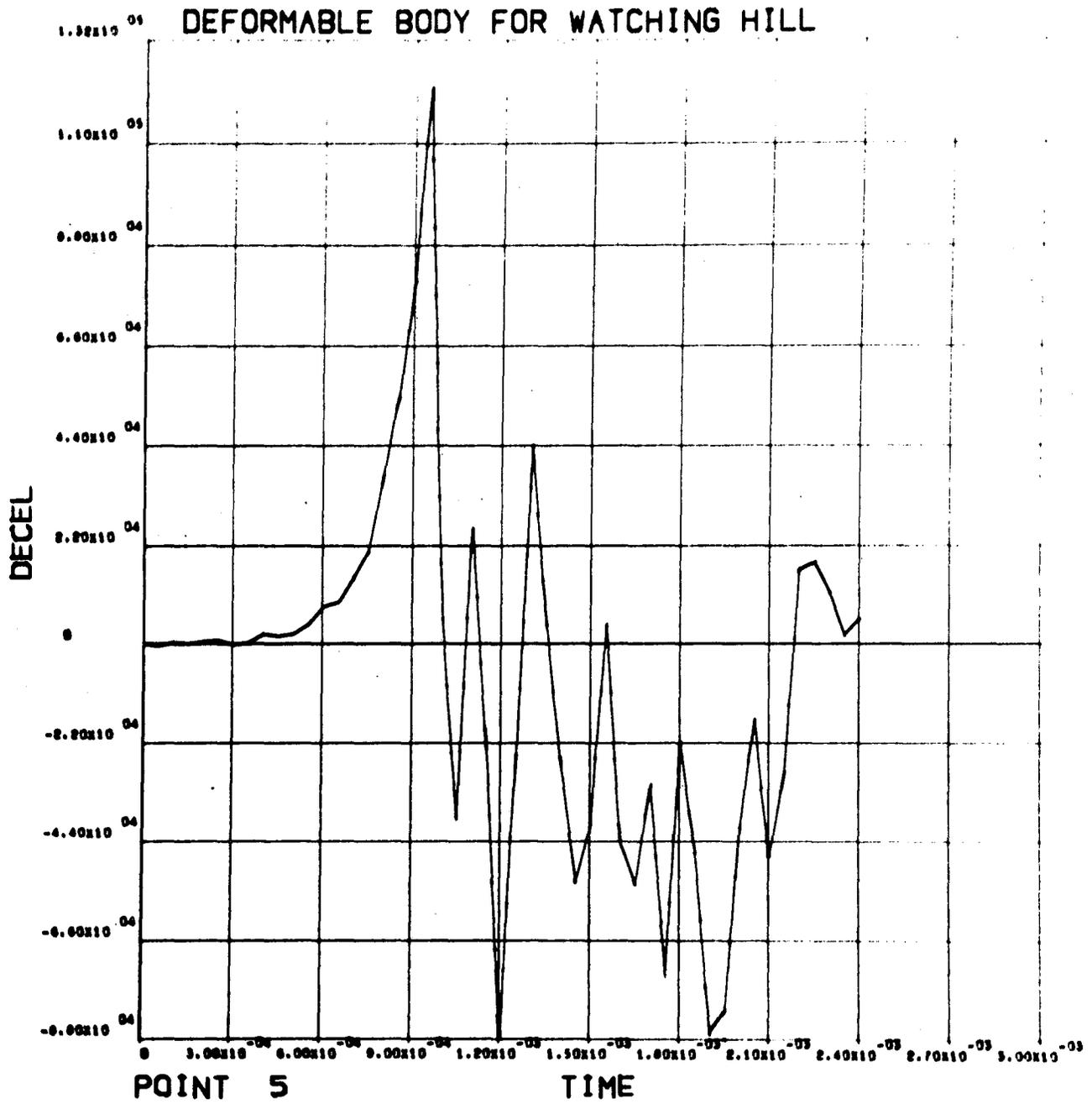


Figure B-28  
Deceleration history (g) for point 5, 28 mm behind penetrator tip and 6 mm from central axis.

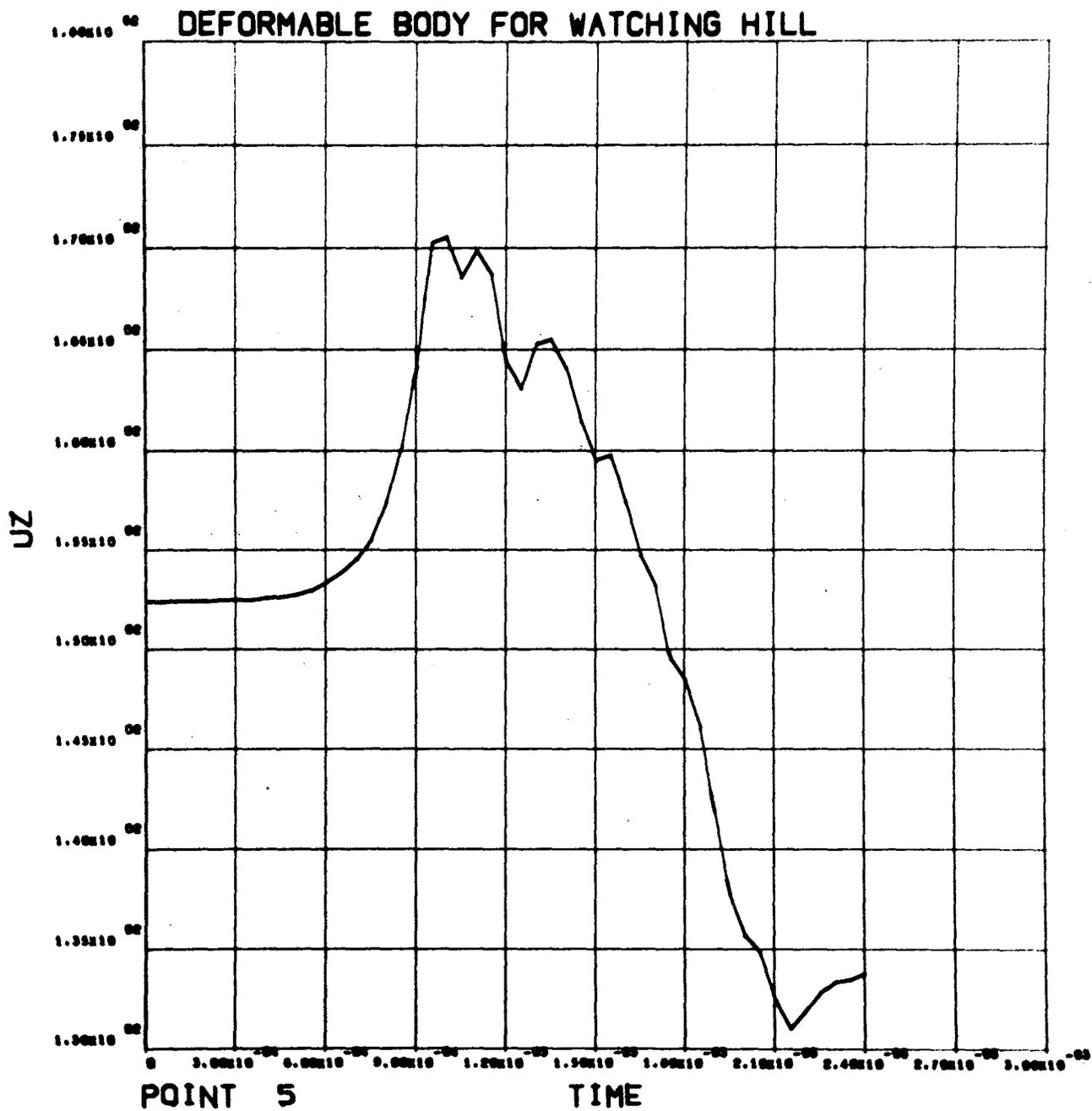


Figure B-29

Vertical velocity history (m/s) for point 5, 28 mm behind penetrator tip and 6 mm from central axis.

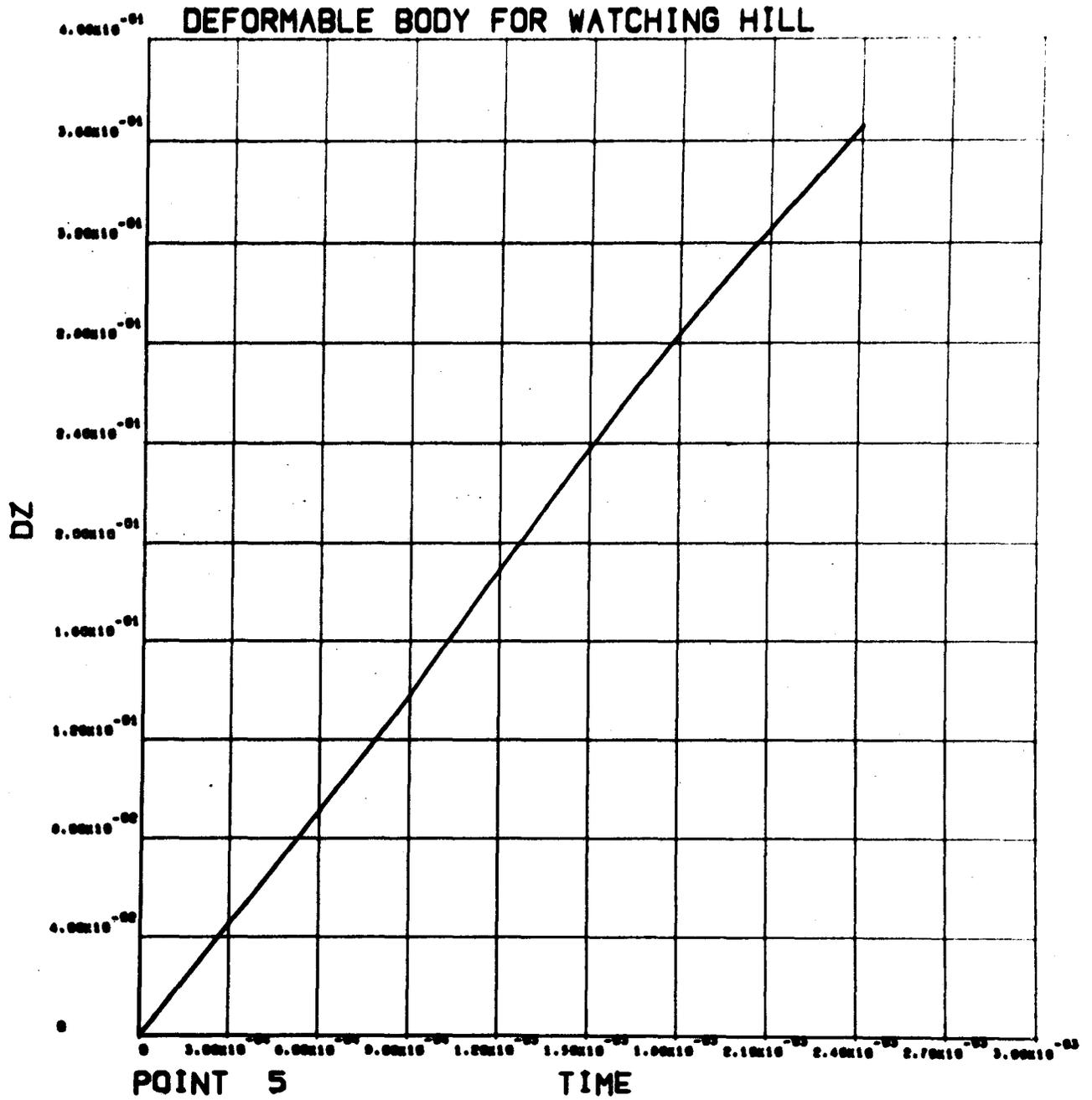


Figure B-30  
 Vertical displacement history (m) for point 5, 28 mm behind penetrator tip and 6 mm from central axis.

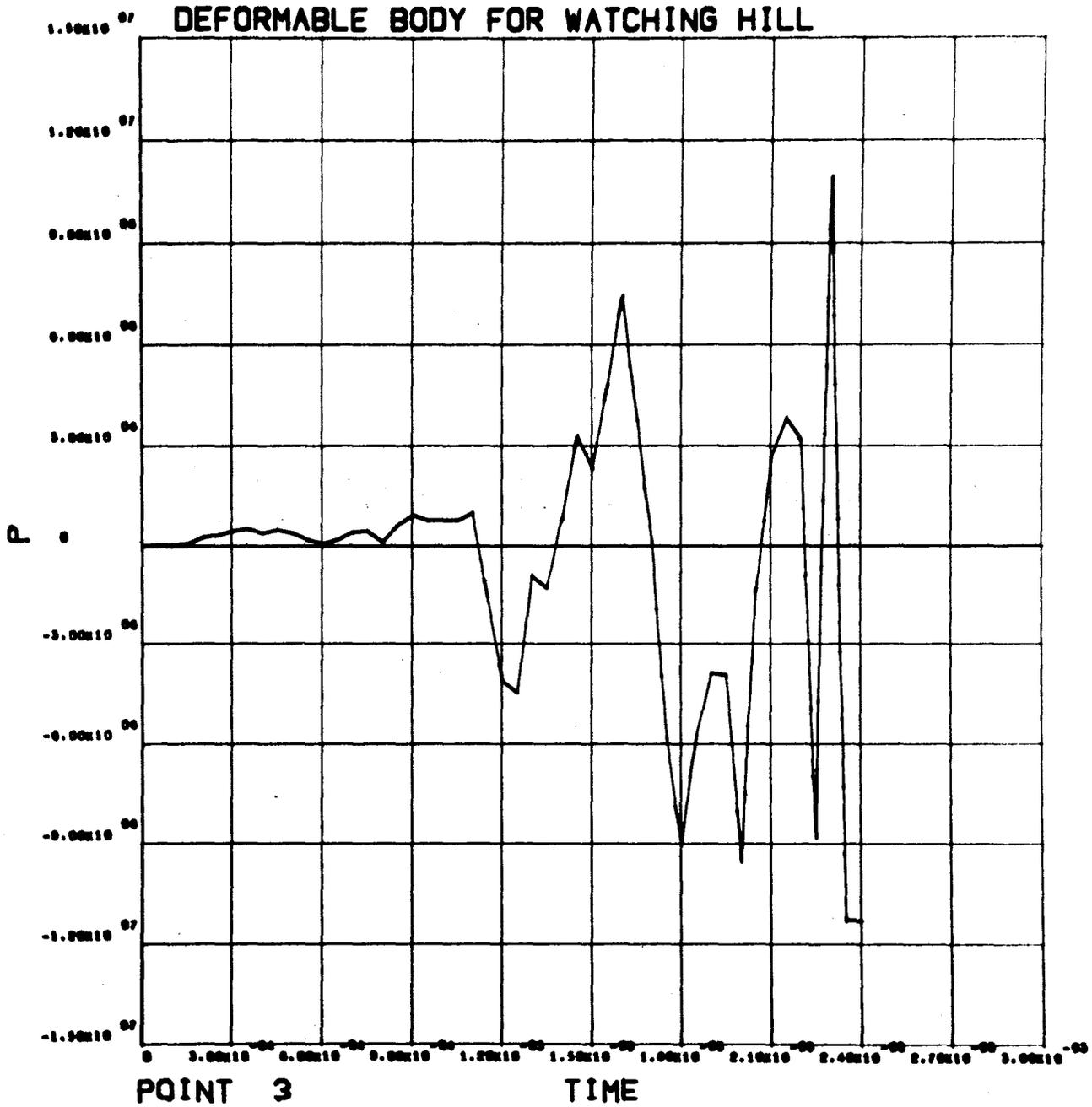


Figure B-31

Pressure history (Pa) for point 3, 0.79 m behind penetrator tip and 69 mm from central axis.

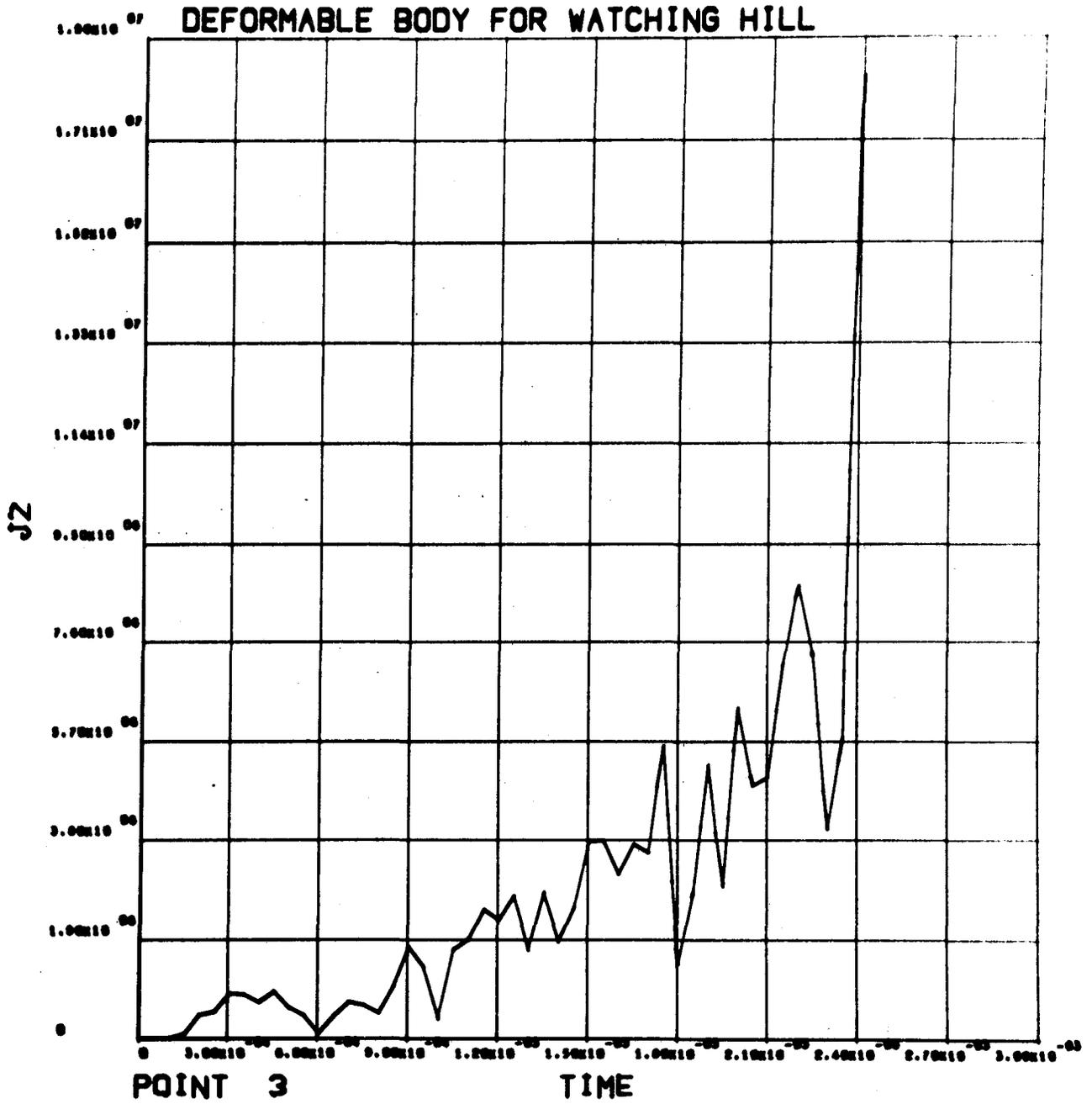


Figure B-32

Deviator stress, J2, history (Pa) for point 3, 0.79 m behind penetrator tip and 69 mm from central axis. (Octahedral shear stress =  $\sqrt{2/3}$  (J2)).

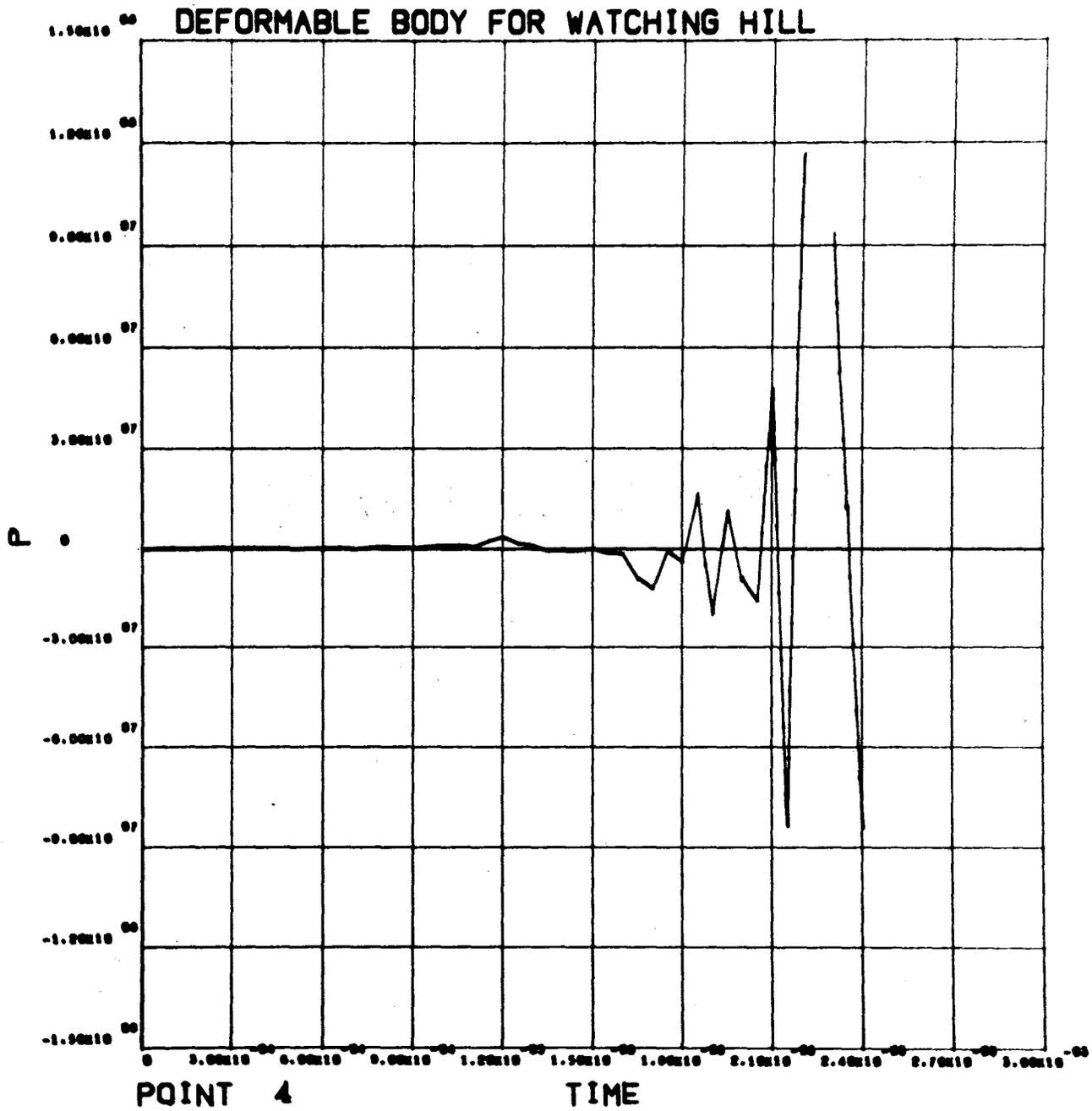


Figure B-33

Pressure history (Pa) for point 4, 1.39 m behind penetrator tip and 69 mm from central axis.

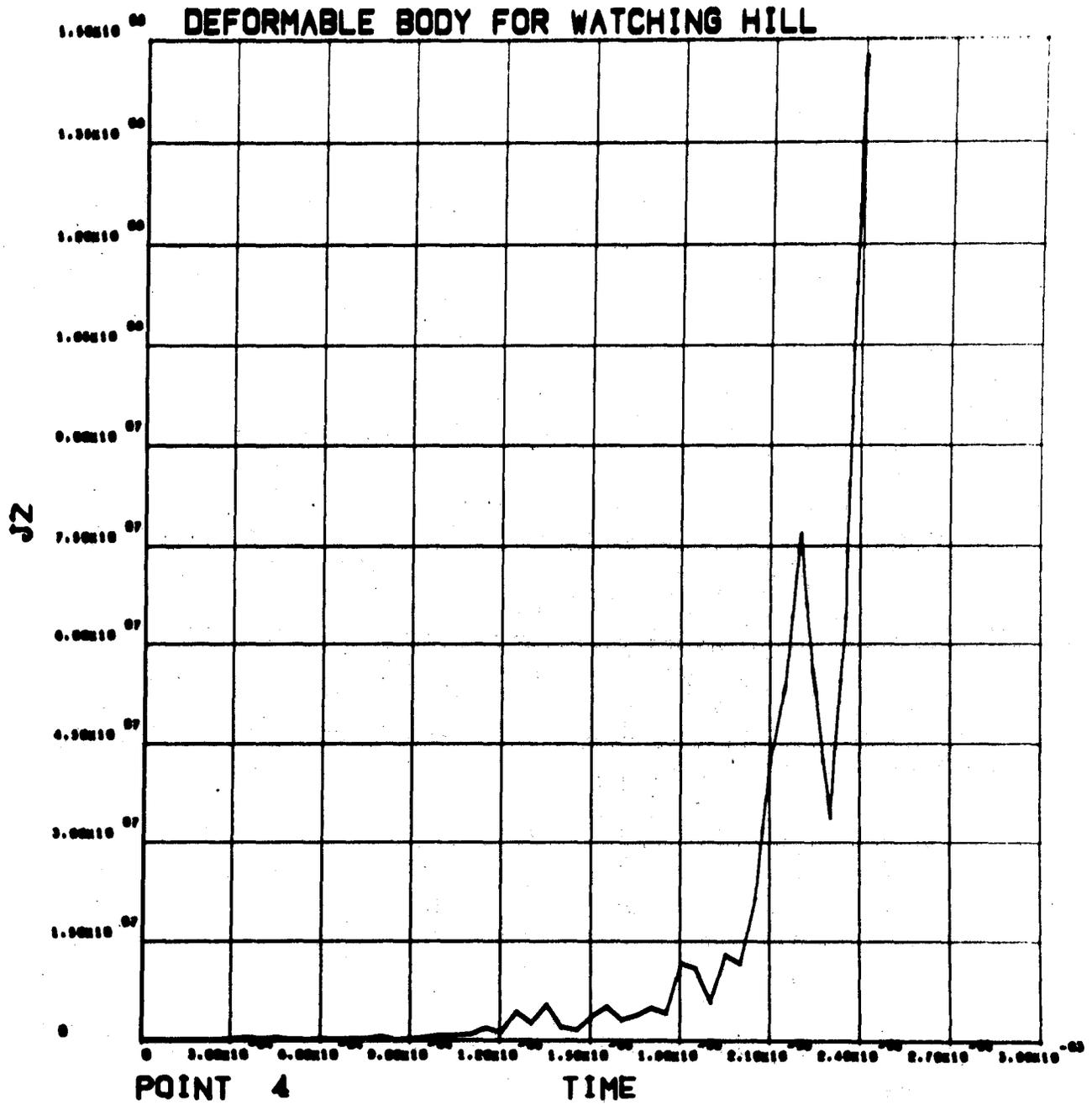


Figure B-34

Deviator stress, J2, history (Pa) for point 4, 1.39 m behind penetrator tip and 69 mm. from central axis. (Octahedral shear stress =  $\sqrt{2/3}$  (J2)).

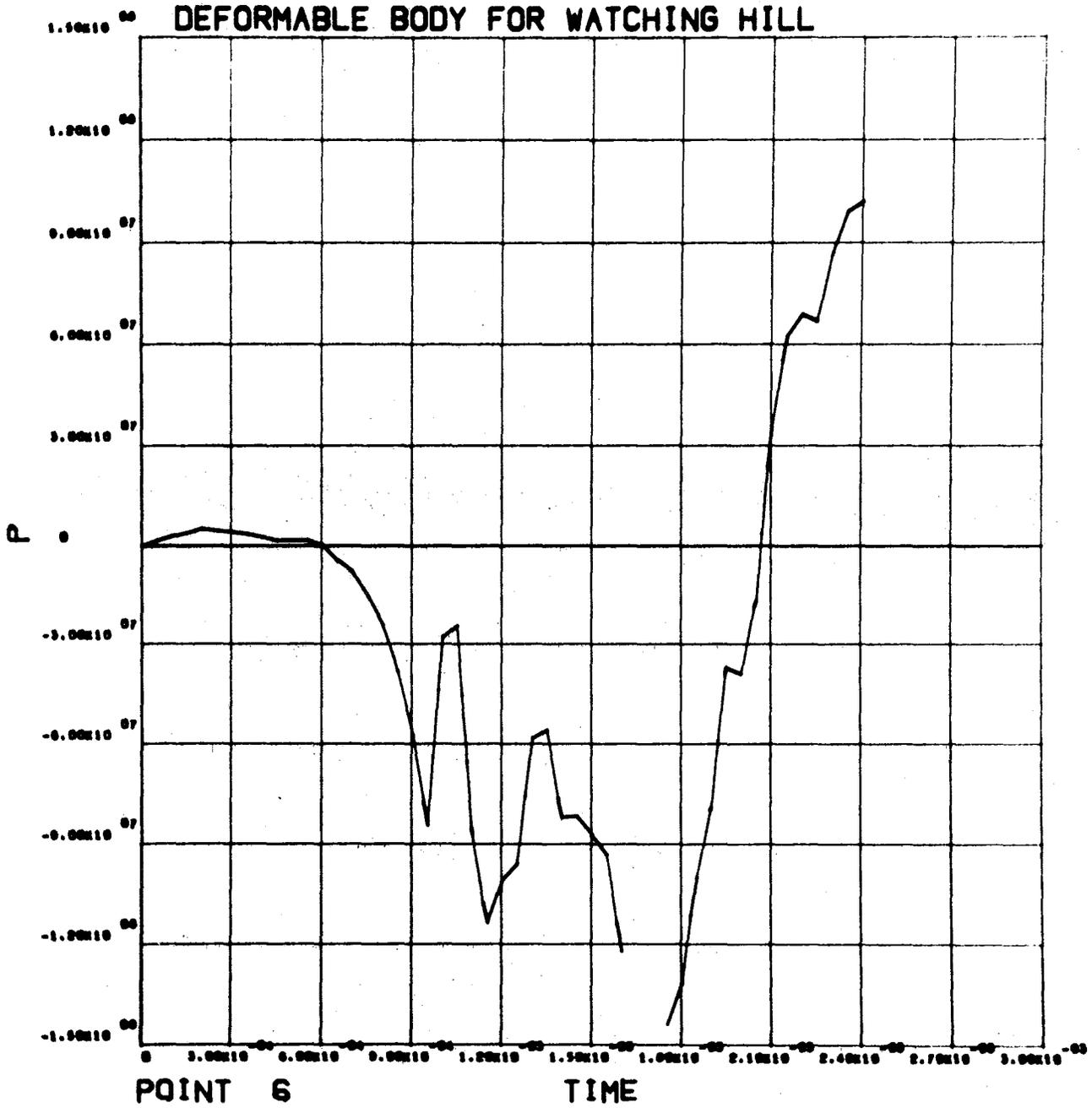


Figure B-35

Pressure history (Pa) for point 6, 48 mm behind penetrator tip and 17 mm from central axis.

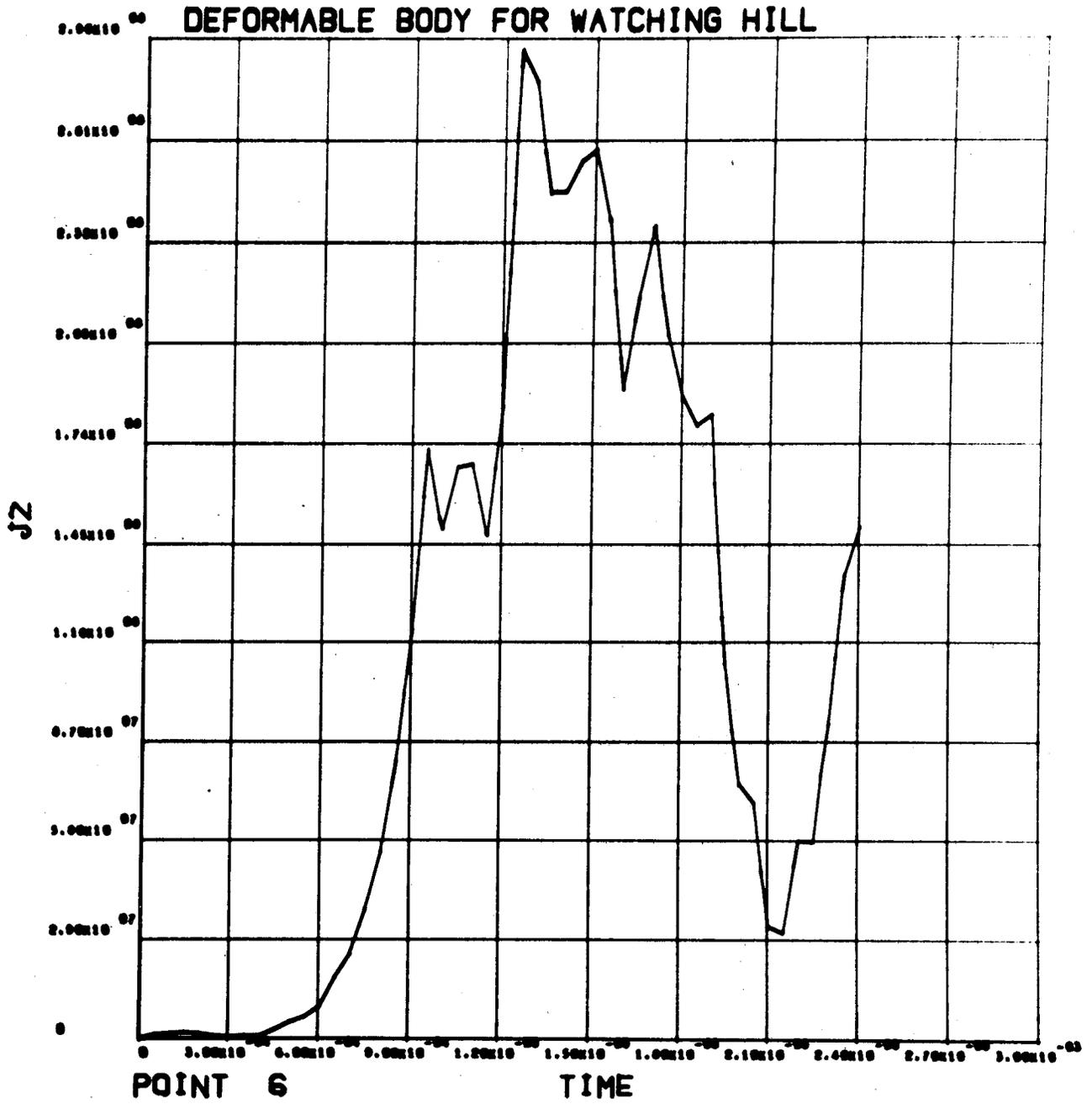


Figure B-36

Deviator stress,  $J_2$ , history (Pa) for point 6, 48 mm behind penetrator tip and 17 mm from central axis. (Octahedral shear stress =  $\sqrt{2/3} (J_2)$ ).

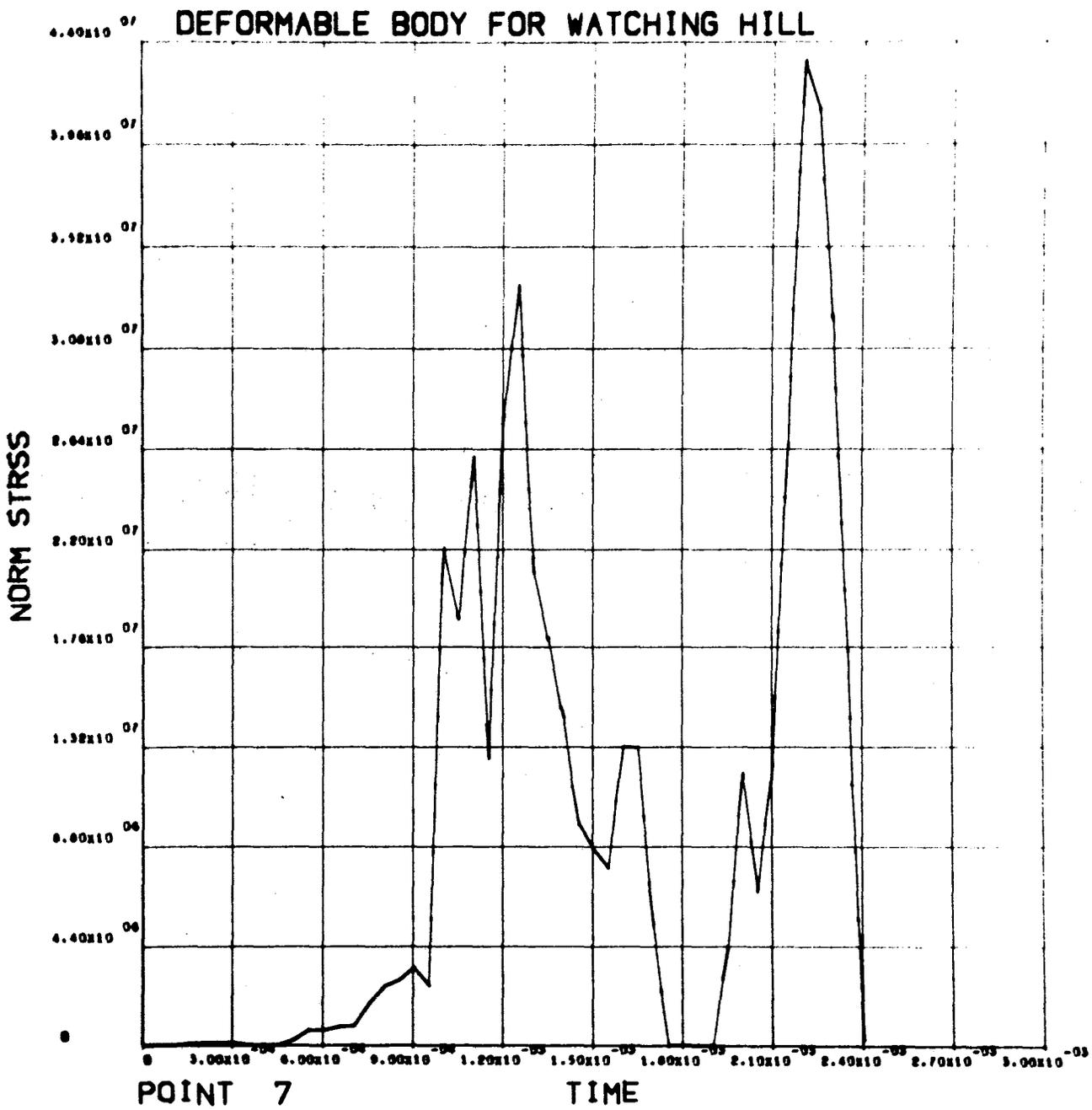


Figure B-37

Normal stress history (Pa) for point 7, 0.14 m behind penetrator tip and 41 mm from central axis.

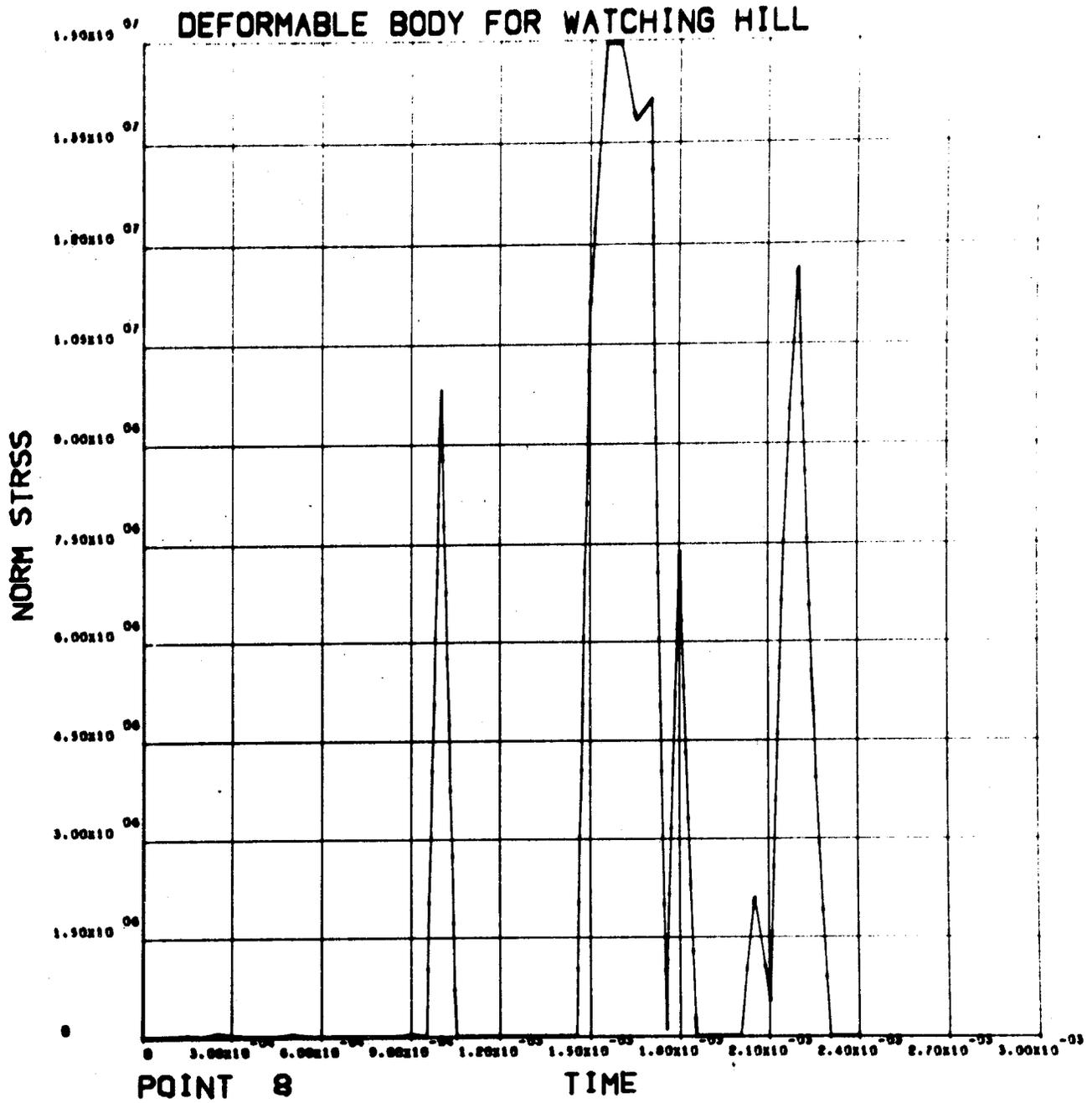


Figure B-38

Normal stress history (Pa) for point 8.0.23 m behind penetrator tip and 60 mm from central axis.

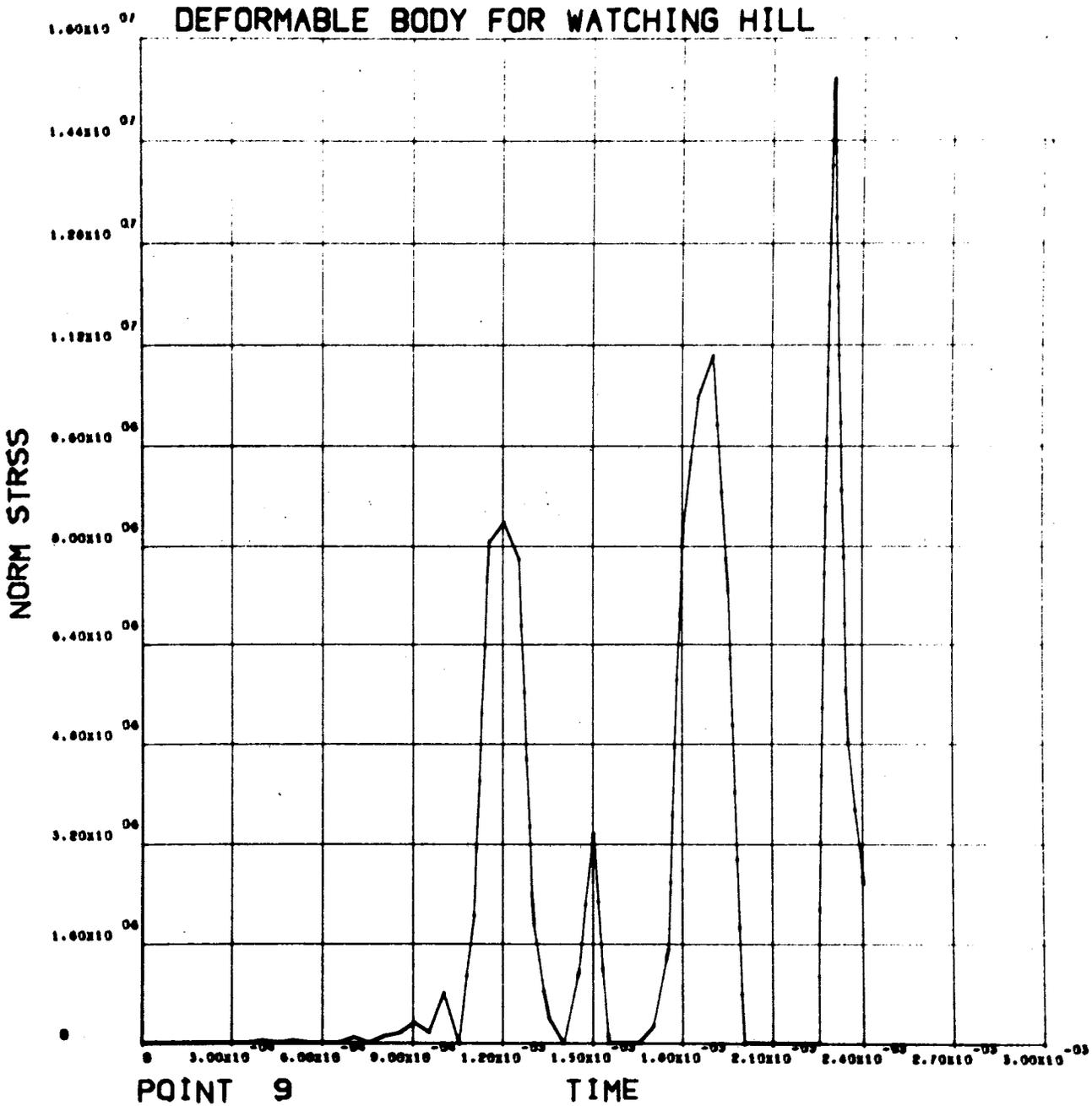


Figure B-39

Normal stress history (Pa) for point 9, 0.38 m behind penetrator tip and 77 mm from central axis.

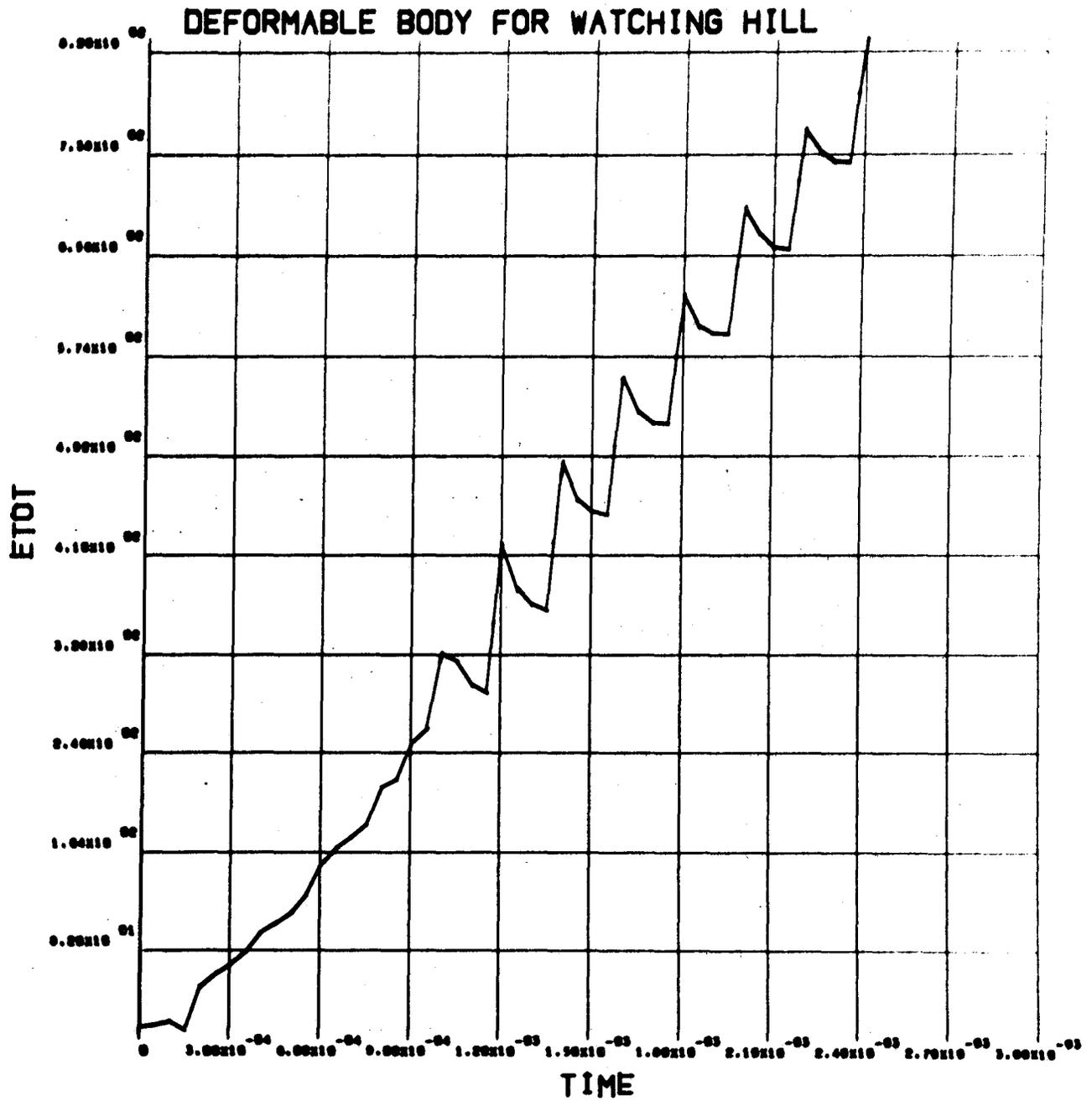


Figure B-40  
Soil kinetic energy 1 radian vs time (deformable penetrator).

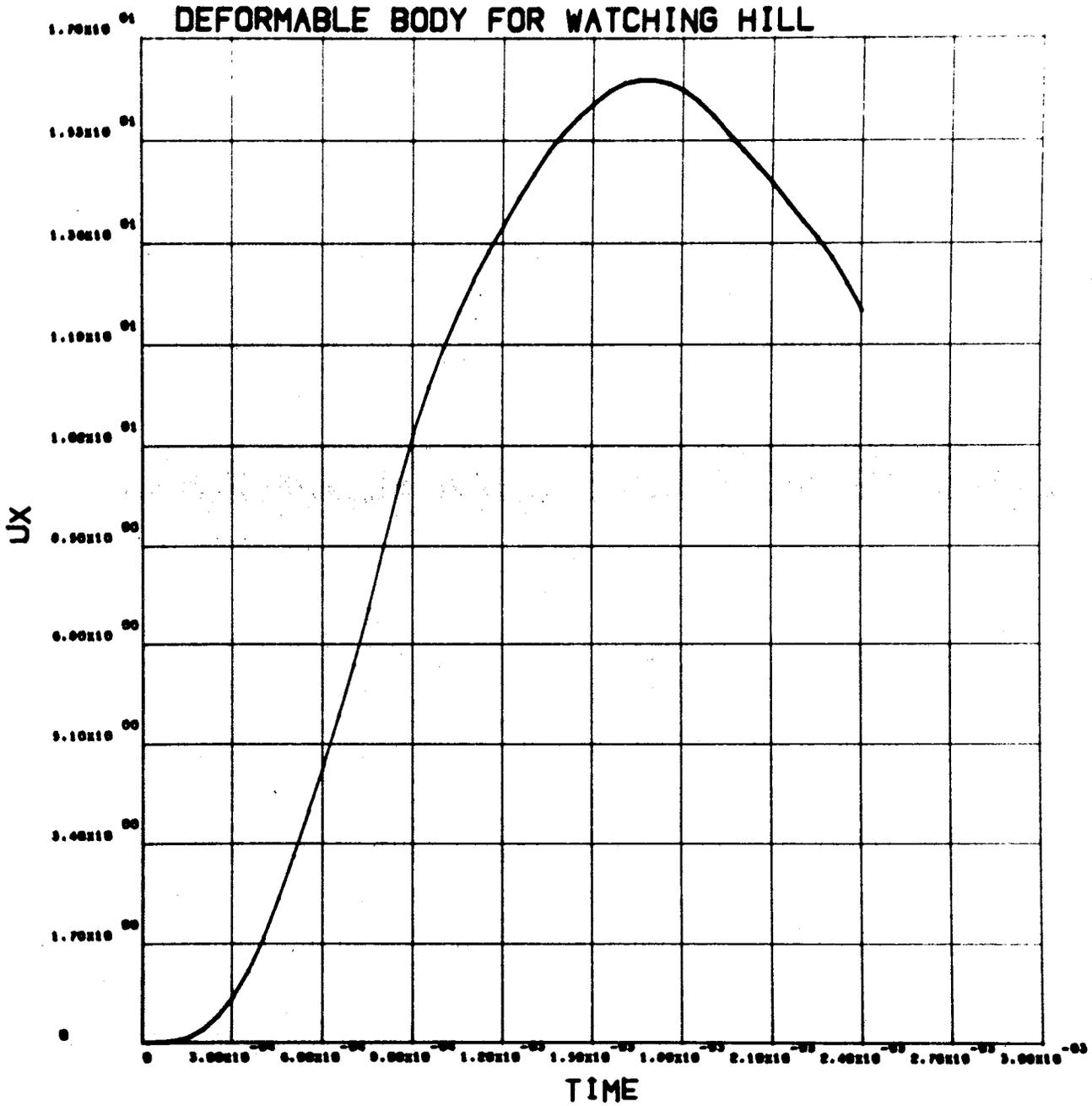


Figure B-41

Radial velocity history (m/s) in soil at range 75 mm, depth 0.1 m (deformable penetrator).

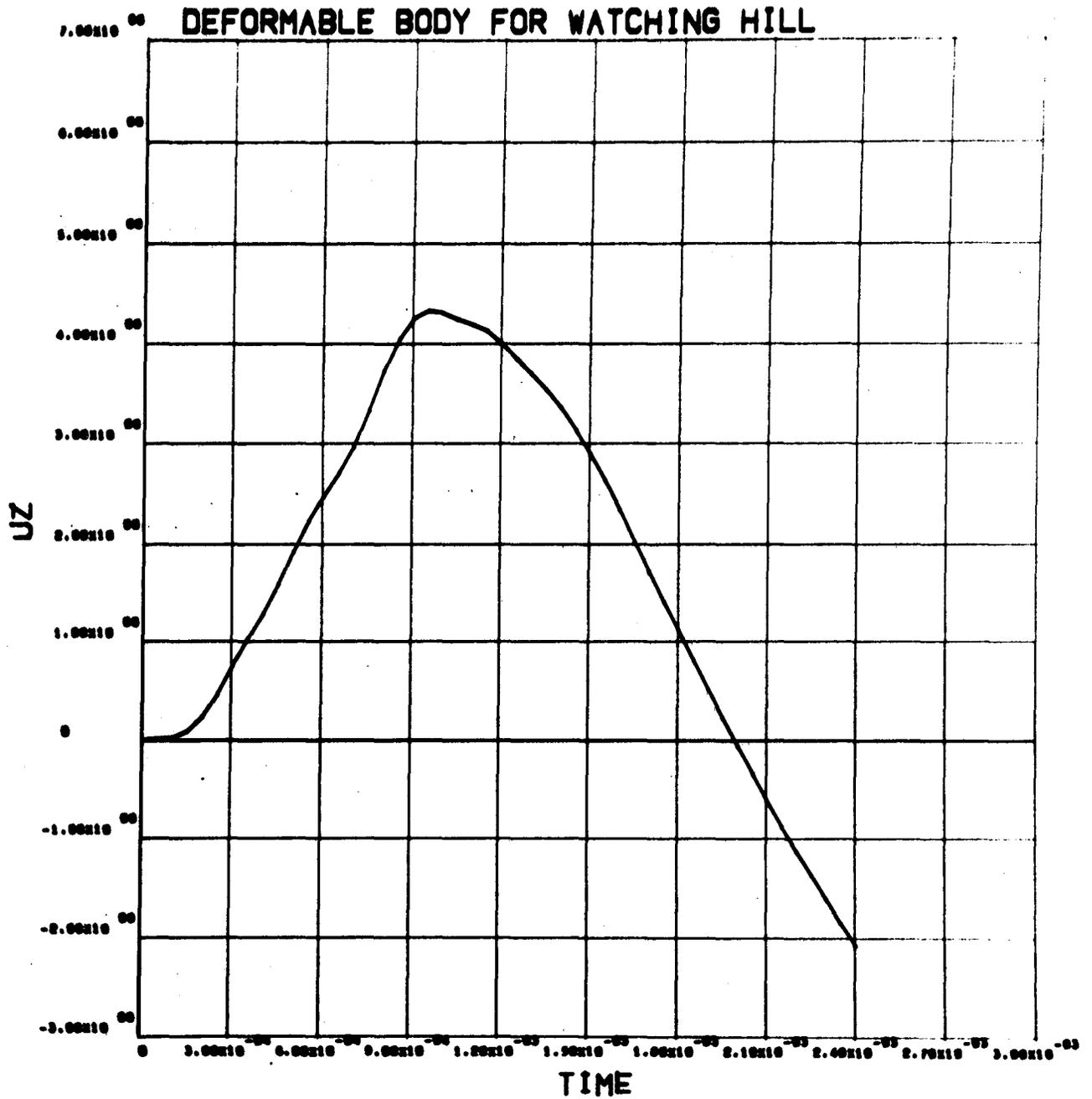


Figure B-42

Vertical velocity history (m/s) in soil at range 75 mm, depth 0.1 m (deformable penetrator).

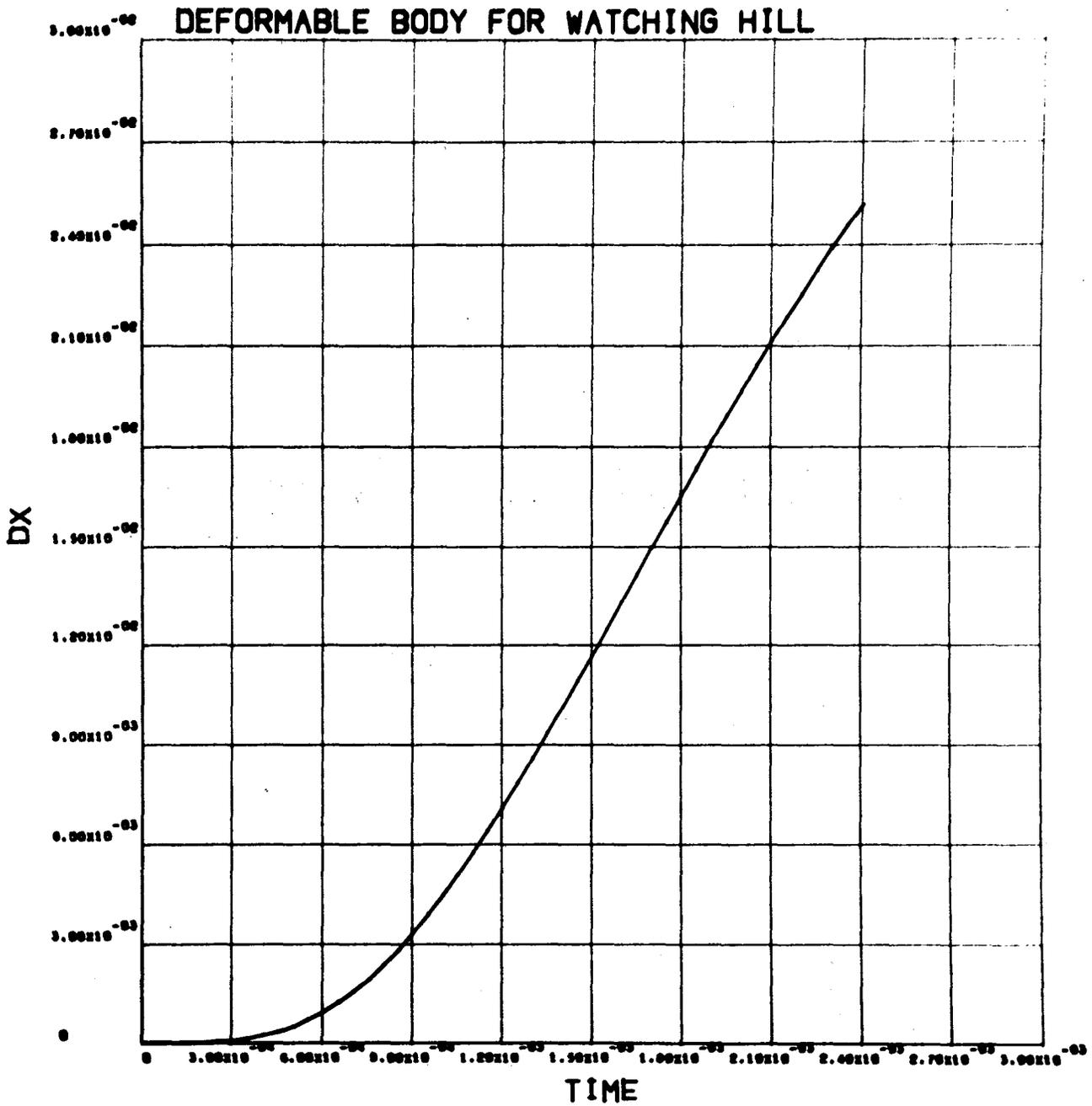


Figure B-43

Radial displacement history (m) in soil at range 75 mm, depth 0.1 m (deformable penetrator).

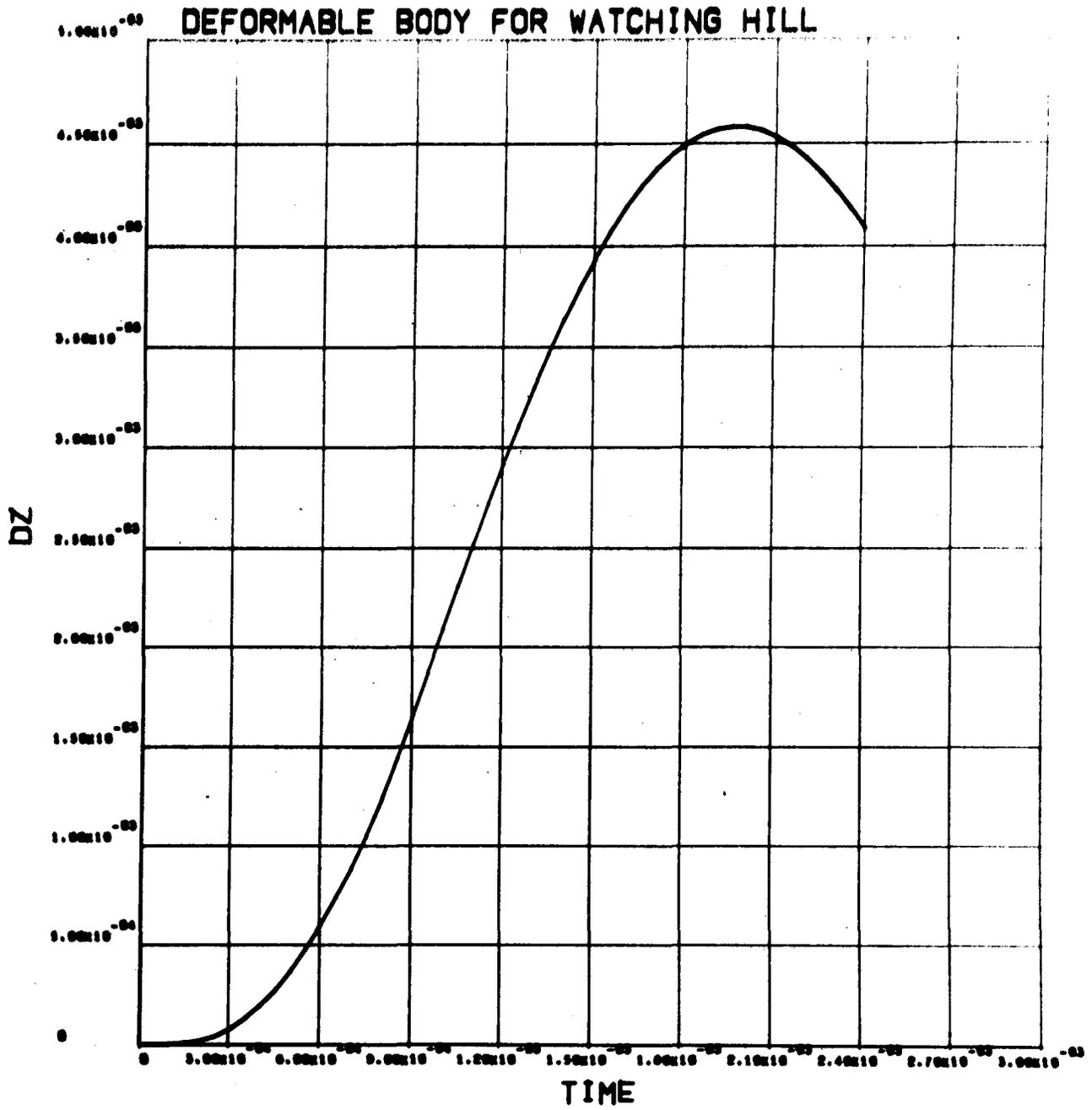


Figure B-44  
 Vertical displacement history (m) in soil at range 75 mm, depth 0.1 m (deformable penetrator).

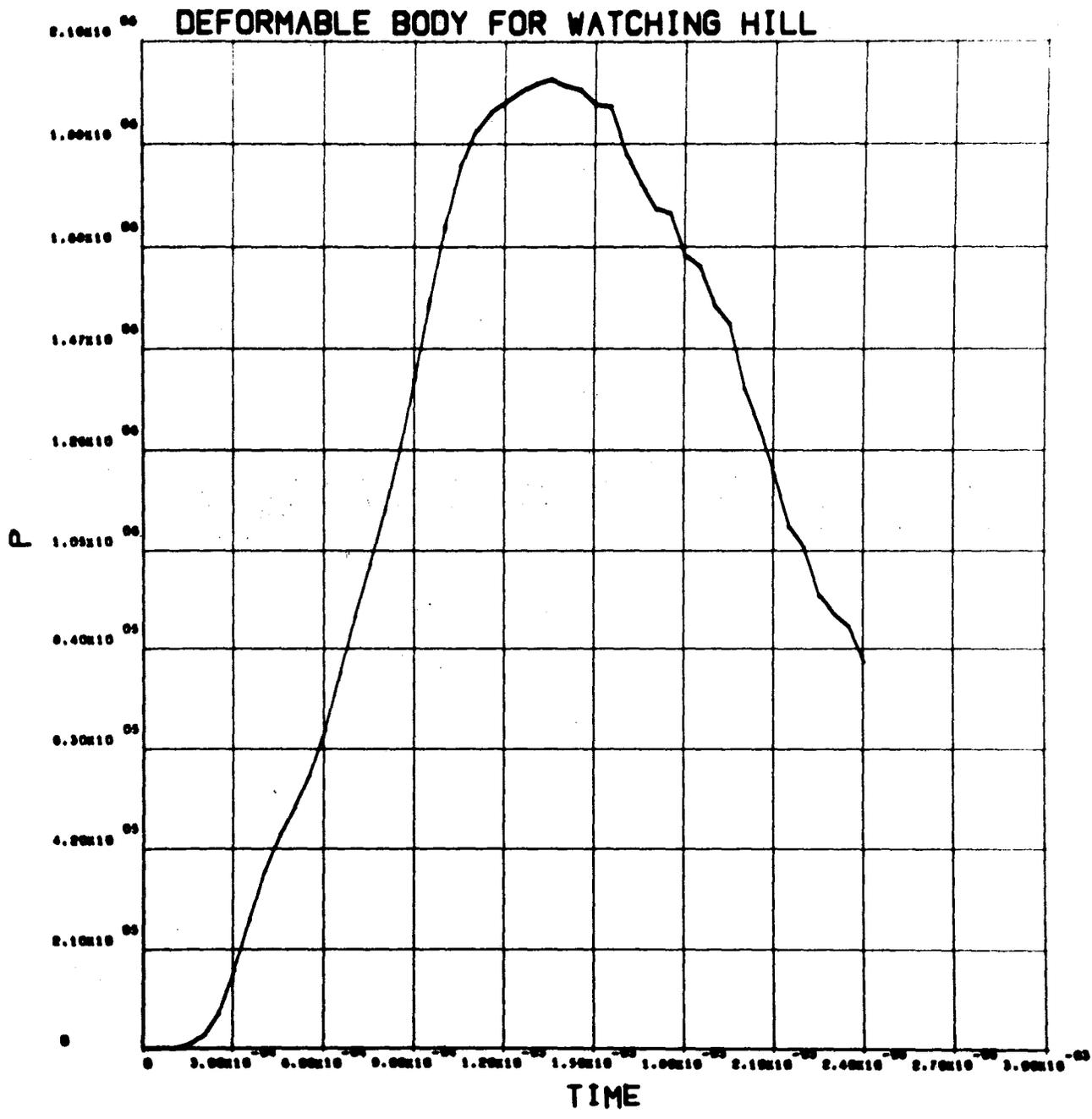


Figure B-45  
 Pressure history (Pa) in soil at range 75 mm, depth 0.1 m (deformable penetrator).

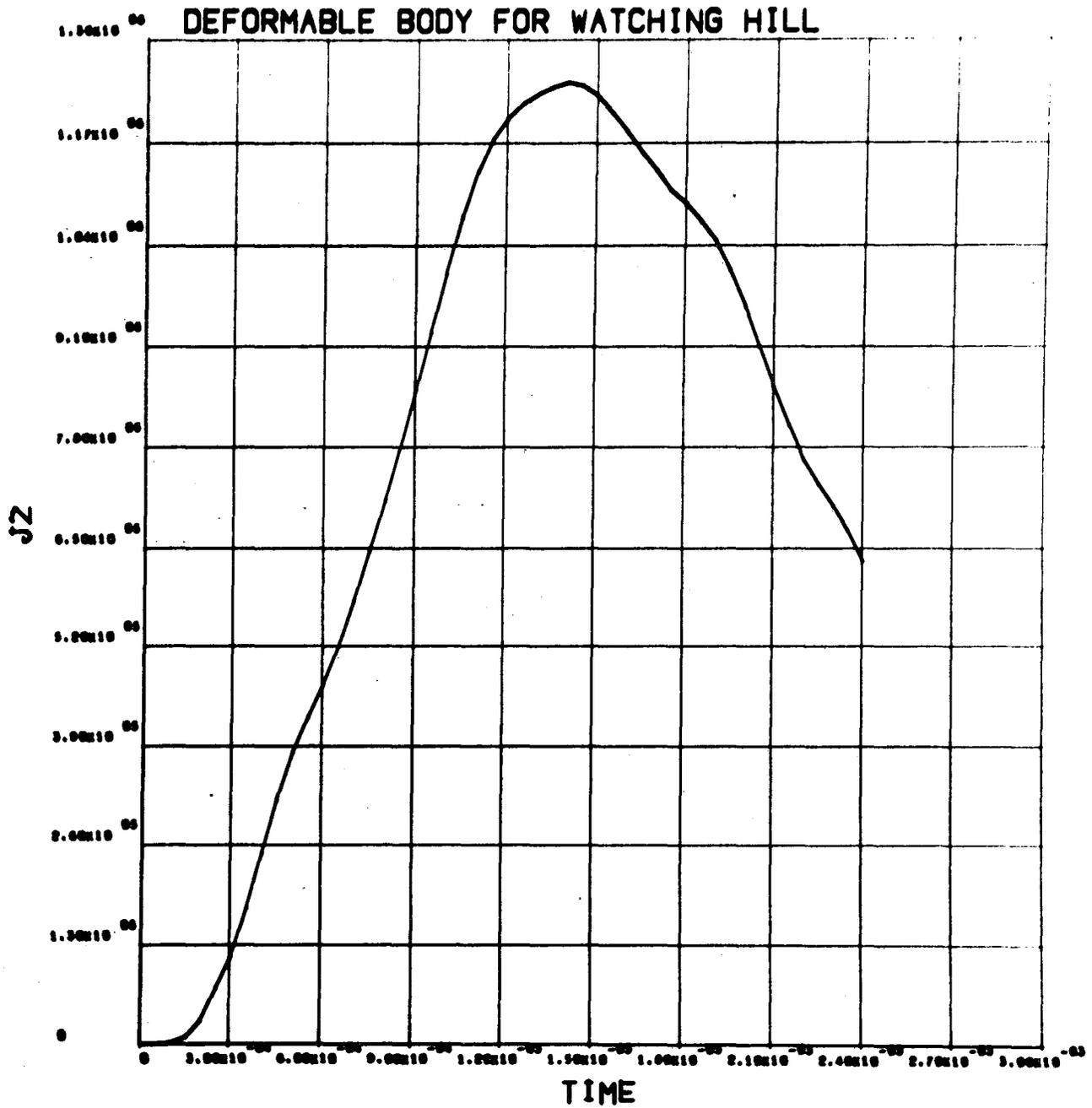


Figure B-46

Deviator stress,  $J_2$ , history (Pa) in soil at range 75 mm, depth 0.1 m (deformable penetrator), (octahedral shear stress =  $\sqrt{2/3} (J_2)$ ).

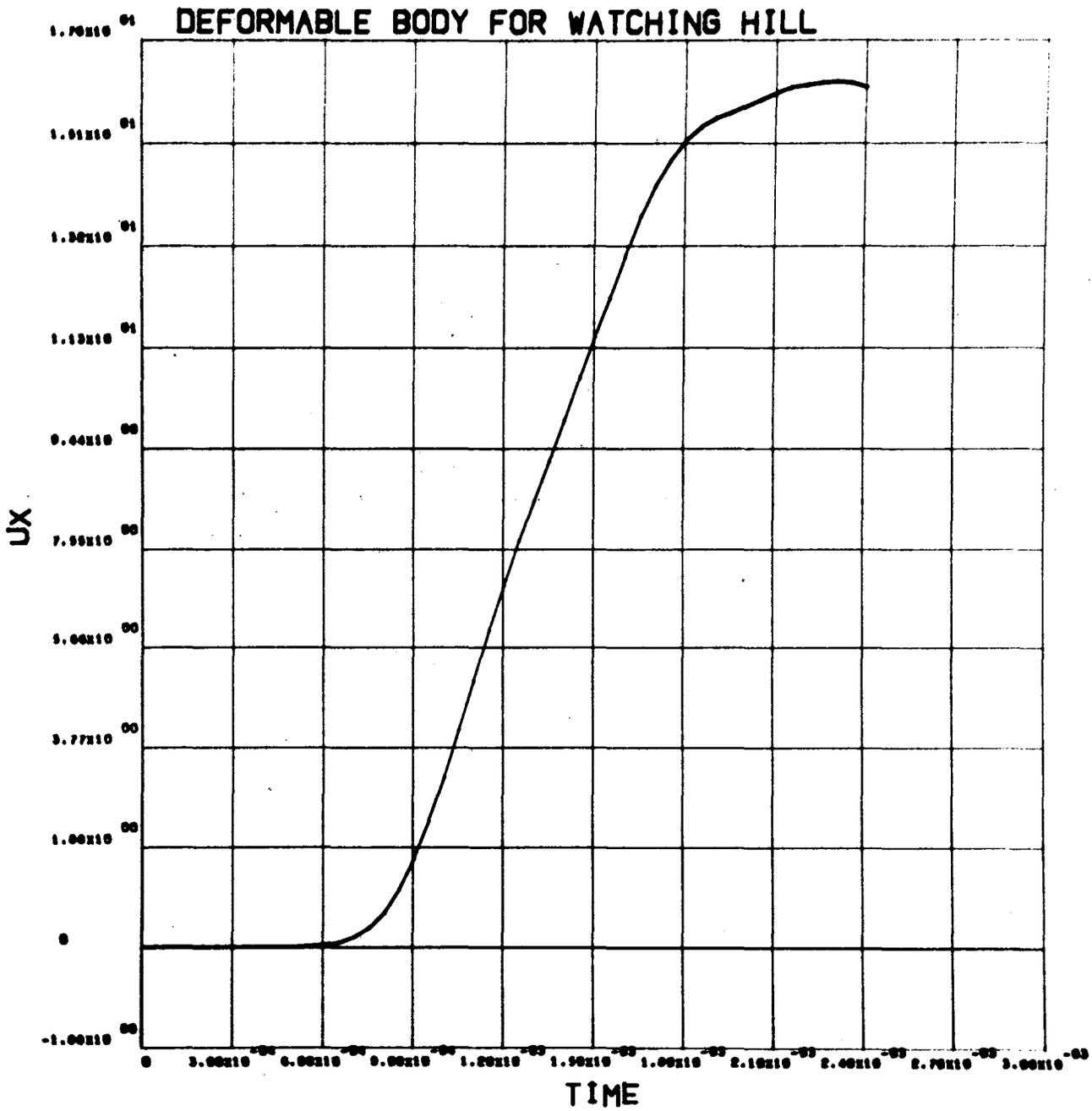


Figure B-47  
 Radial velocity history (m/s) in soil at range 75 mm, depth 0.2 m (deformable penetrator).

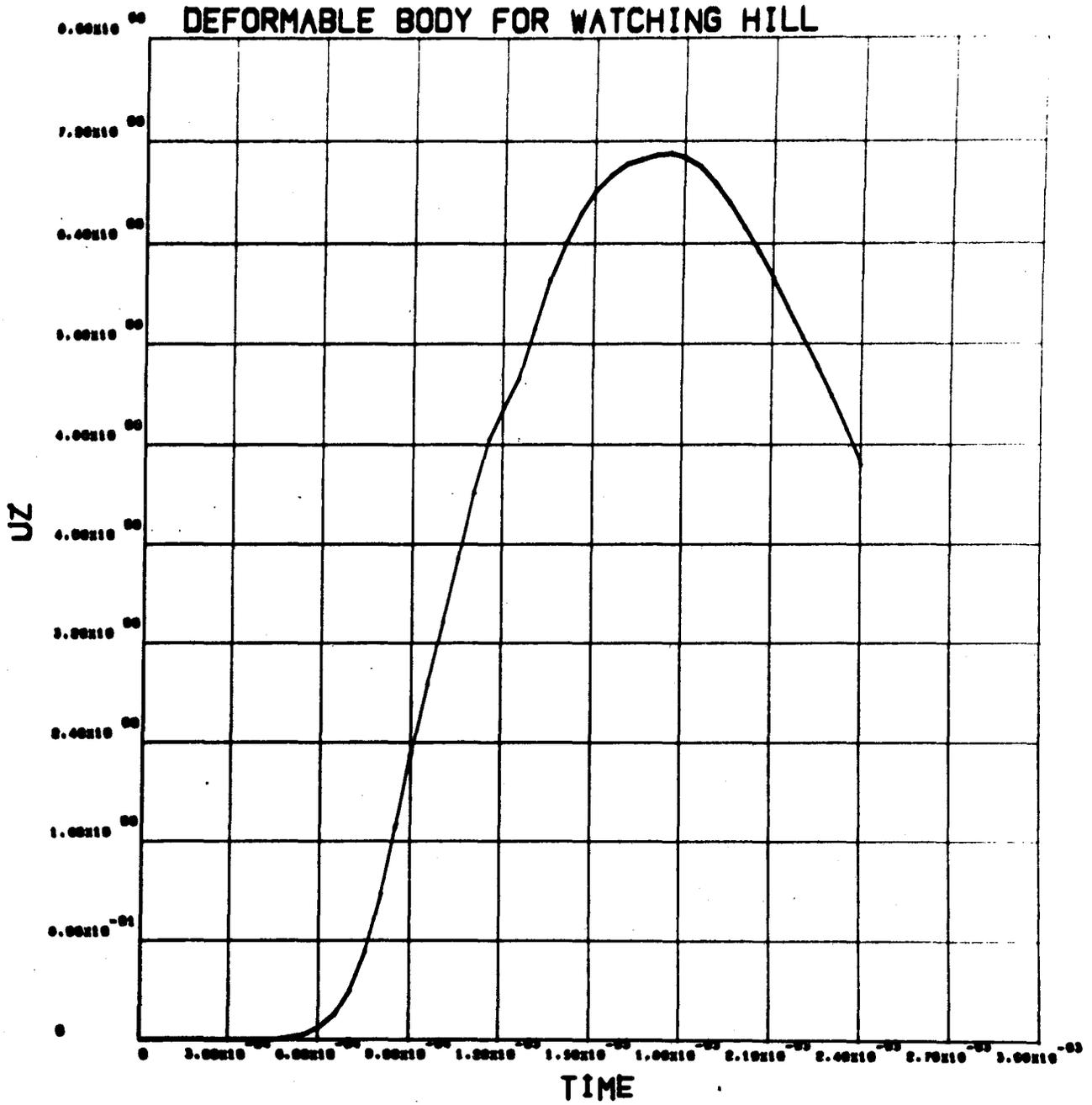


Figure B-48  
 Vertical velocity history (m/s) in soil at range 75 mm, depth 0.2 m (deformable penetrator).

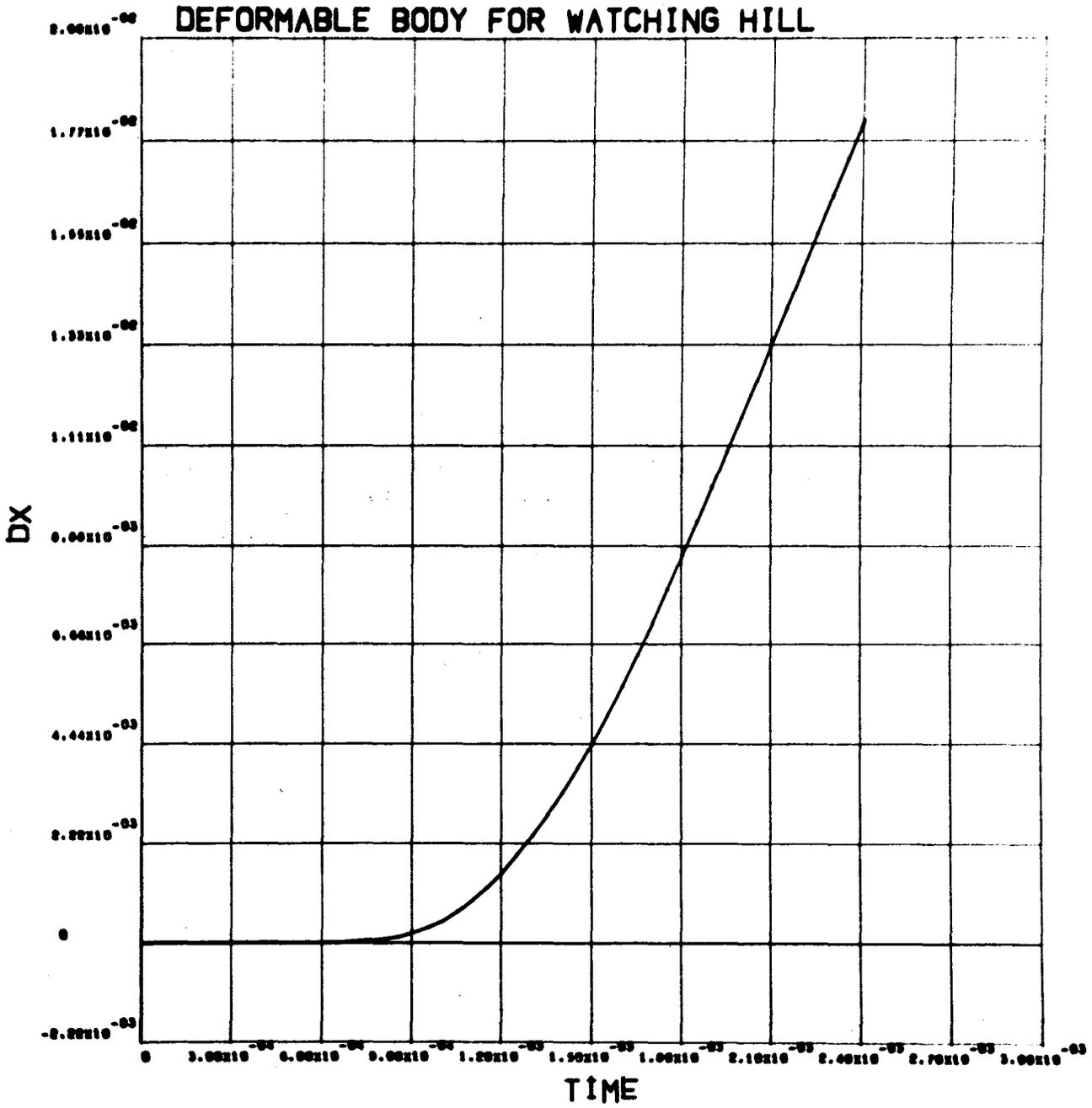


Figure B-49

Radial displacement history (m) in soil at range 75 mm, depth 0.2 m (deformable penetrator).

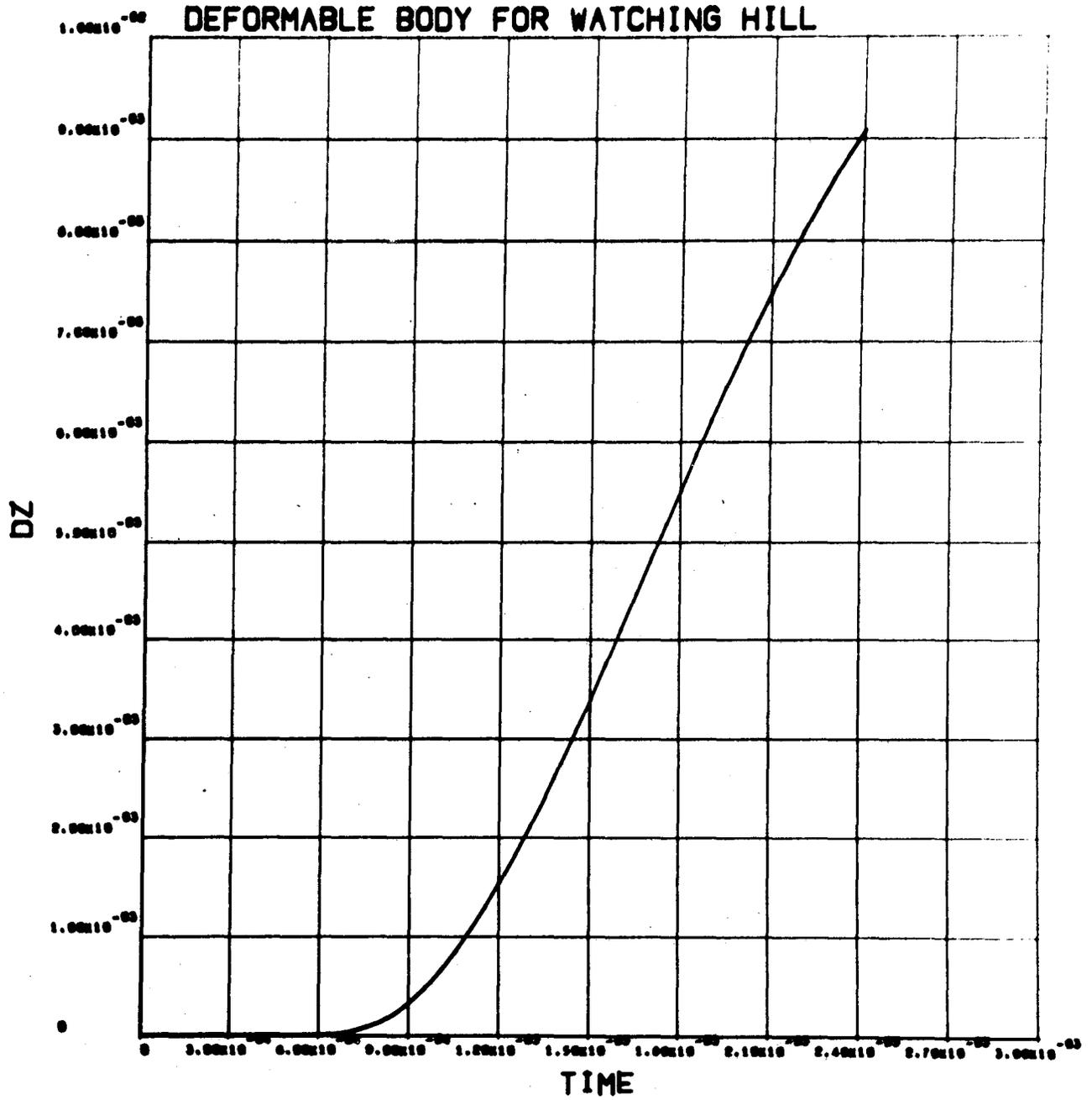


Figure B-50  
 Vertical displacement history (m) in soil at range 75 mm, depth 0.2 m (deformable  
 penetrator).

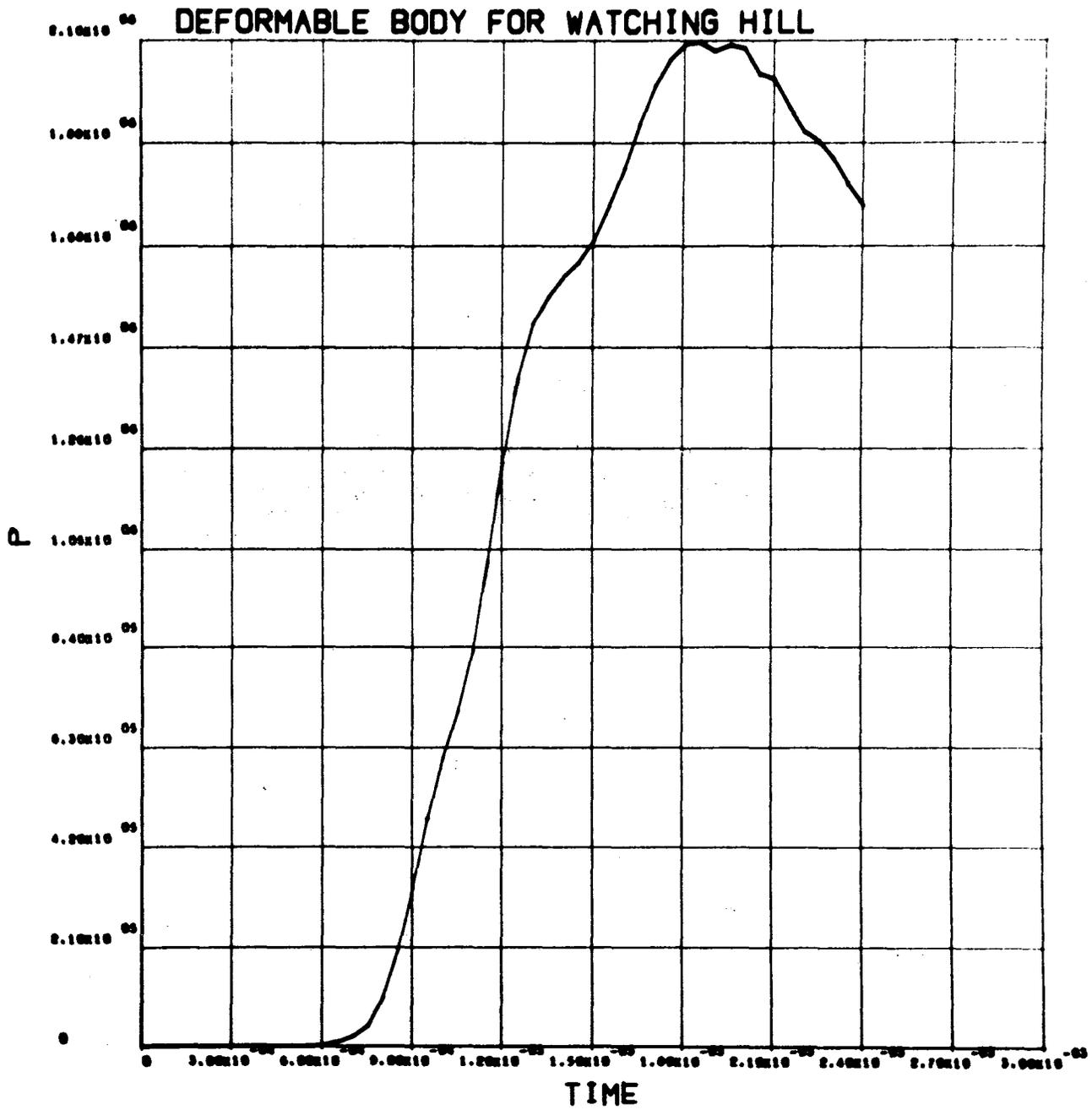


Figure B-51  
 Pressure history (Pa) in soil at range 75 mm, depth 0.2 (deformable penetrator).

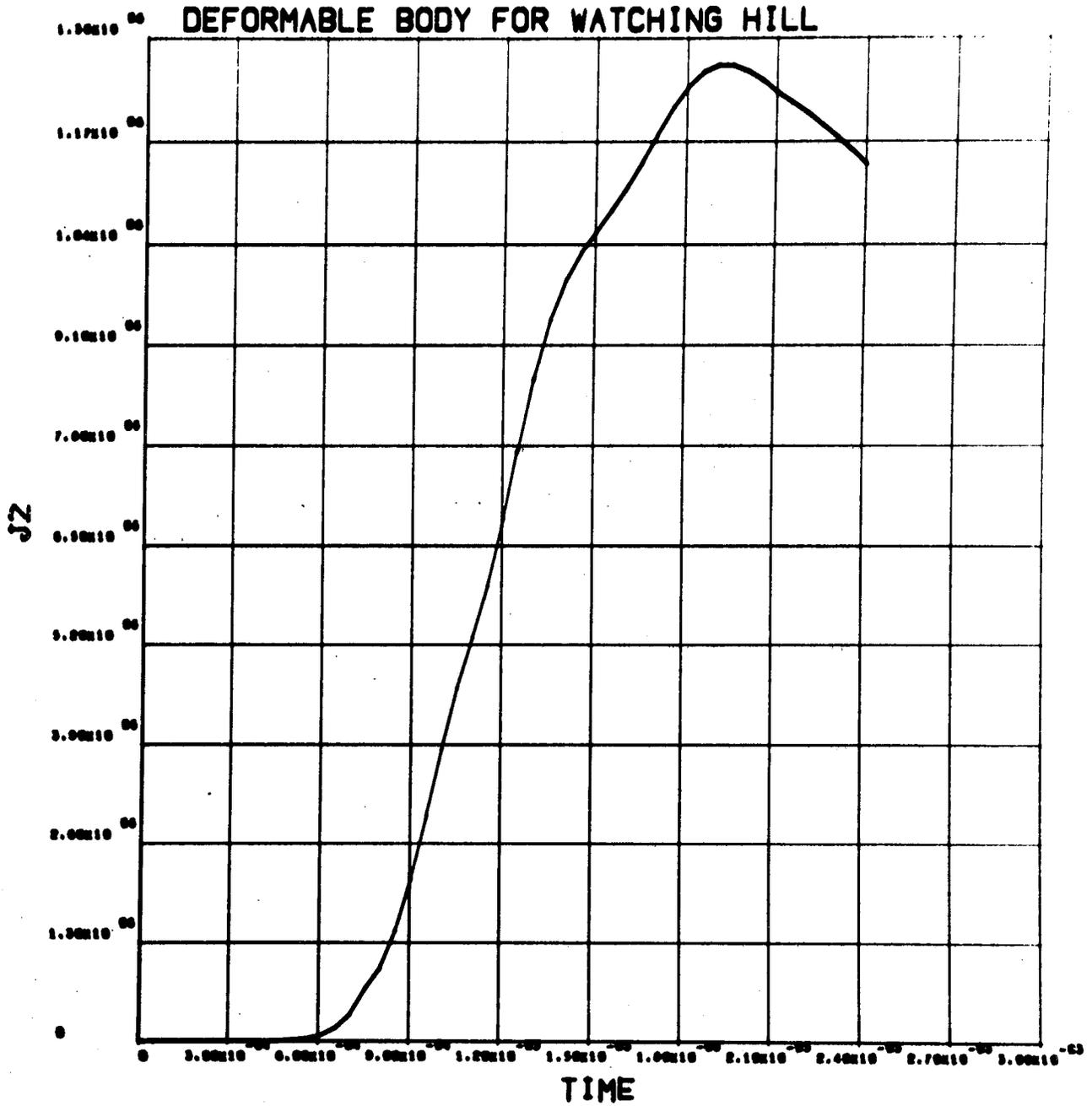


Figure B-52  
 Deviator stress, J2, history (Pa) in soil at range 75 mm, depth 0.2 m (deformable penetrator).

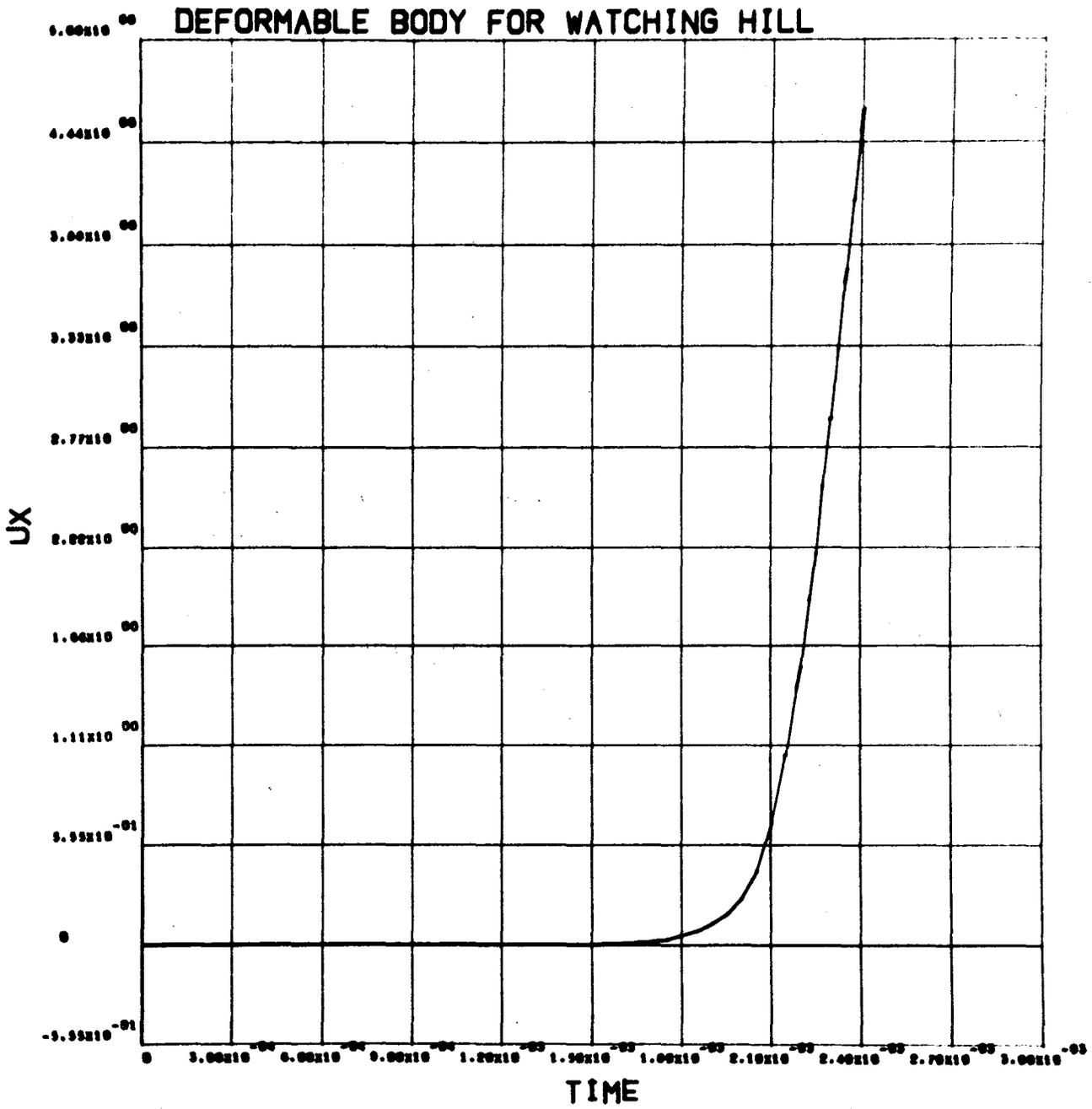


Figure B-53

Radial velocity history (m/s) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

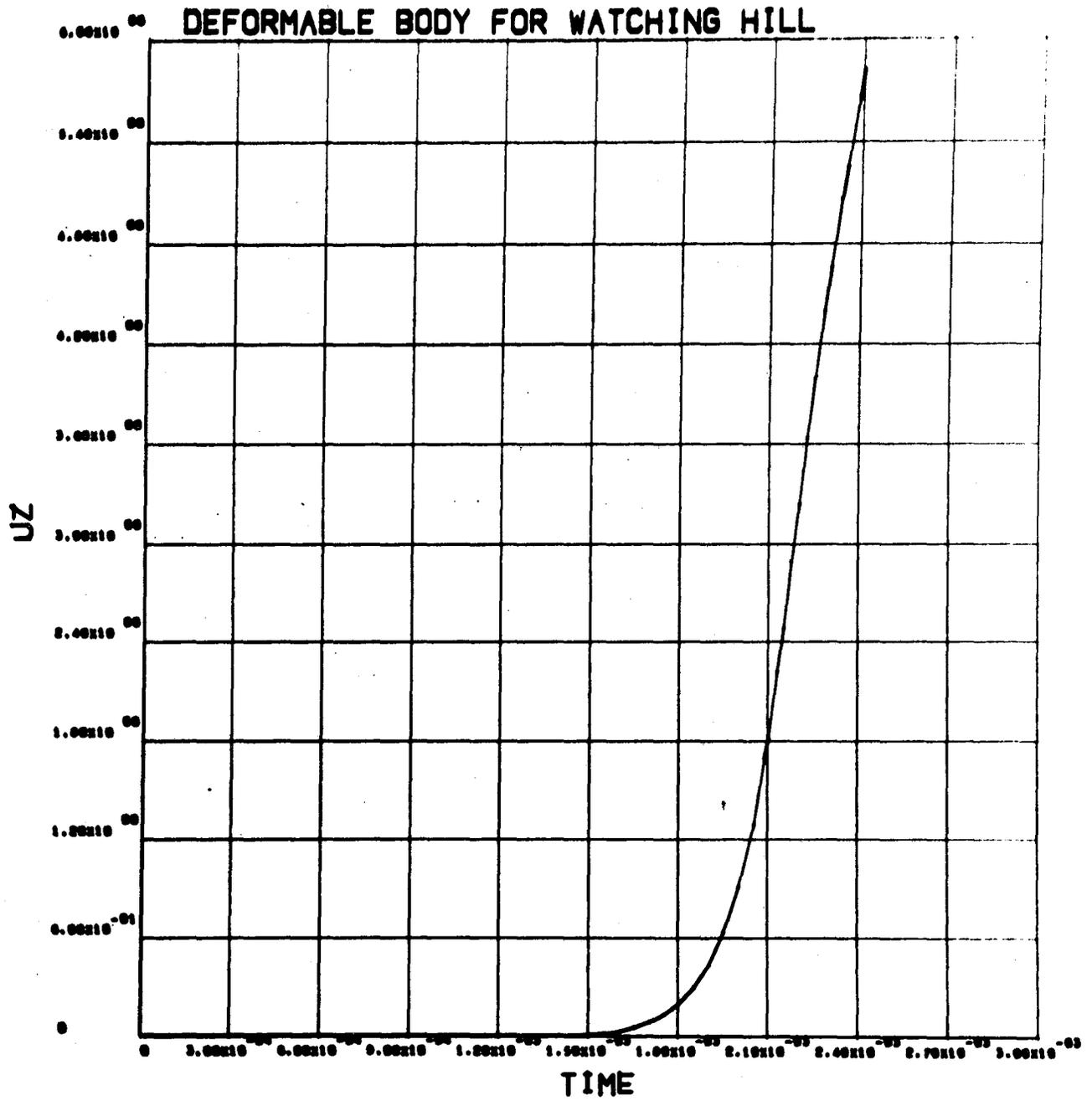


Figure B-54  
 Vertical velocity history (m/s) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

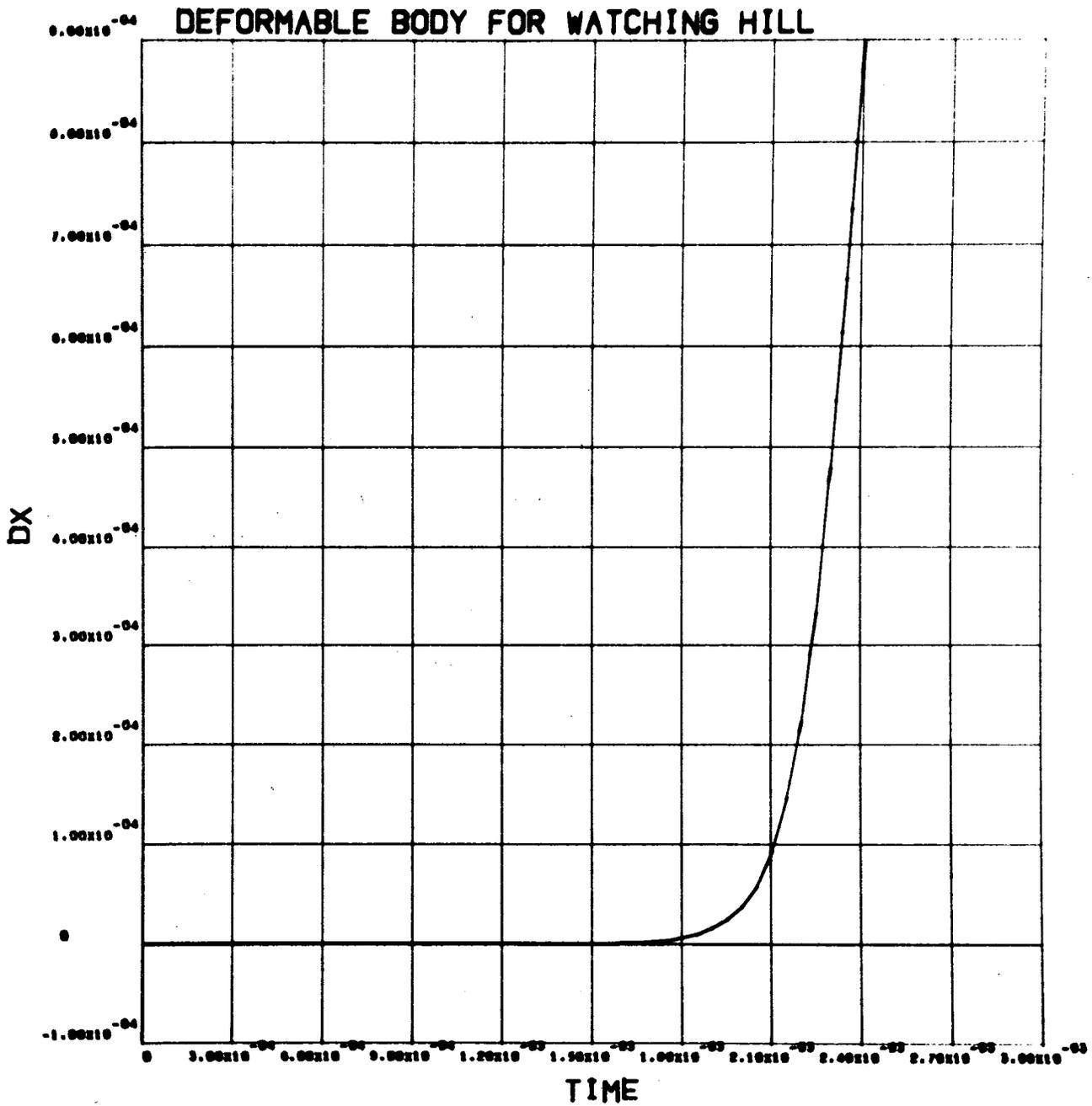


Figure B-55

Radial displacement history (m) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

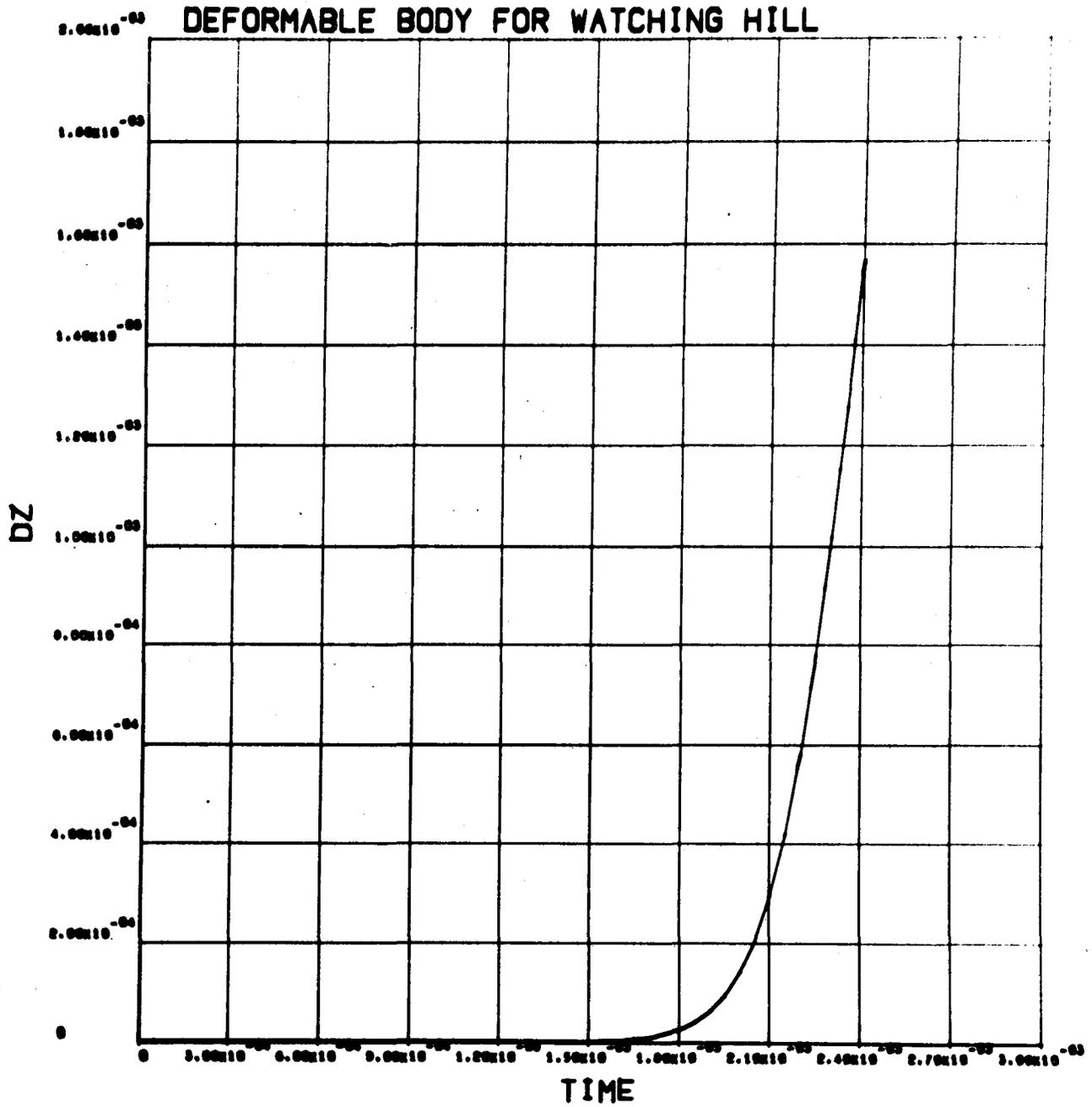


Figure B-56  
 Vertical displacement history (m) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

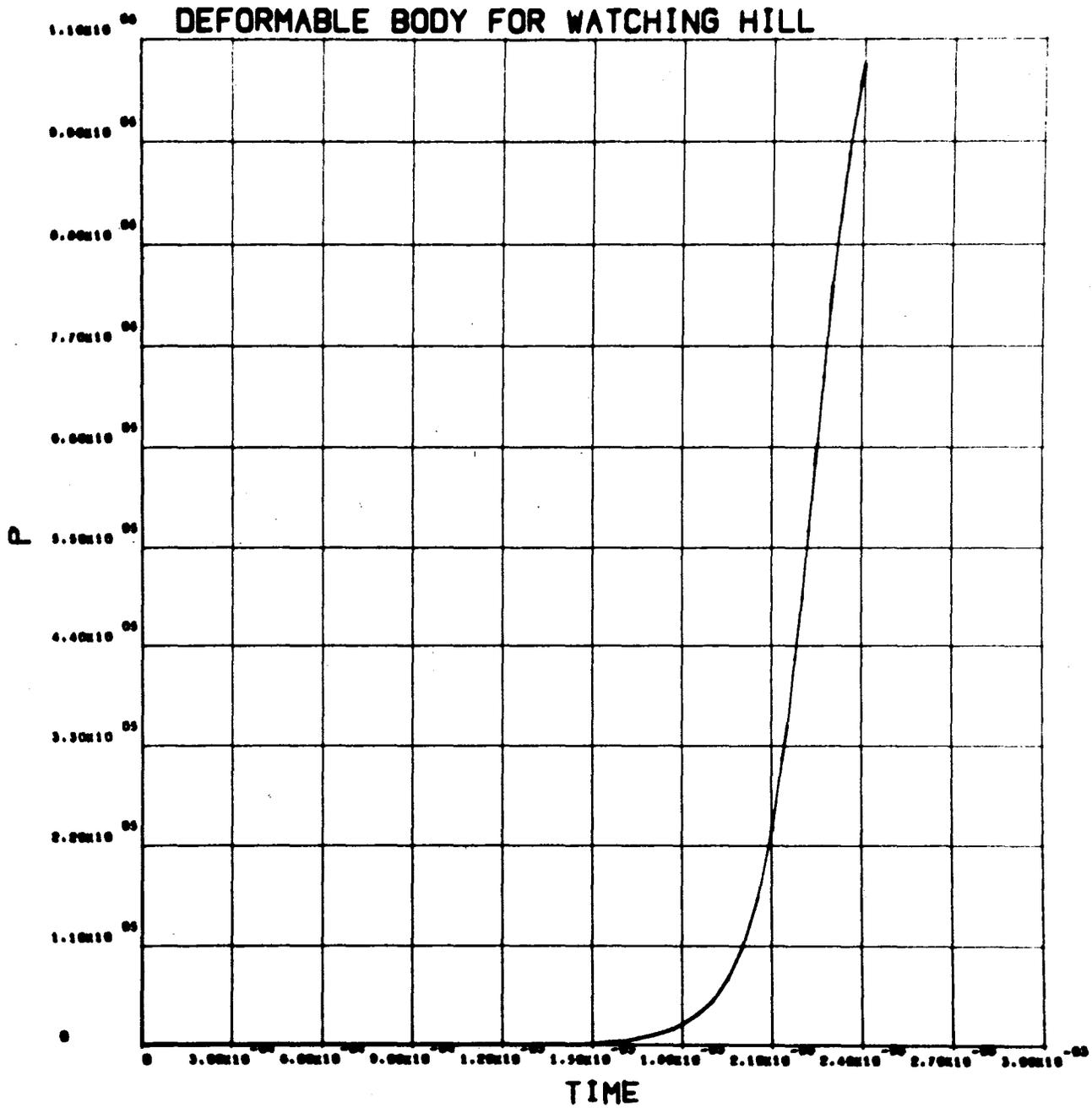


Figure B-57

Pressure history (Pa) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

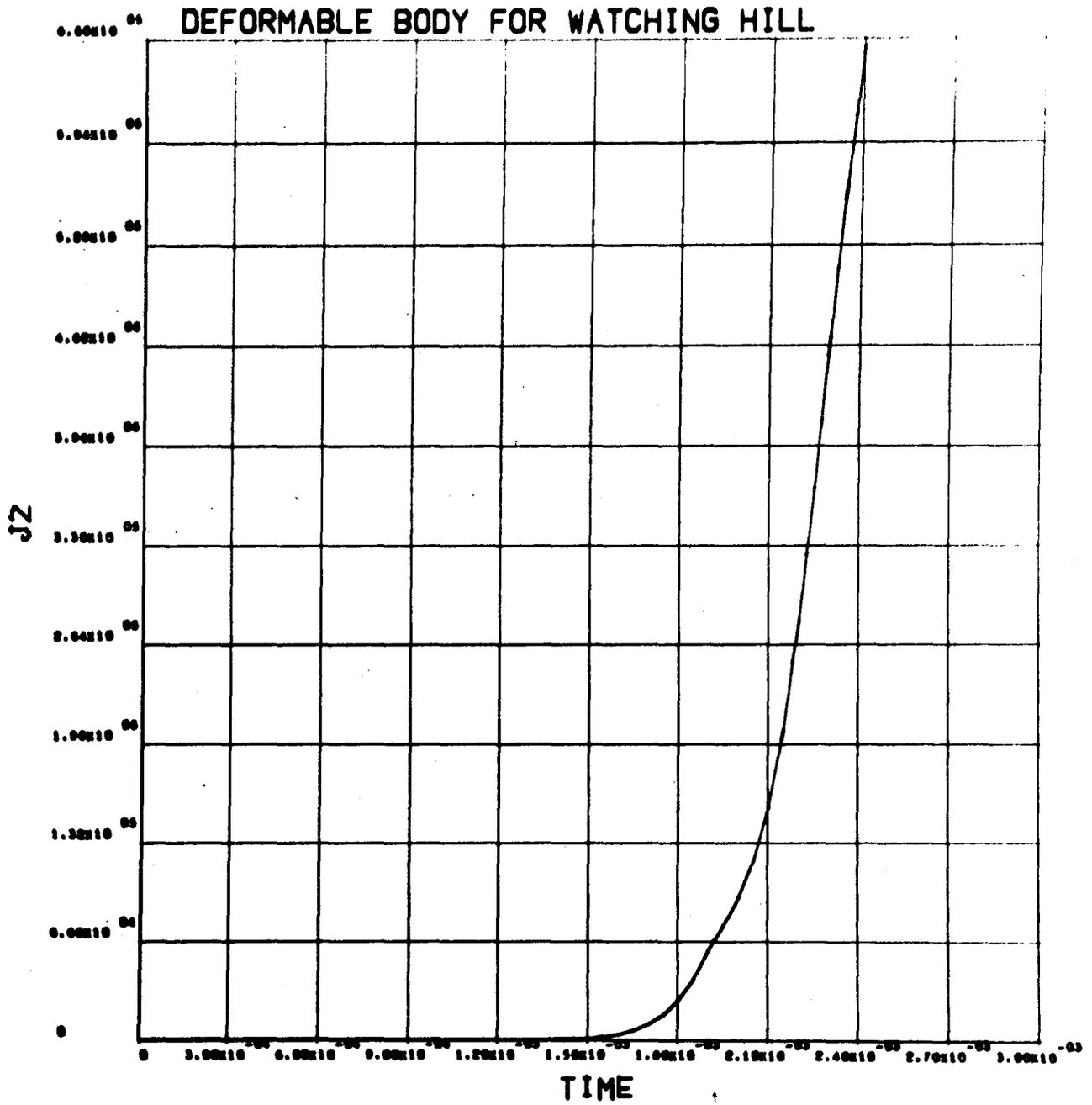


Figure B-58

Deviator stress, J2, history (Pa) in soil at range 75 mm, depth 0.4 m (deformable penetrator).

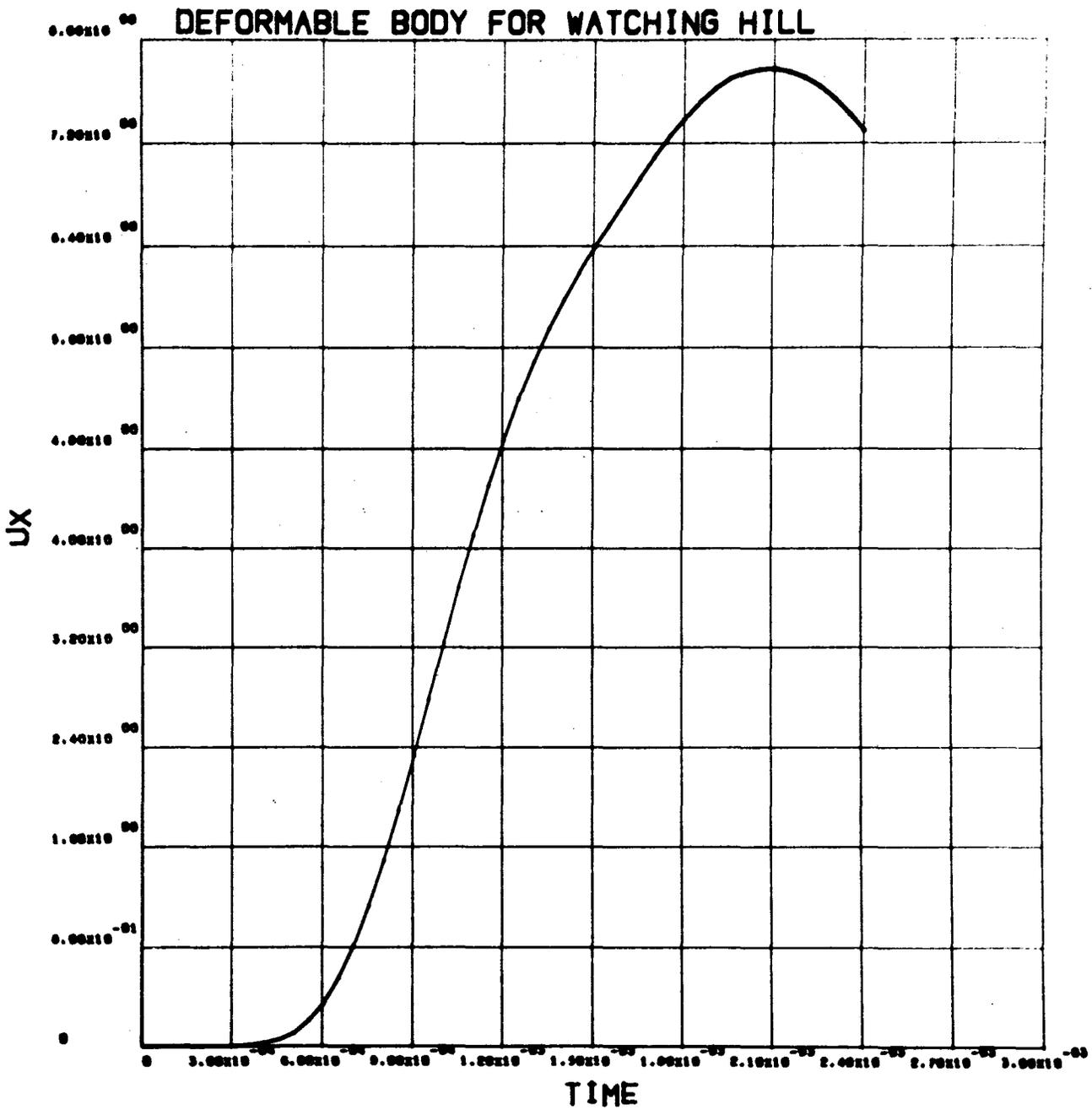


Figure B-59

Radial velocity history (m/s) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

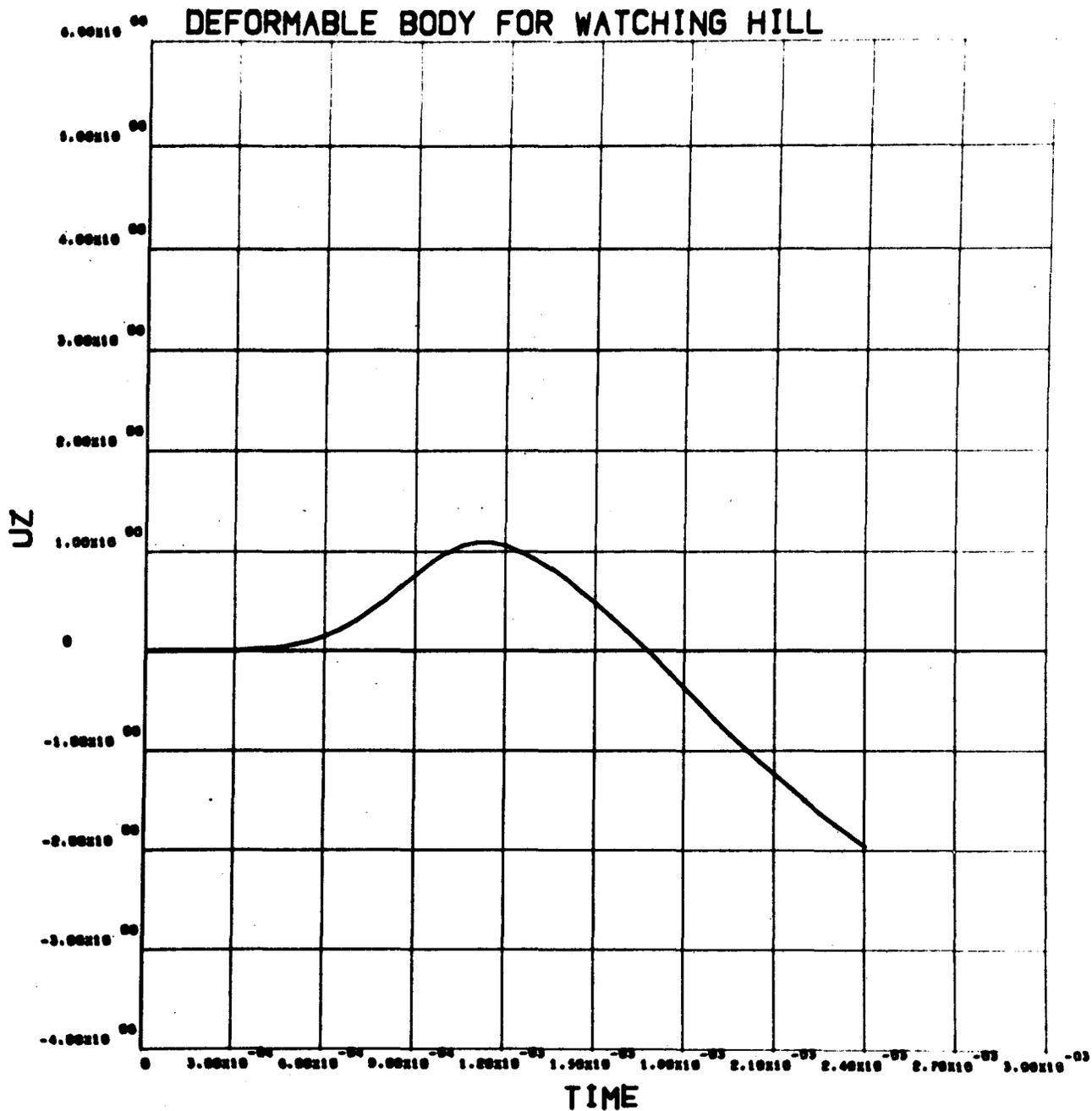


Figure B-60

Vertical velocity history (m/s) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

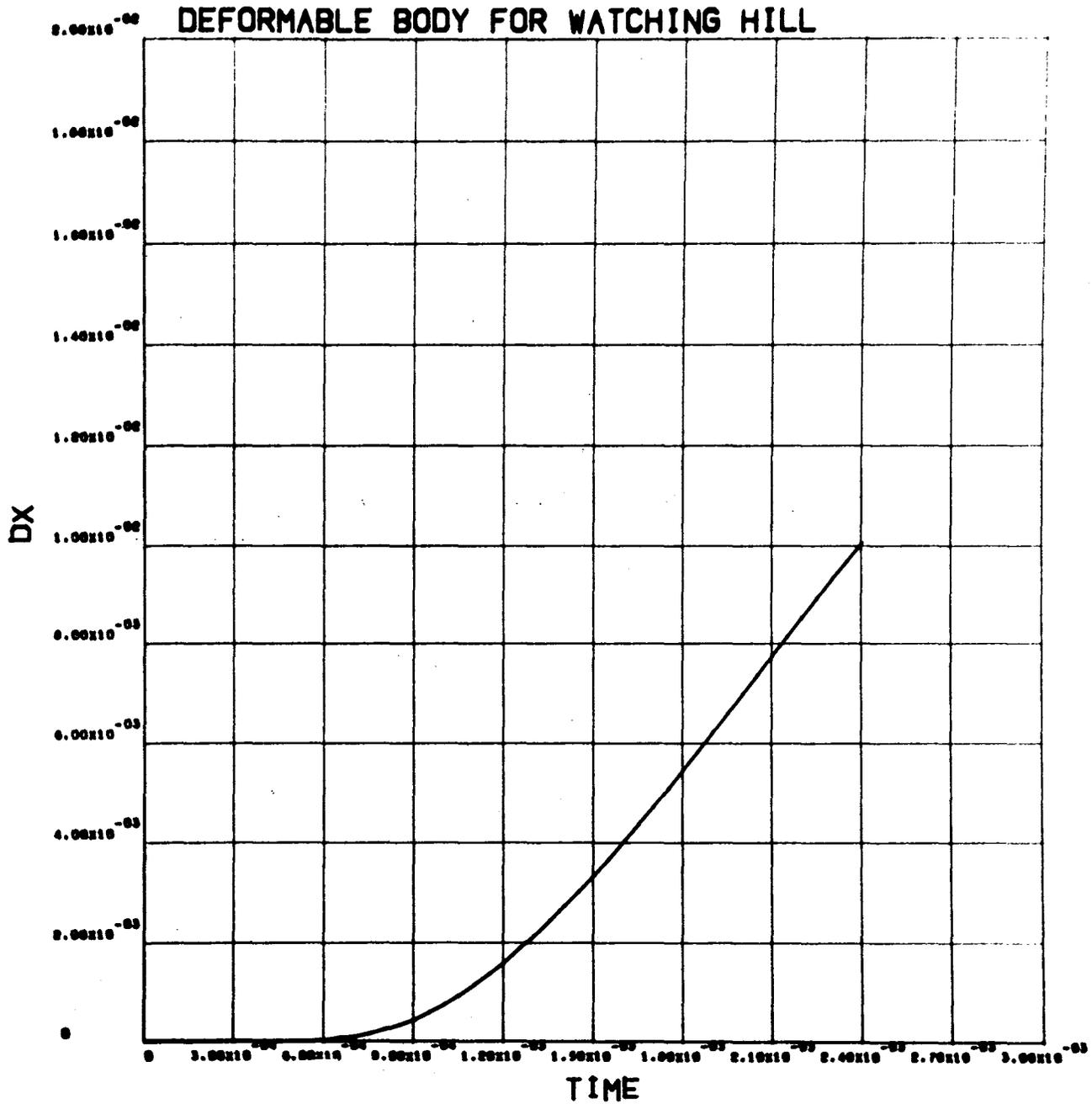


Figure B-61

Radial displacement history (m) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

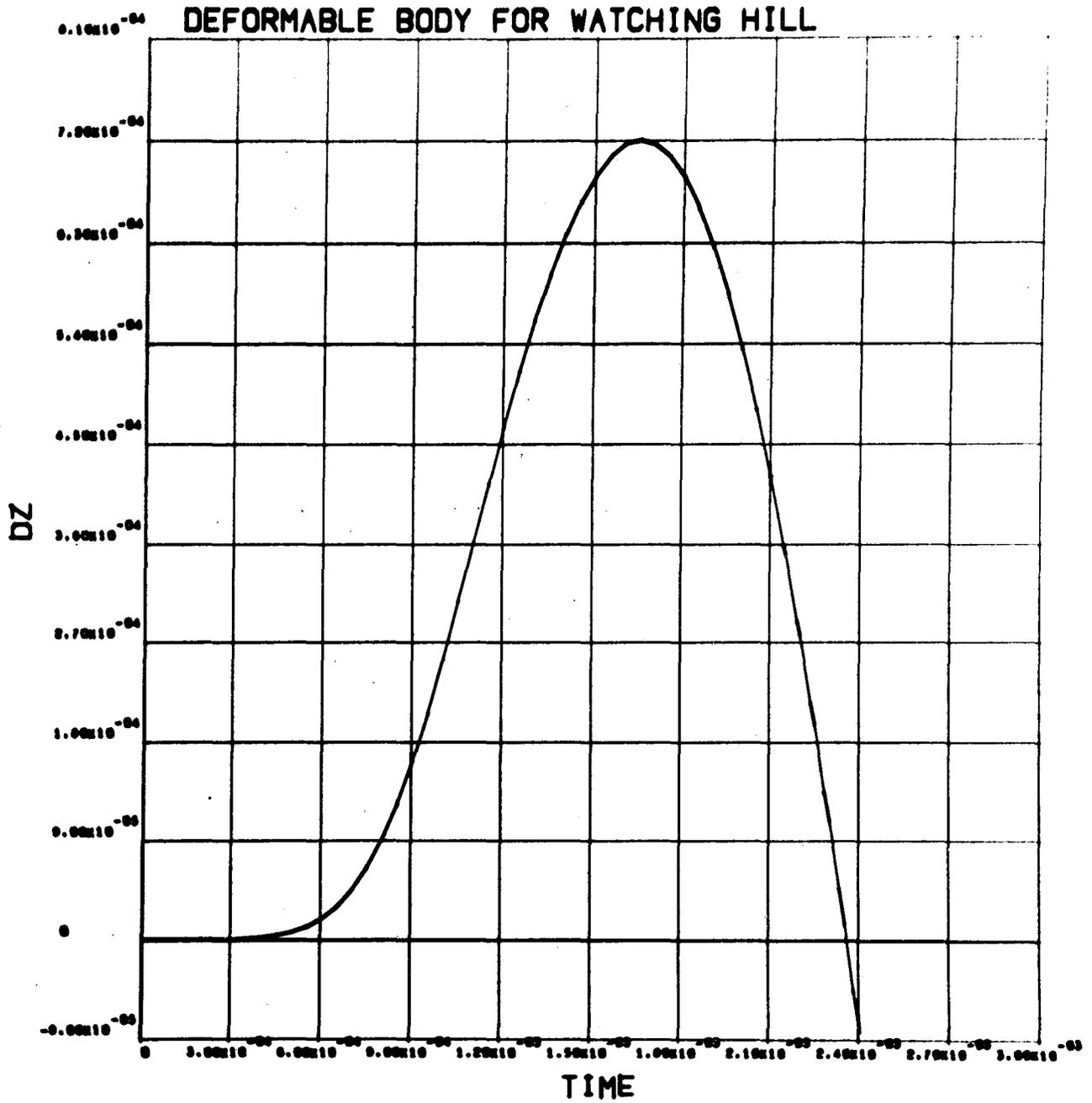


Figure B-62  
 Vertical displacement history (m) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

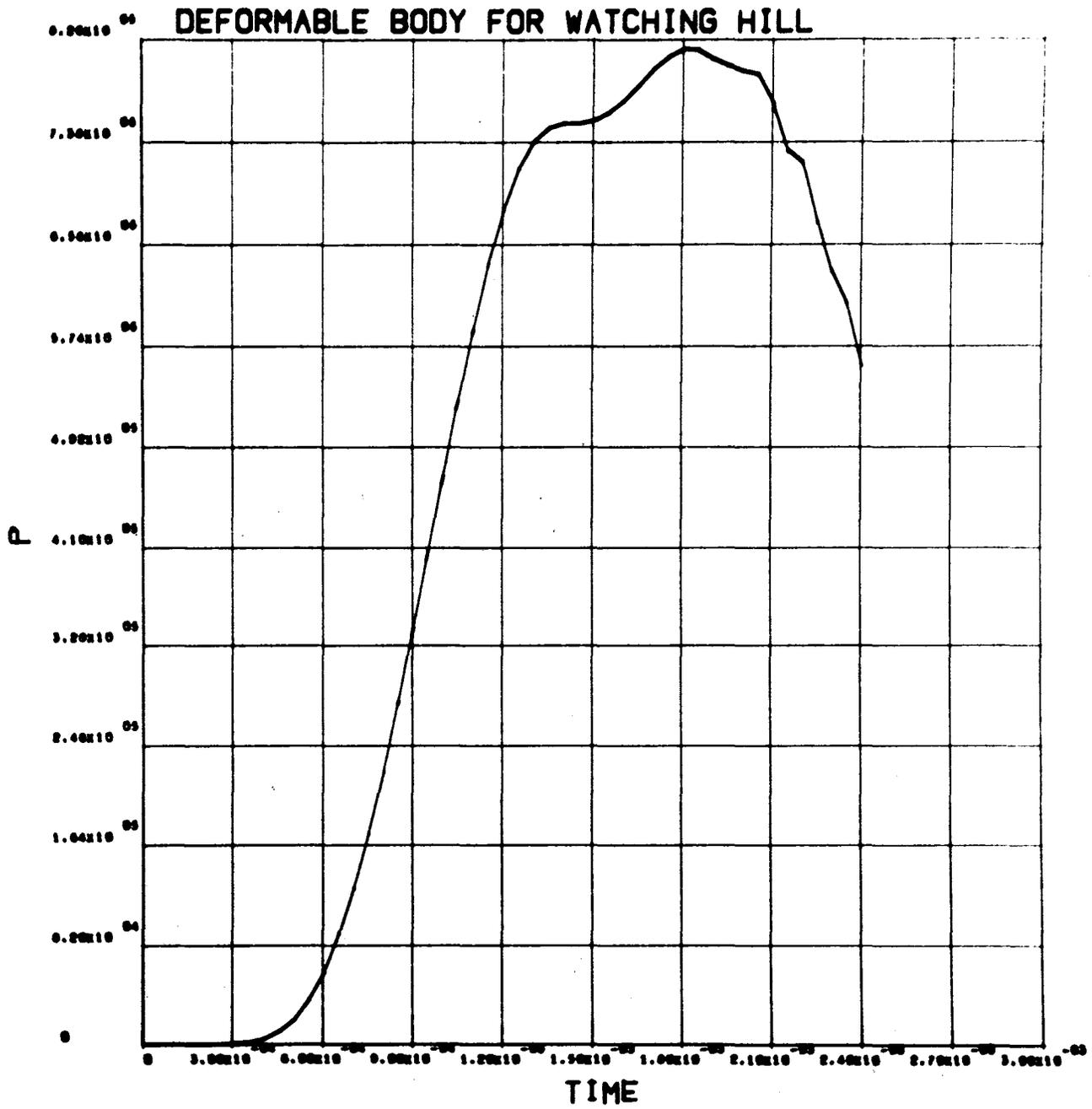


Figure B-63

Pressure history (Pa) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

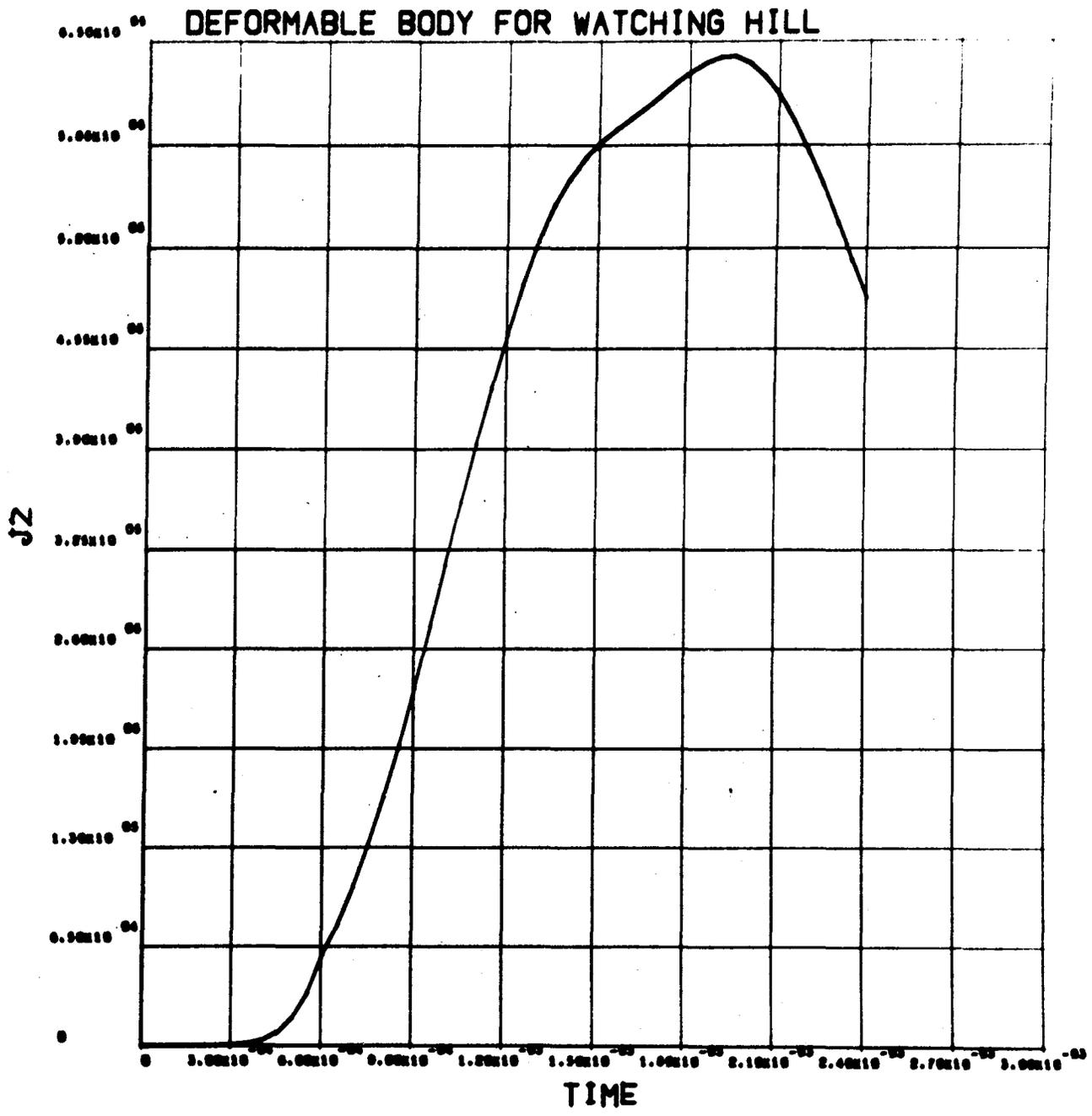


Figure B-64  
 Deviator stress,  $J_2$ , history (Pa) in soil at range 0.14 m, depth 0.1 m (deformable penetrator).

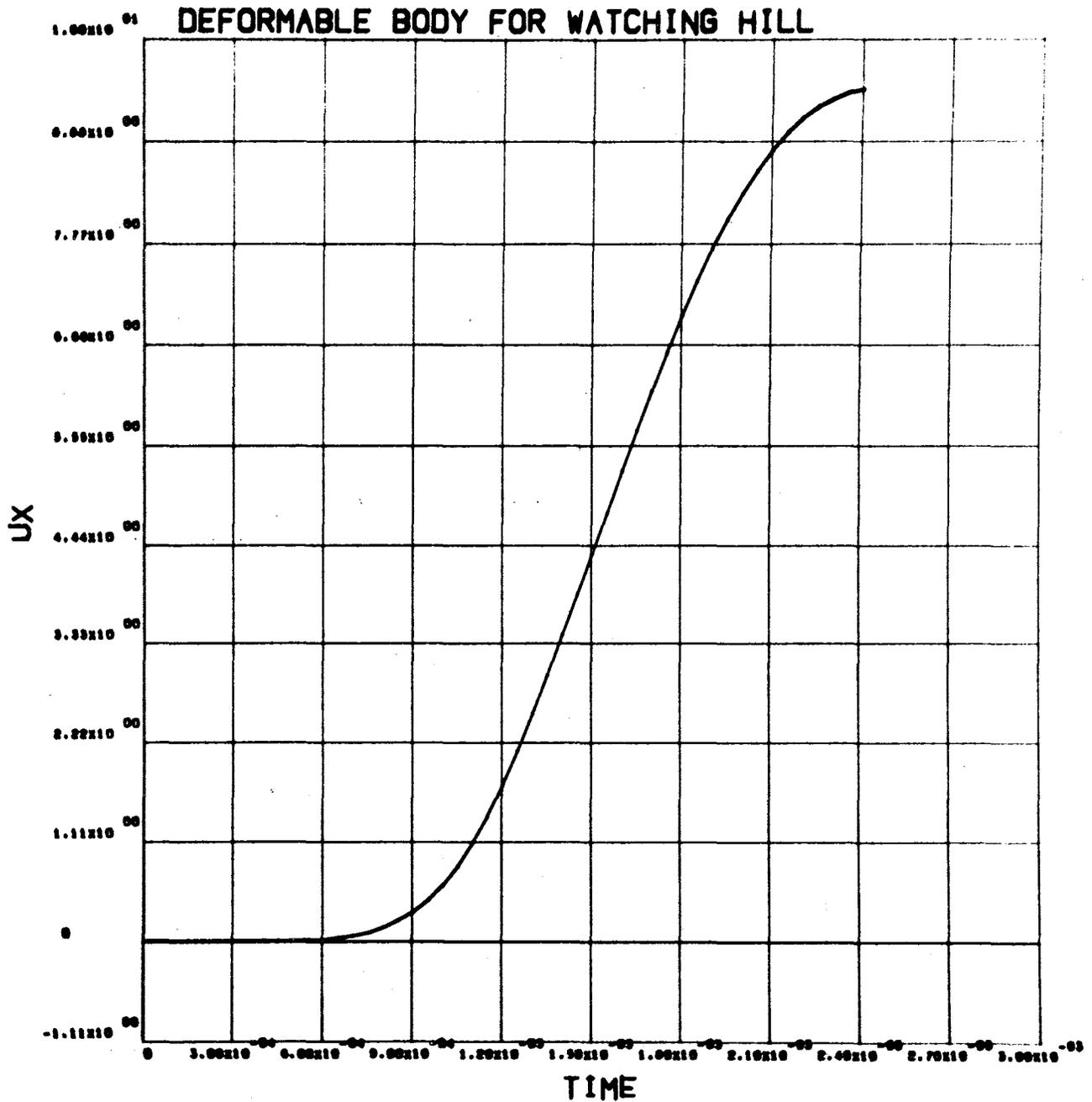


Figure B-65

Radial velocity history (m/s) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

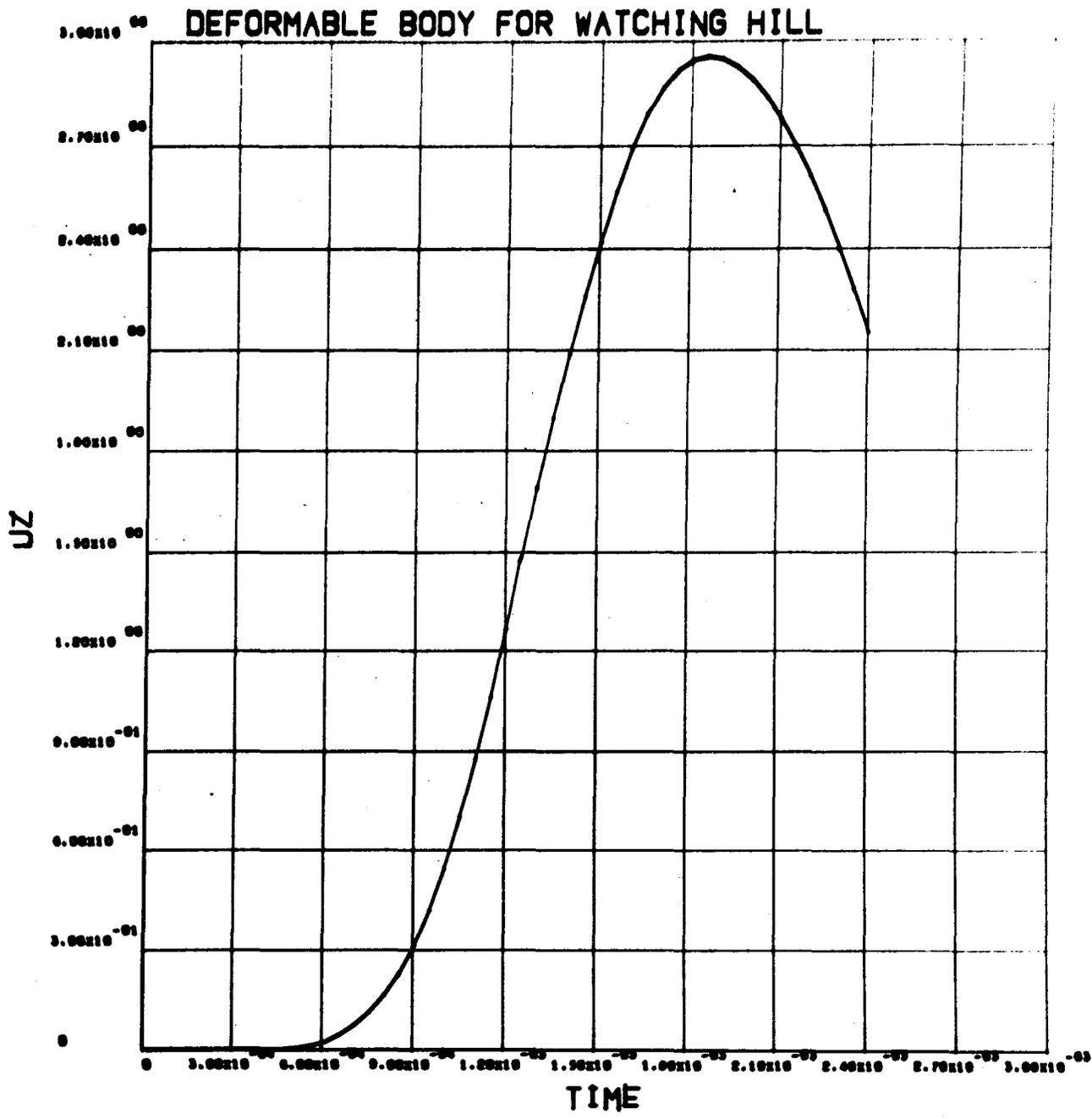


Figure B-66  
 Vertical velocity history (m/s) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

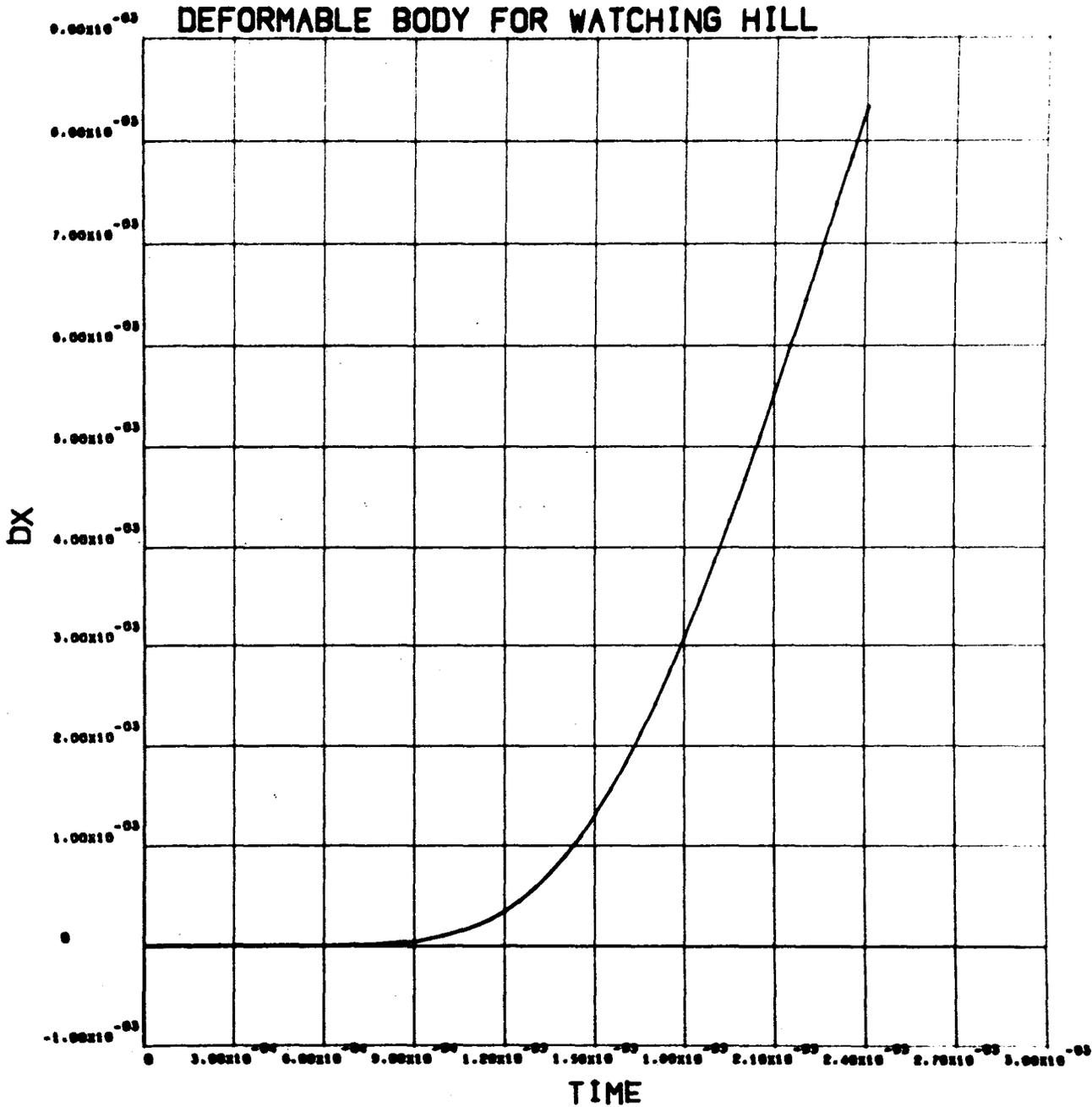


Figure B-67

Radial displacement history (m) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

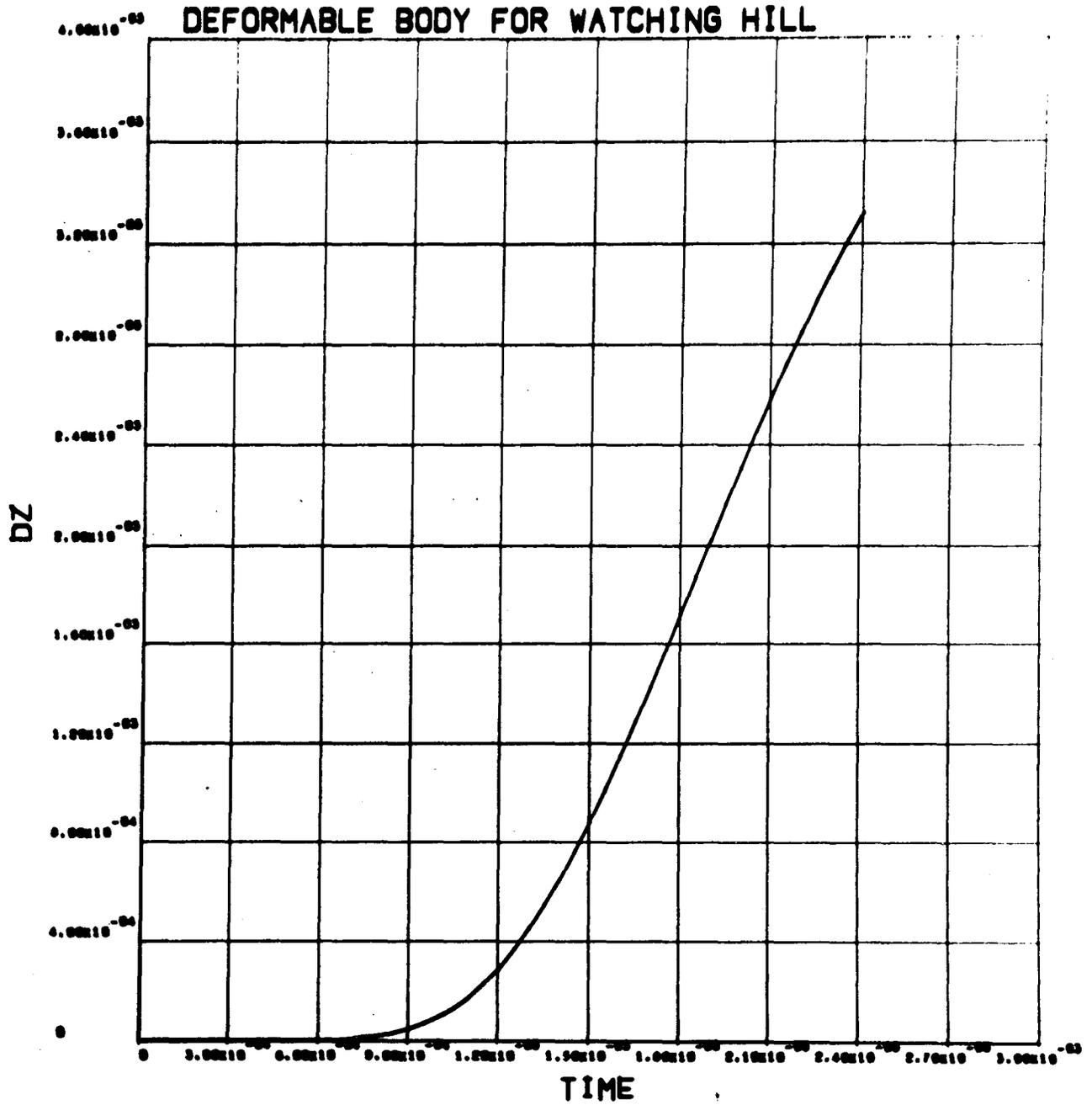


Figure B-68  
 Vertical displacement history (m) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

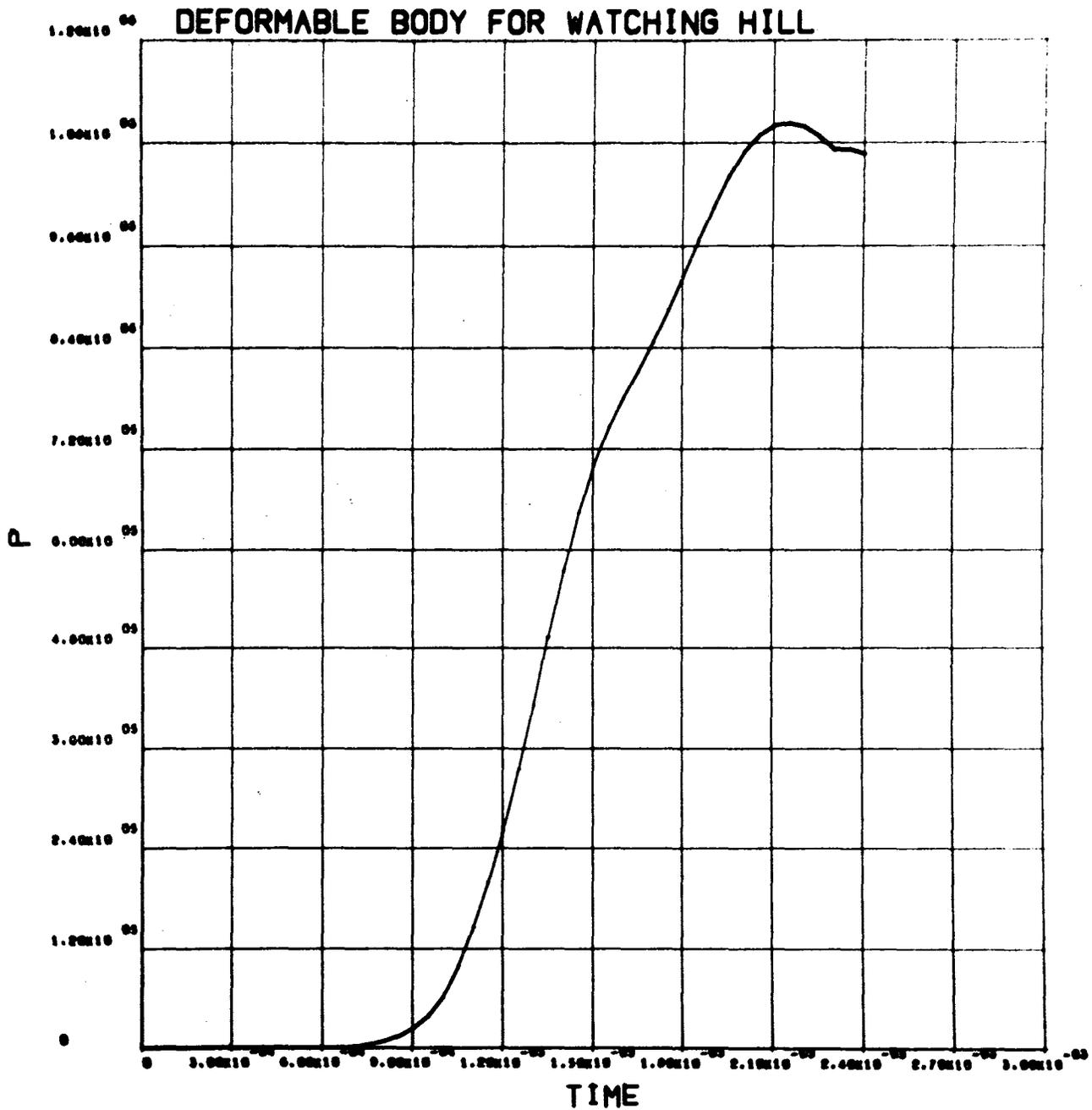


Figure B-69

Pressure history (Pa) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

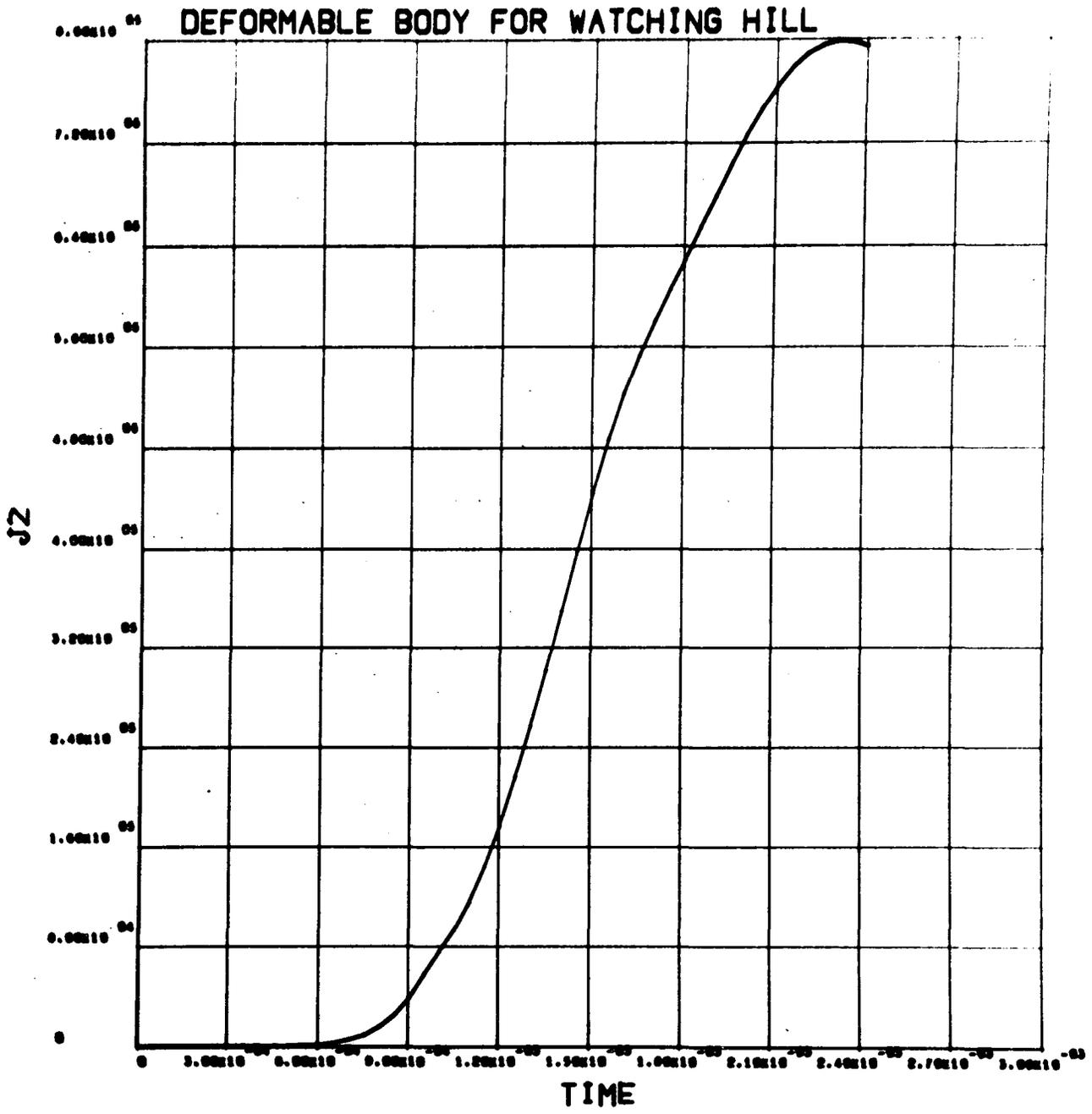


Figure B-70  
 Deviator stress, J2, history (Pa) in soil at range 0.14 m, depth 0.2 m (deformable penetrator).

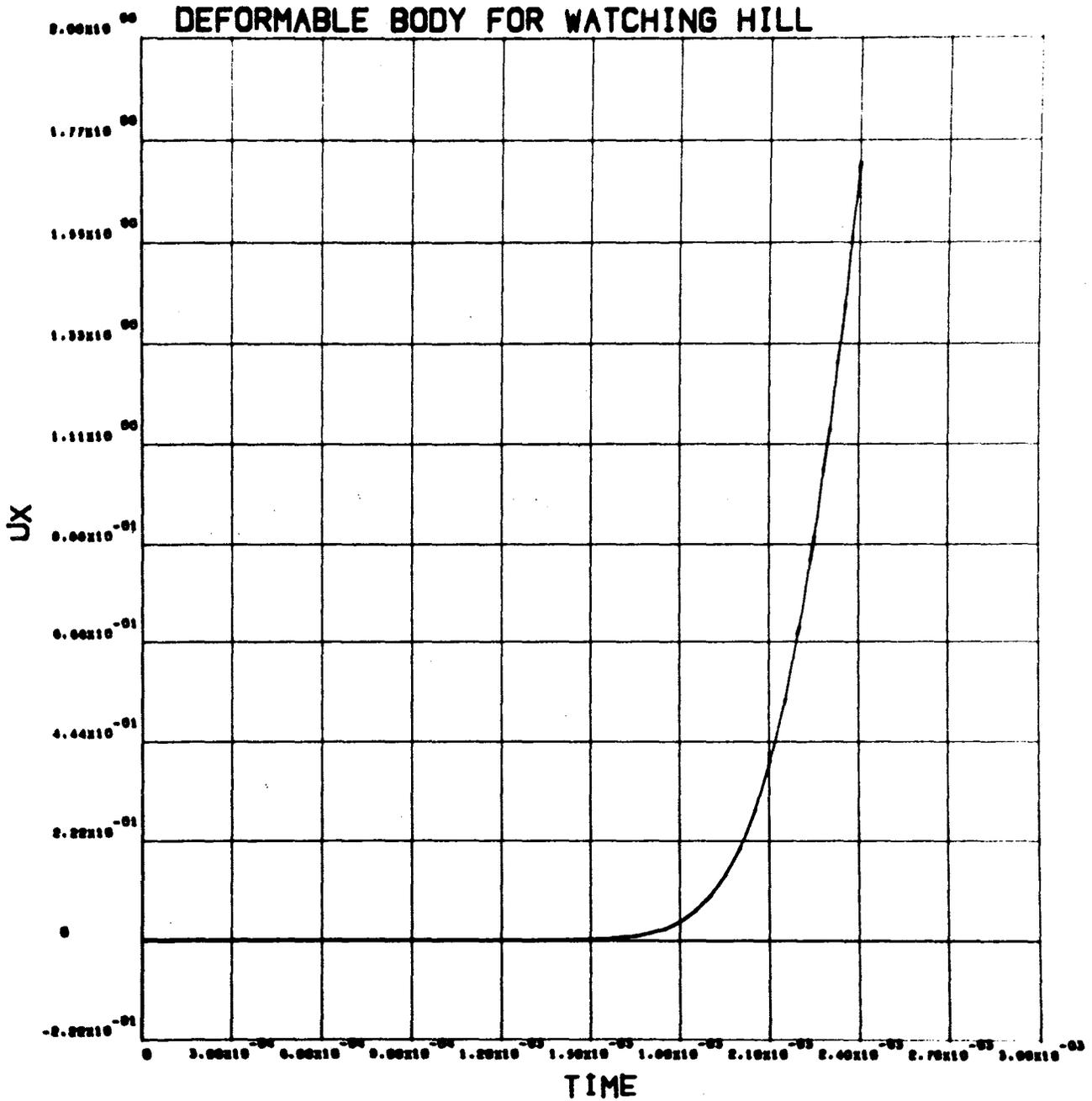


Figure B-71

Radial velocity history (m/s) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

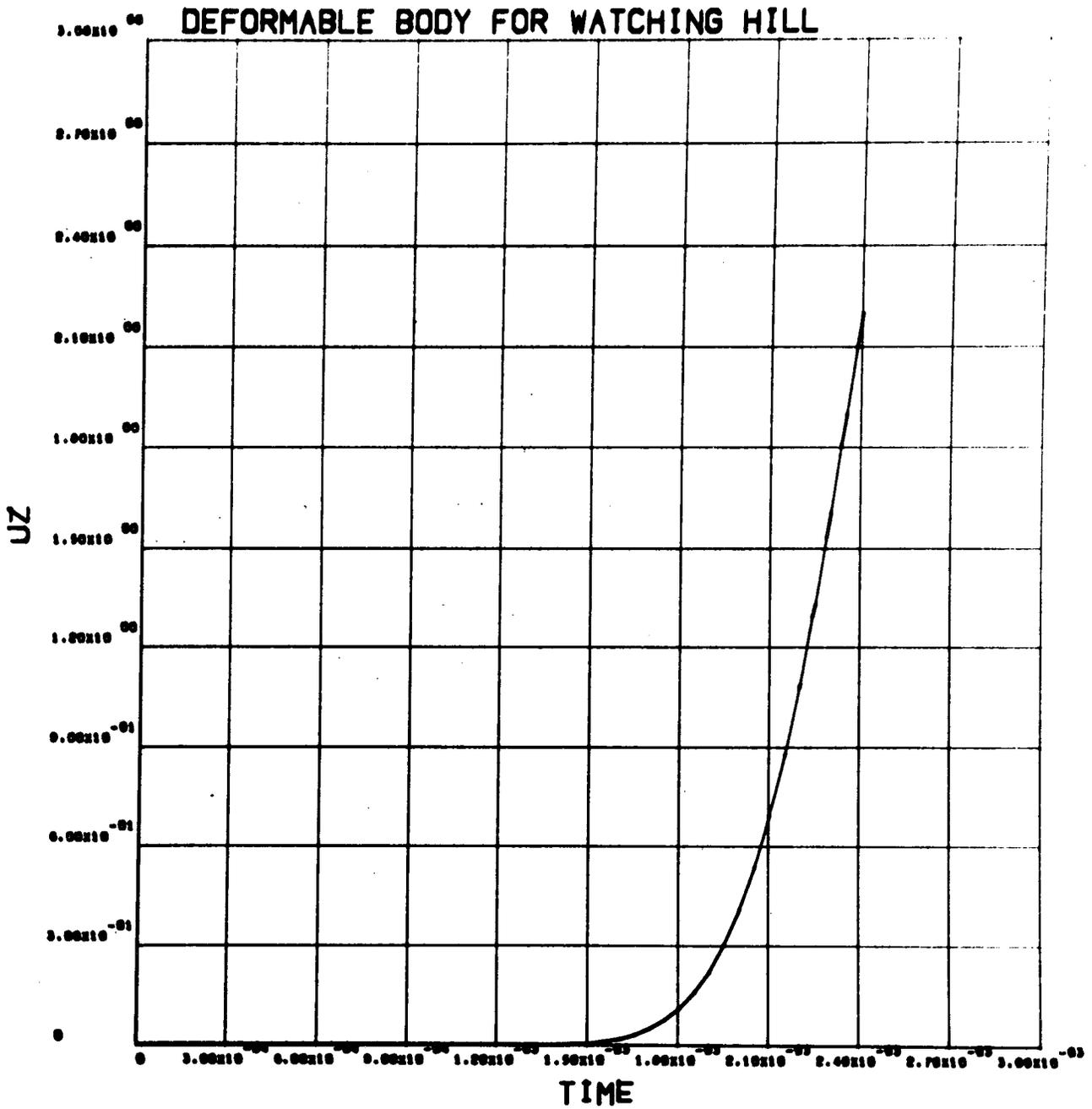


Figure B-72  
 Vertical velocity history (m/s) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

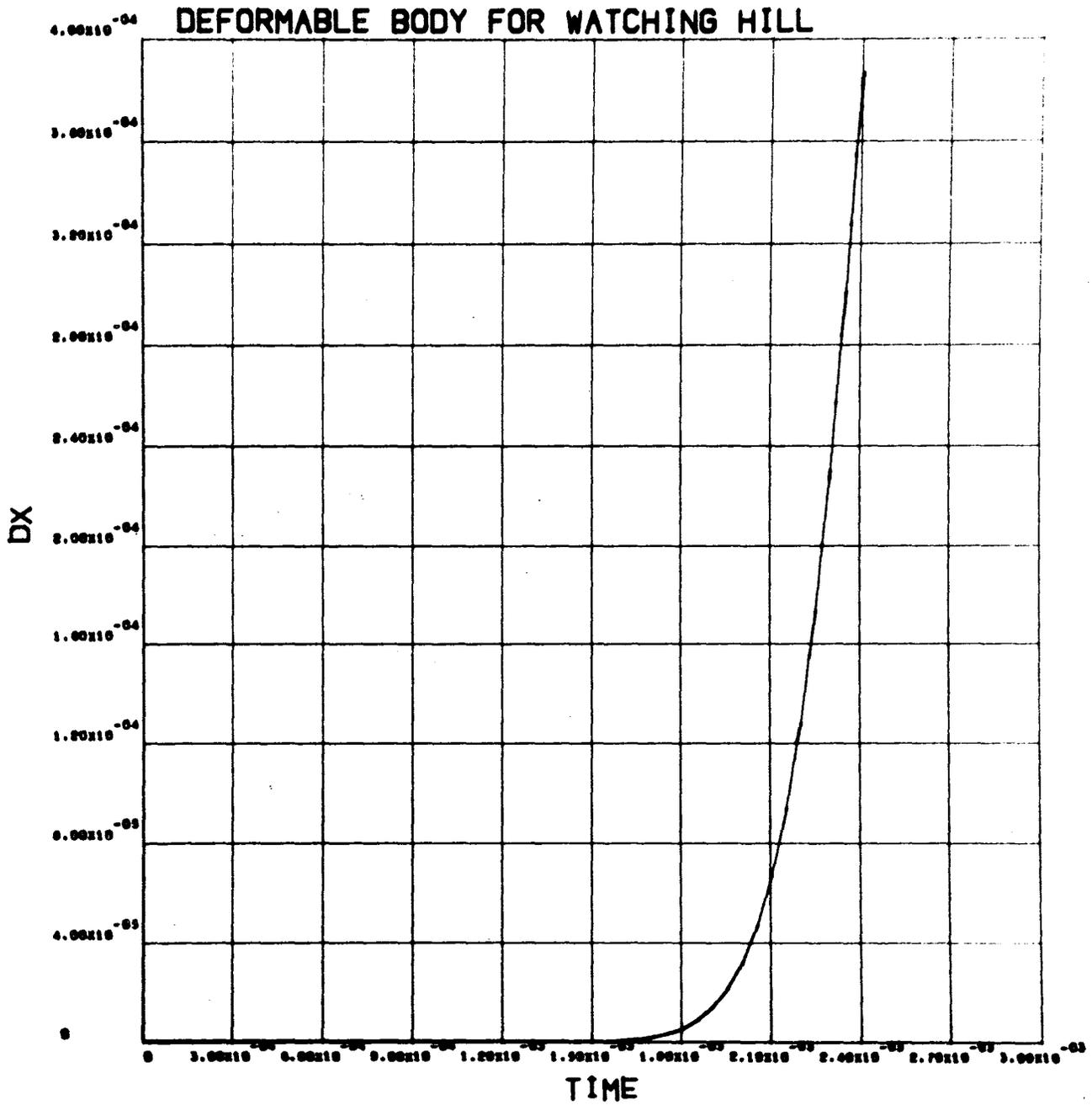


Figure B-73  
 Radial displacement history (m) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

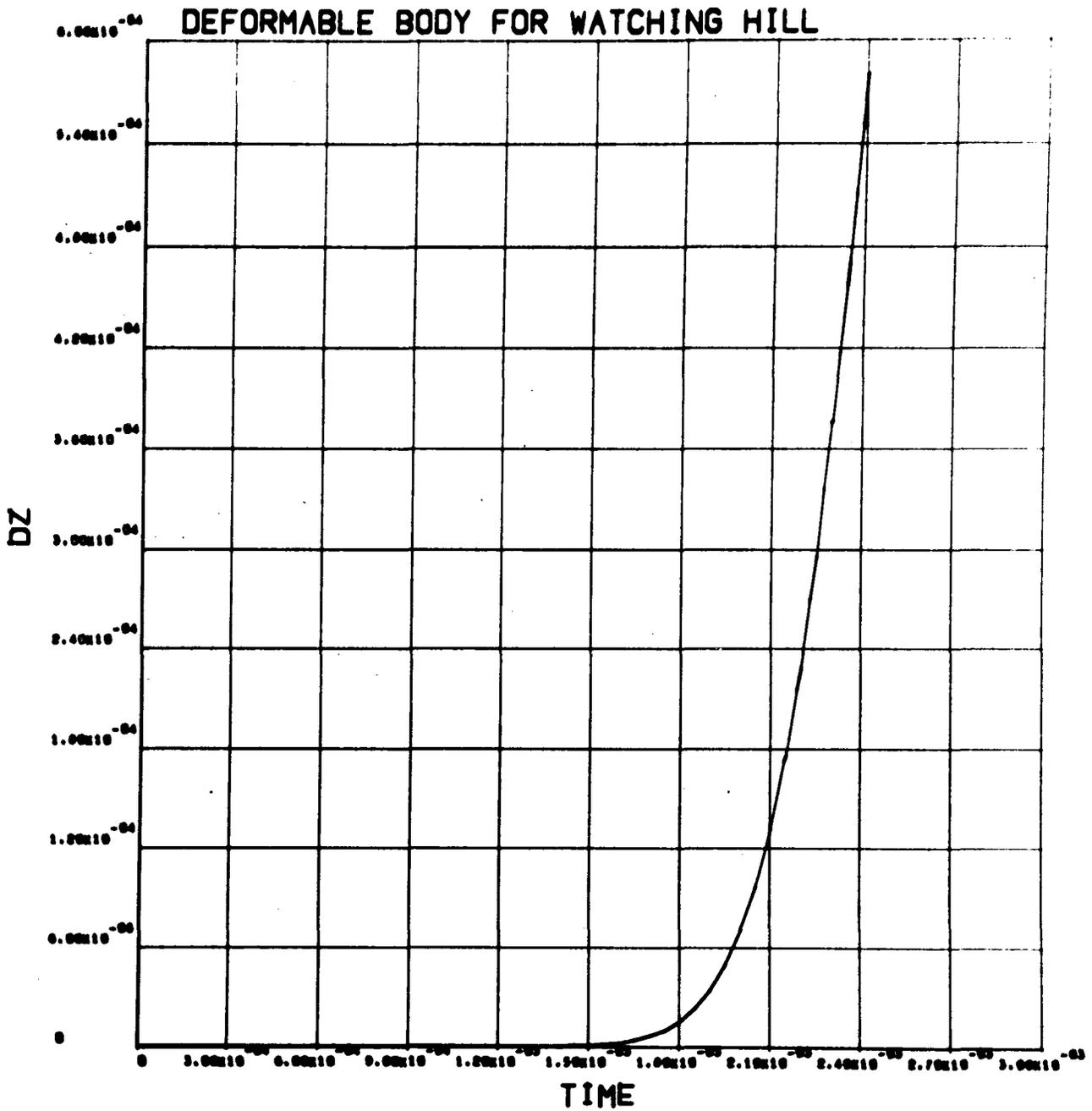


Figure B-74

Vertical displacement history (m) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

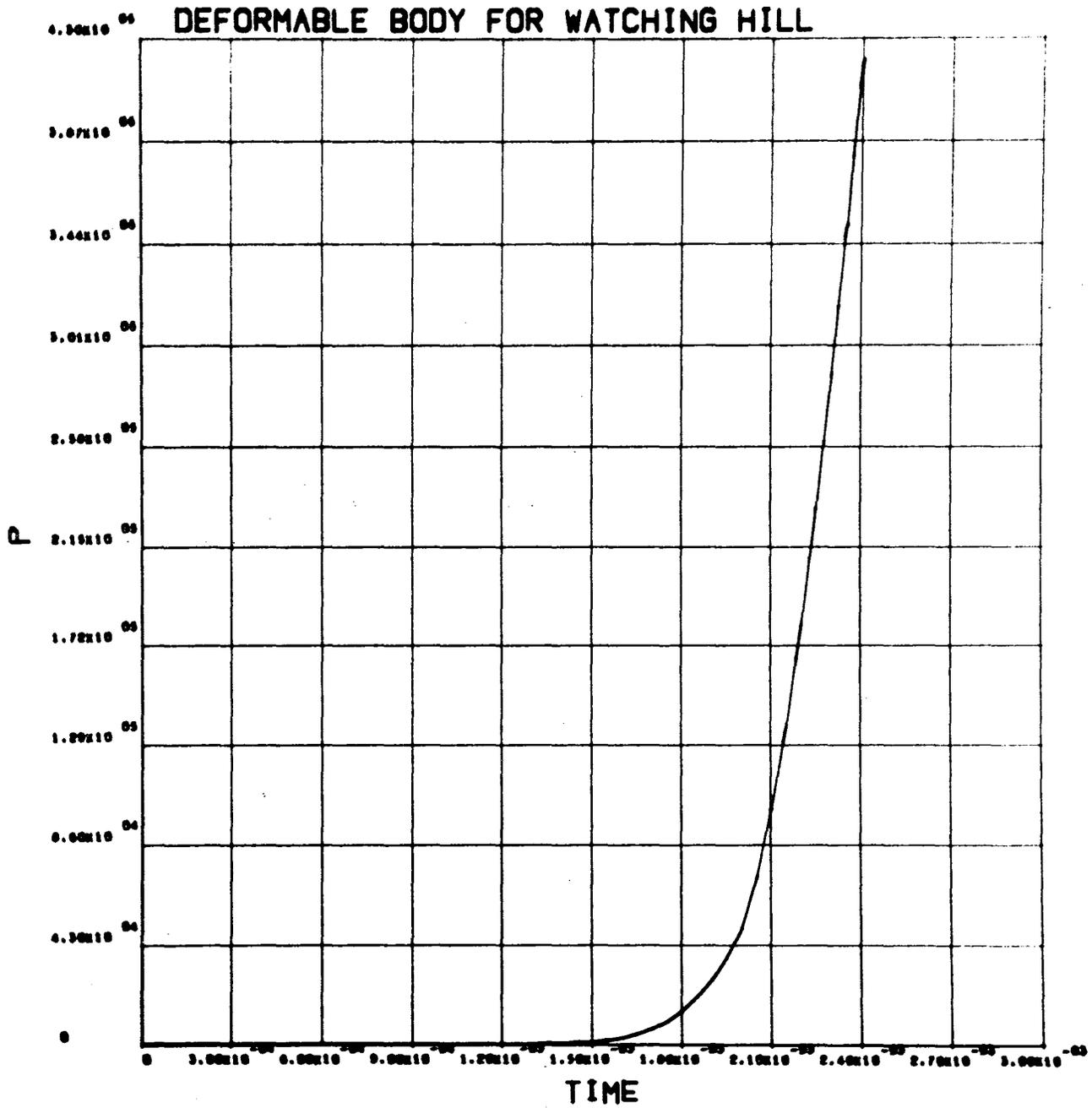


Figure B-75

Pressure history (Pa) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

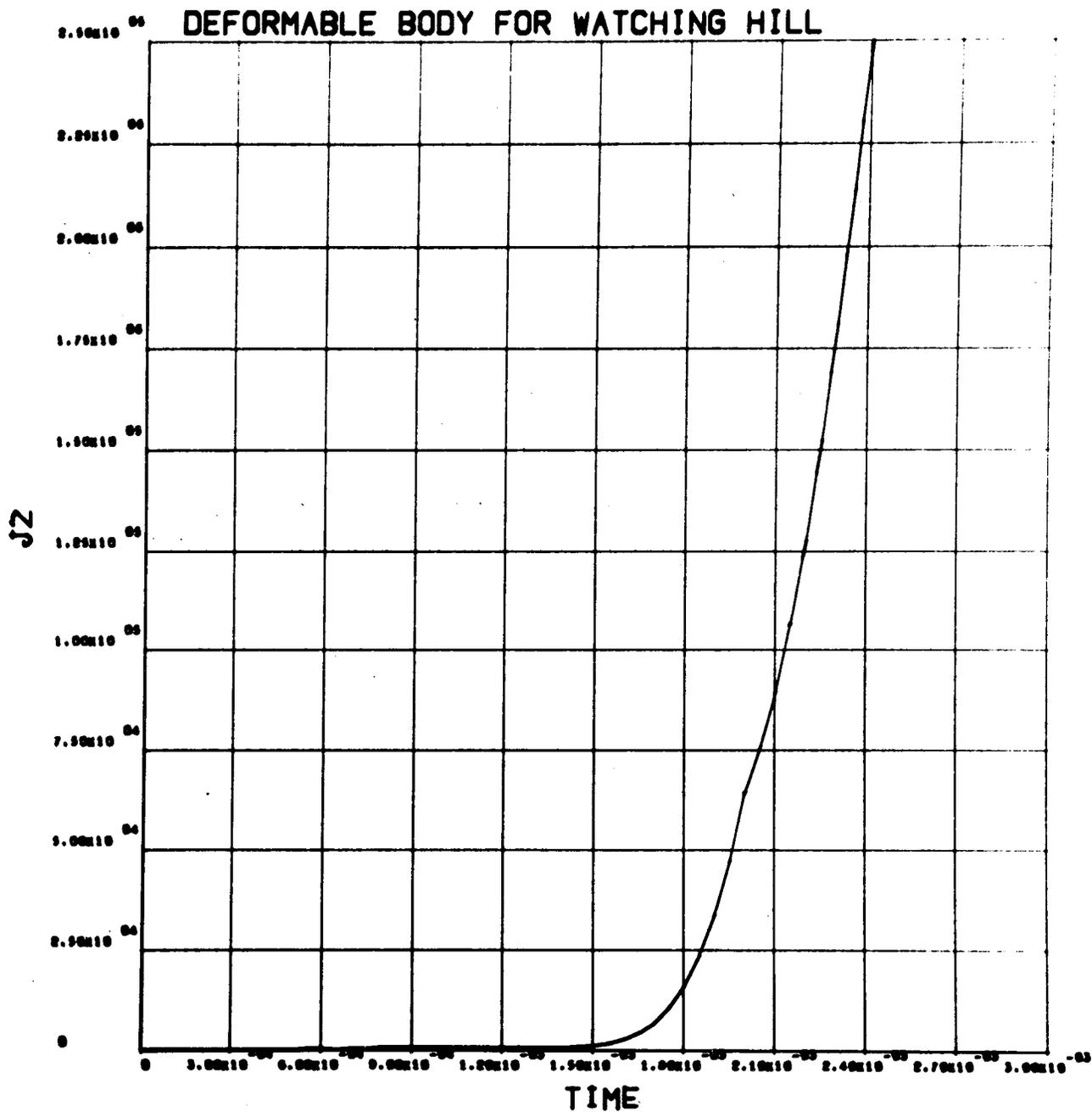


Figure B-76

Deviator stress,  $J_2$ , history (Pa) in soil at range 0.14 m, depth 0.4 m (deformable penetrator).

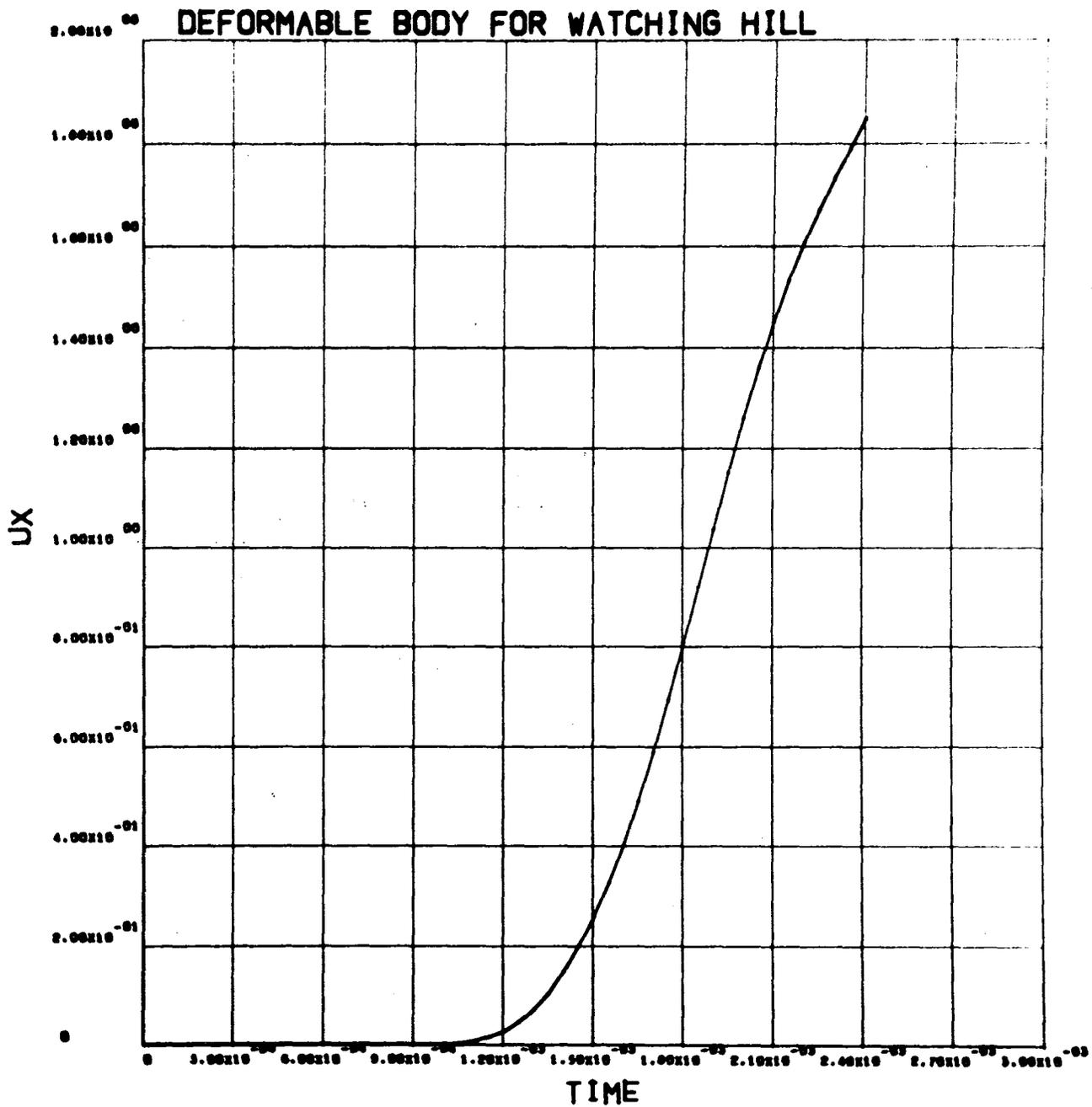


Figure B-77

Radial velocity history (m/s) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

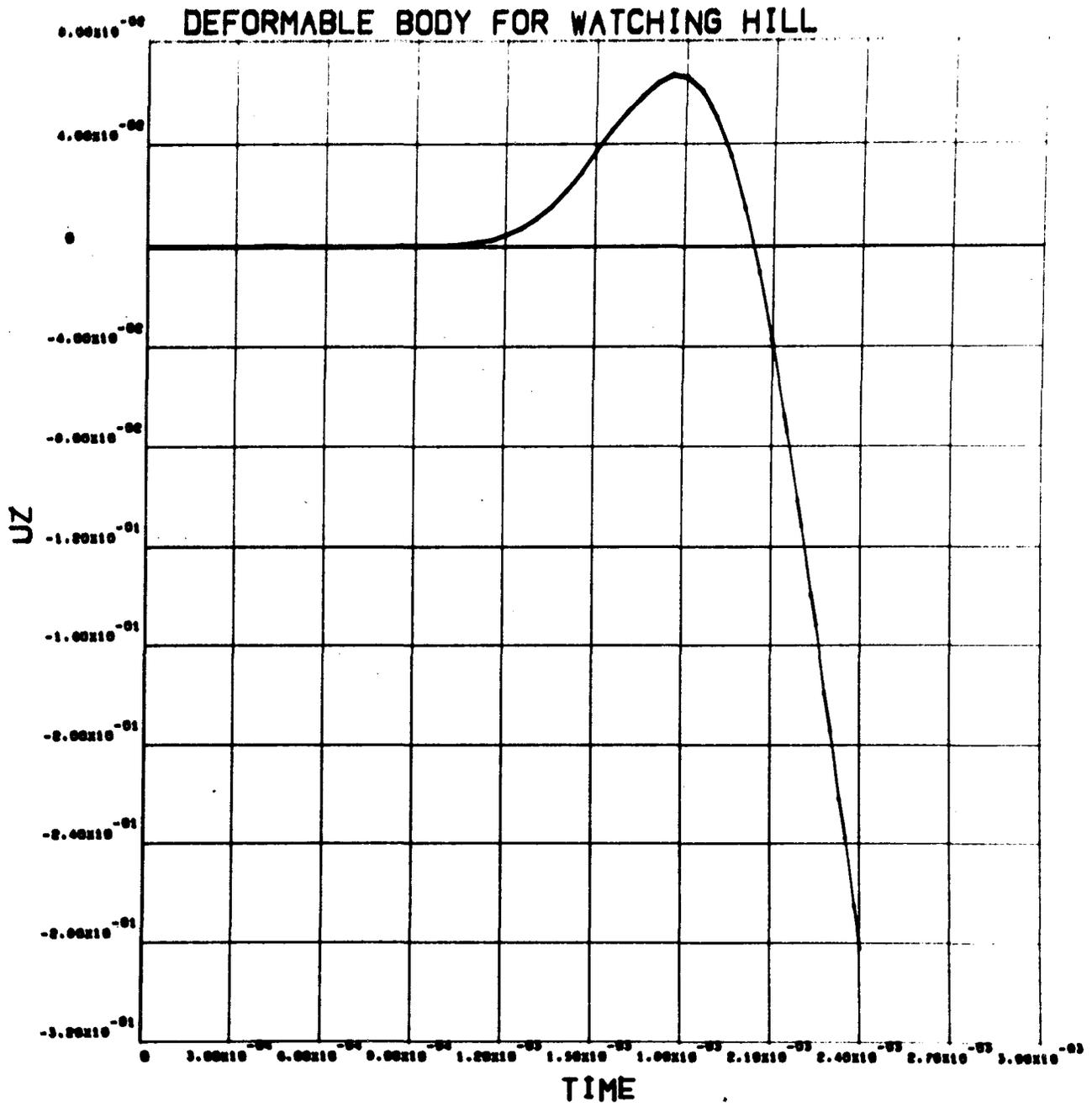


Figure B-78  
 Vertical velocity history (m/s) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

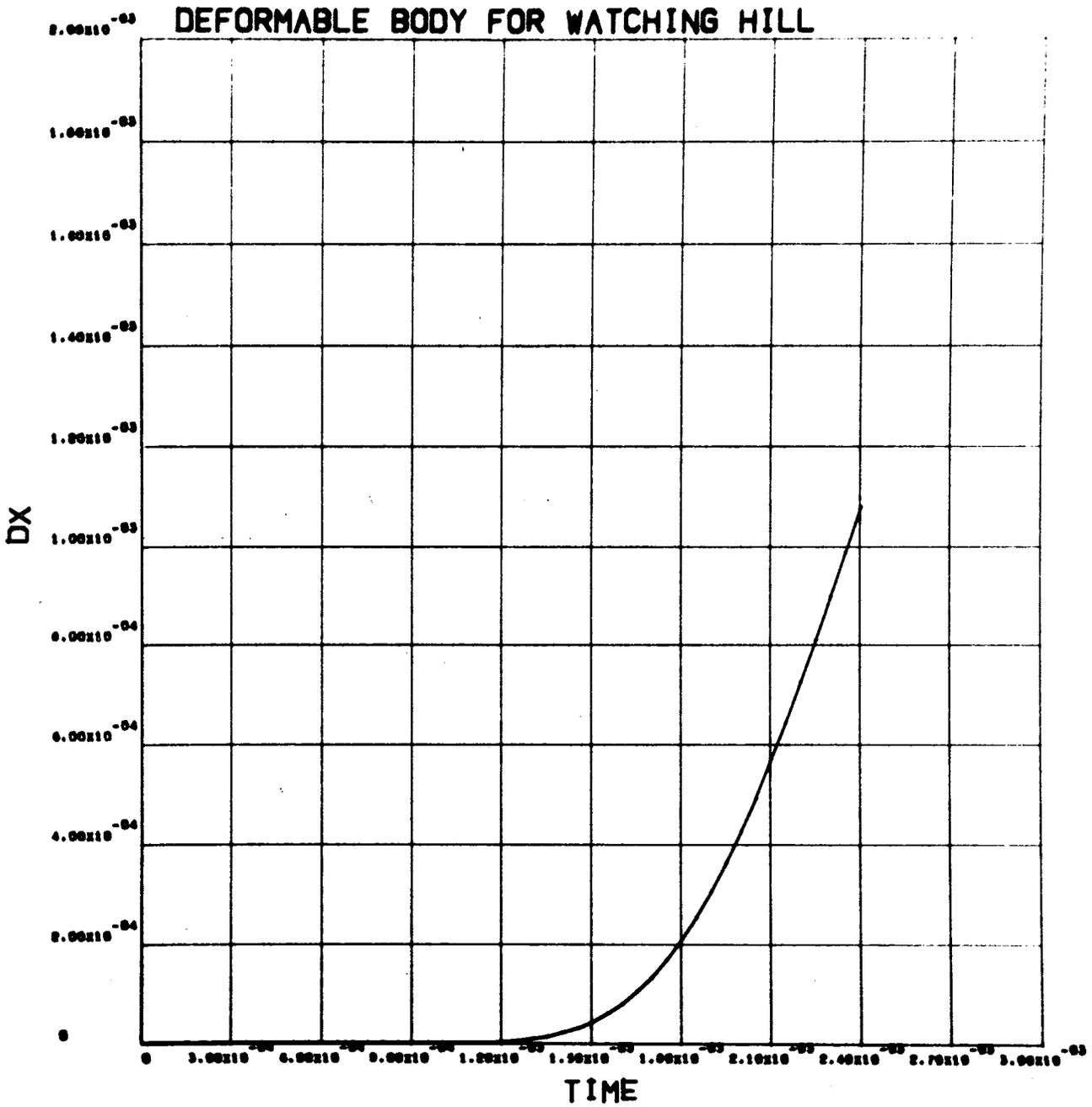


Figure B-79

Radial displacement history (m) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

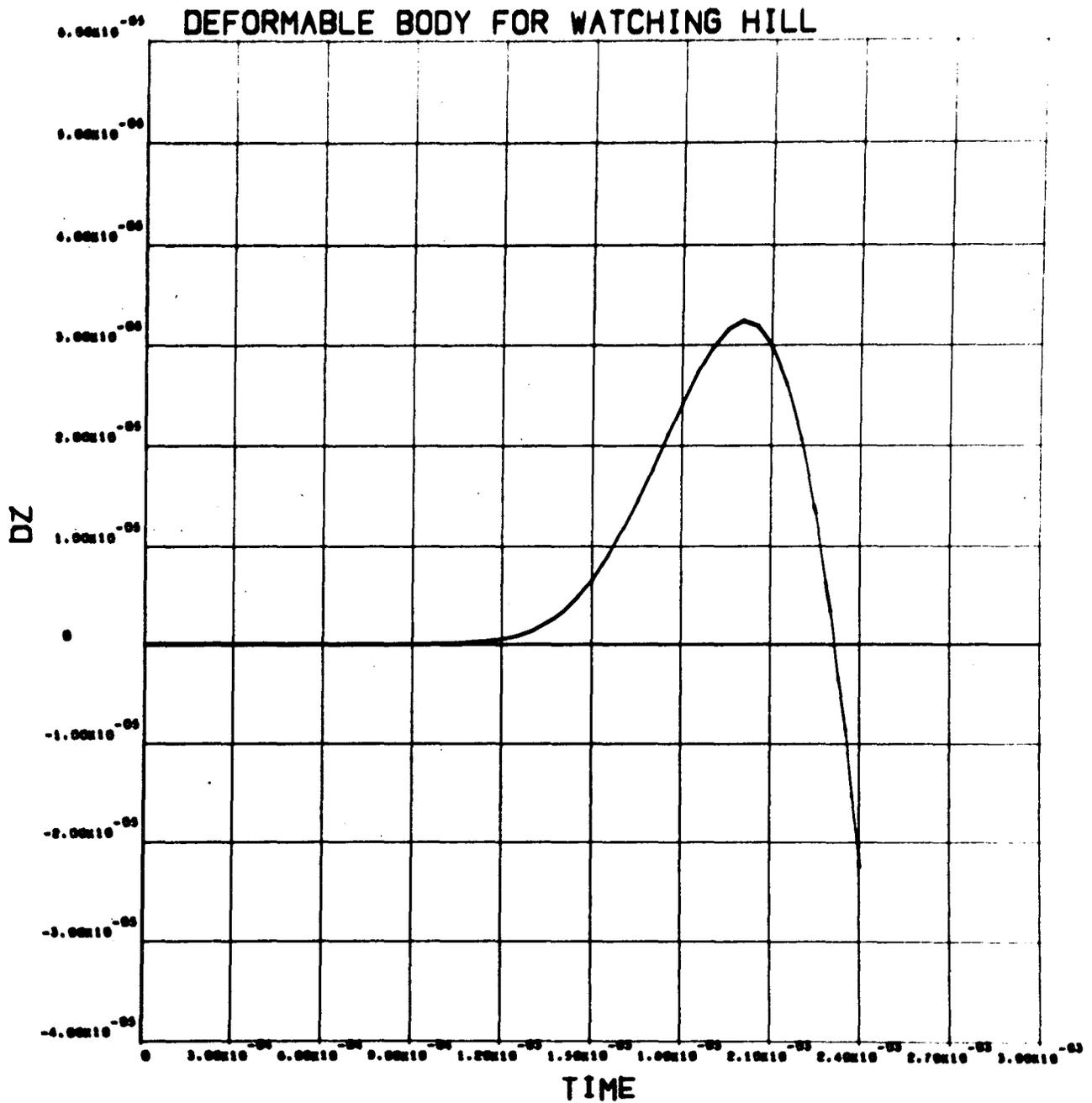


Figure B-80

Vertical displacement history (m) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

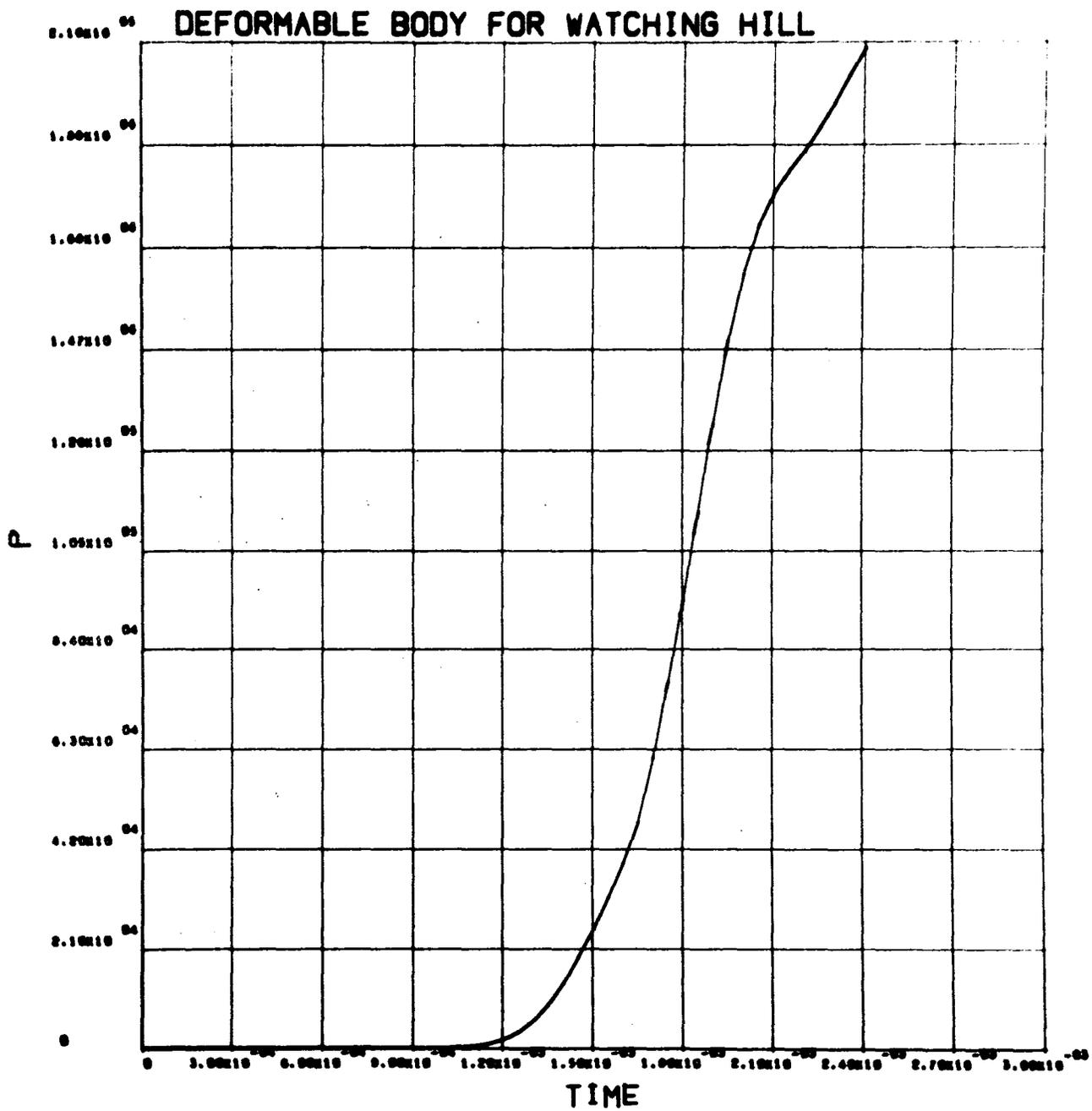


Figure B-81

Pressure history (Pa) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

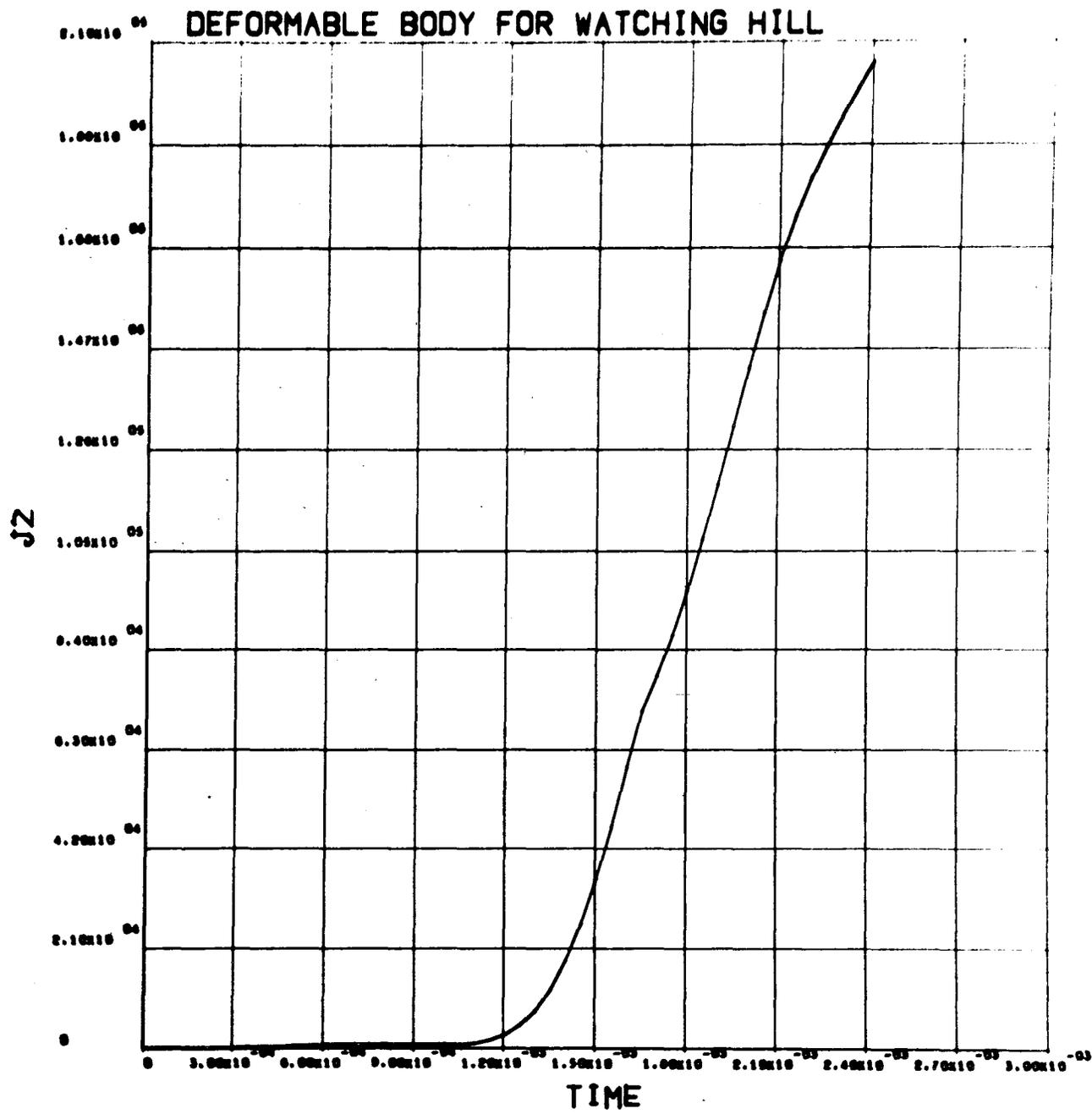


Figure B-82  
 Deviator stress, J2, history (Pa) in soil at range 0.28 m, depth 0.1 m (deformable penetrator).

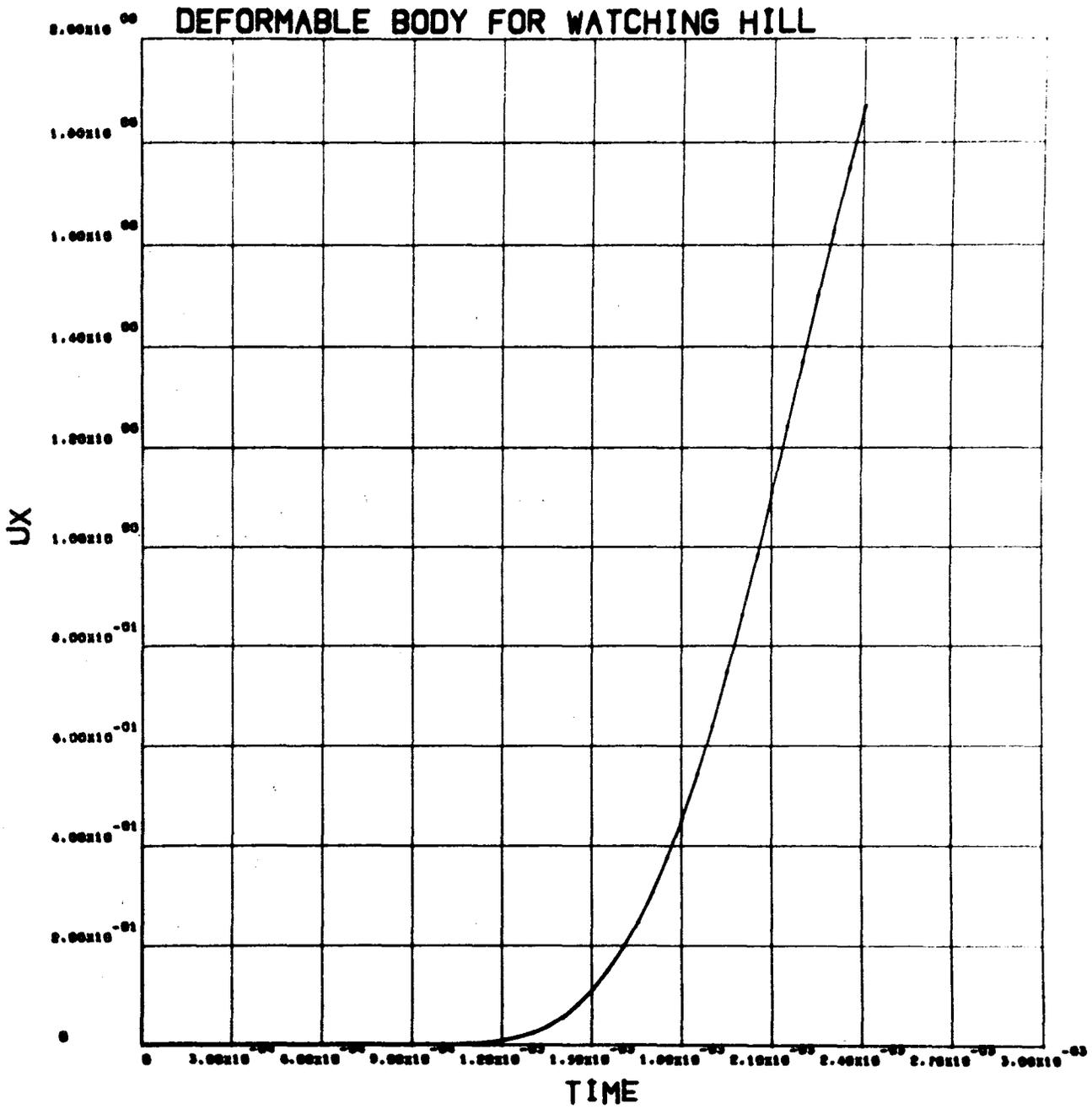


Figure B-83

Radial velocity history (m/s) in soil at range 0.28 m, depth 0.2 m (deformable penetrator).

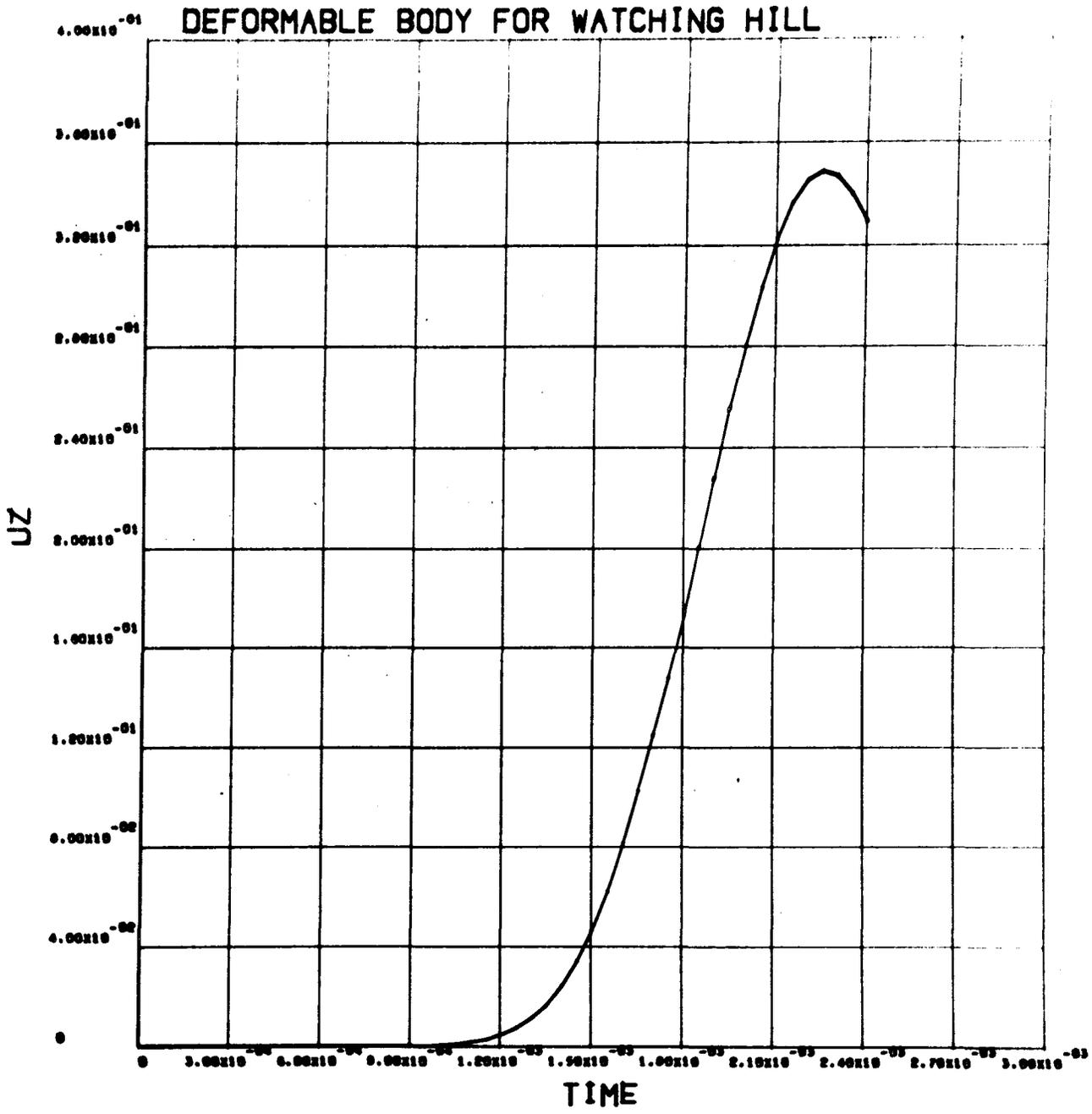


Figure B-84  
 Vertical velocity history (m/s) in soil at range 0.28 m, depth 0.2 m (deformable penetrator).

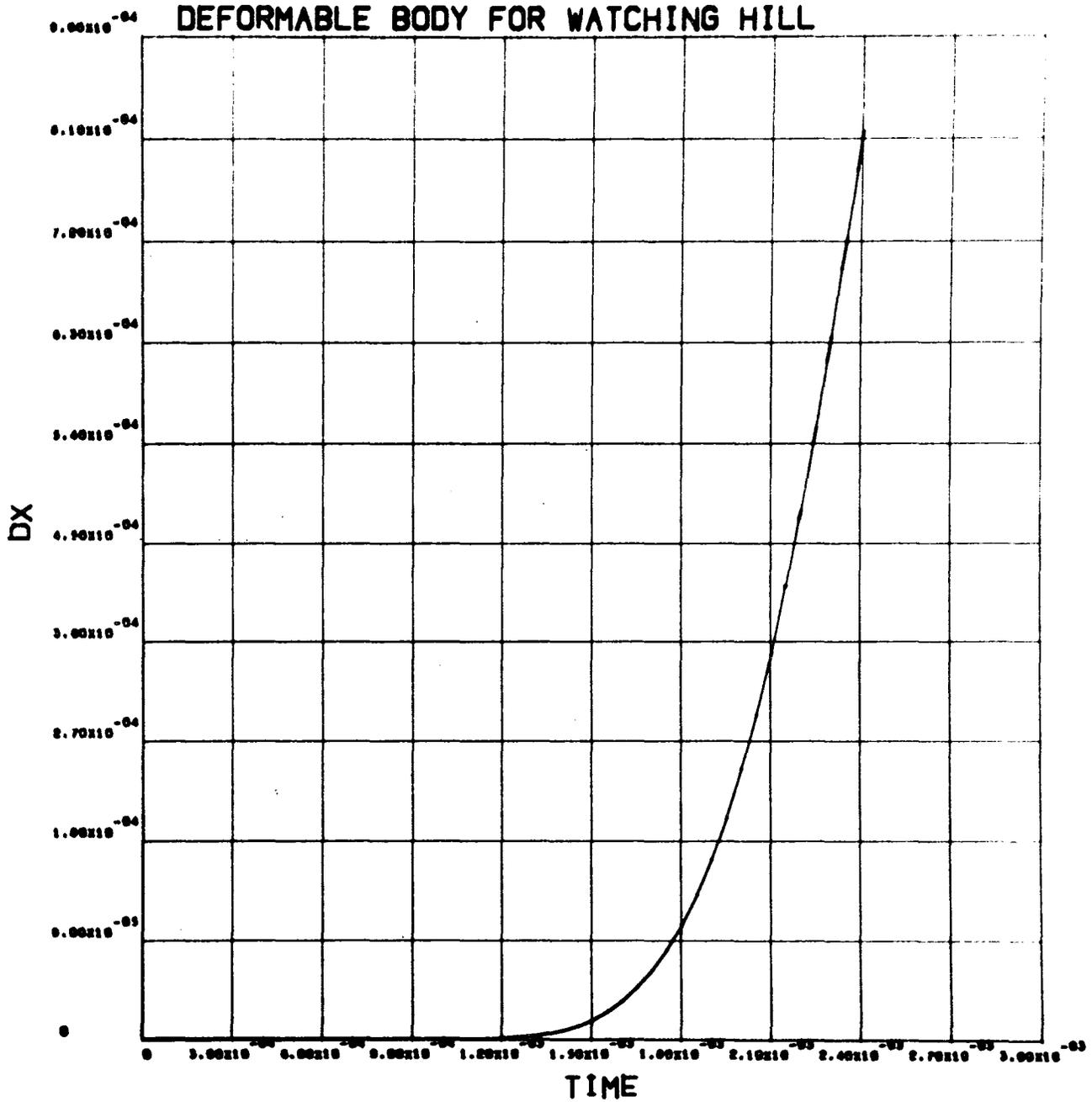


Figure B-85

Radial displacement history (m) in soil at range 0.28 m, depth 0.2 m (deformable penetrator).

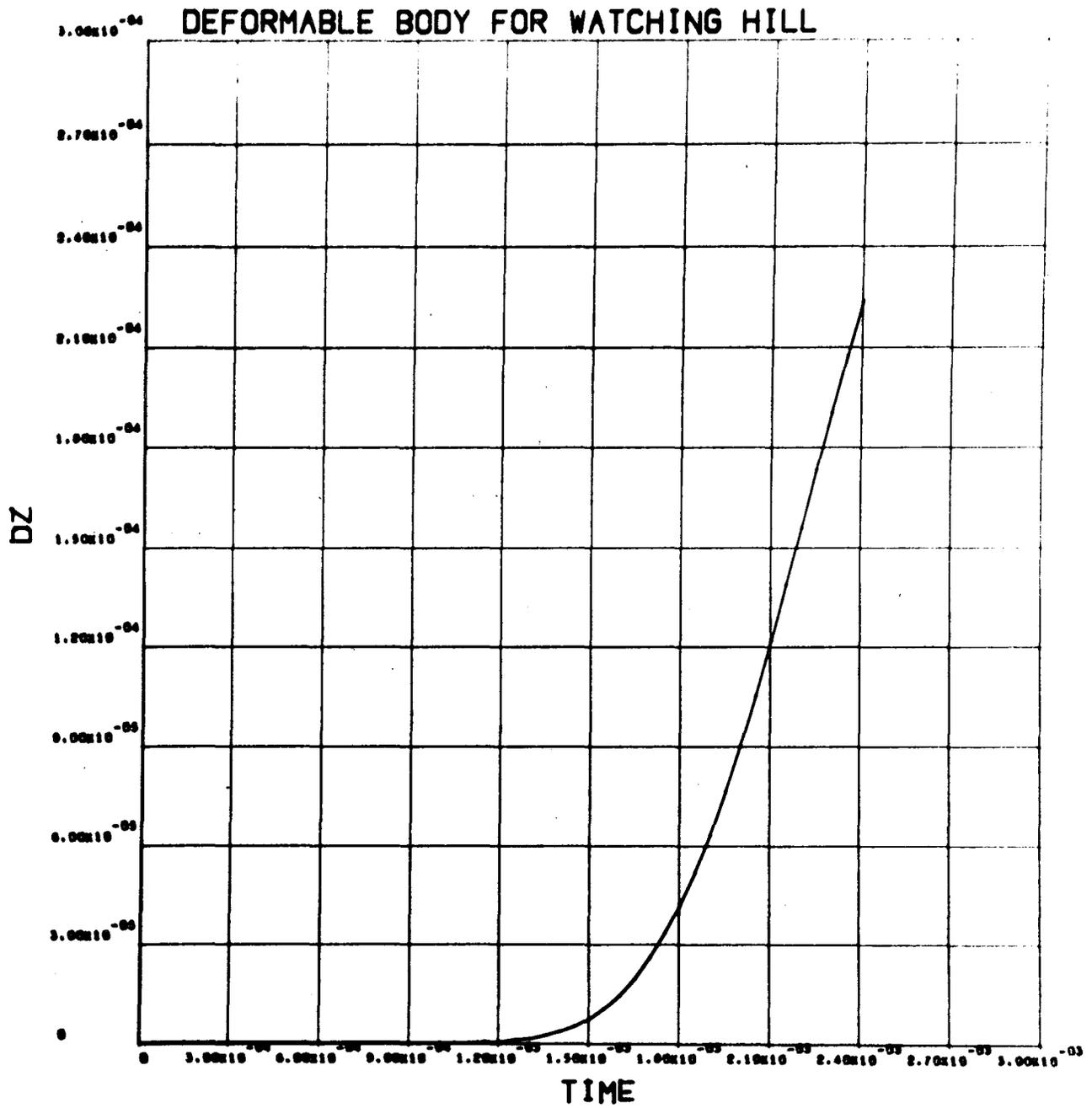


Figure B-86  
 Vertical displacement history (m) in soil at range 0.28 m, depth 0.2 m (deformable penetrator).

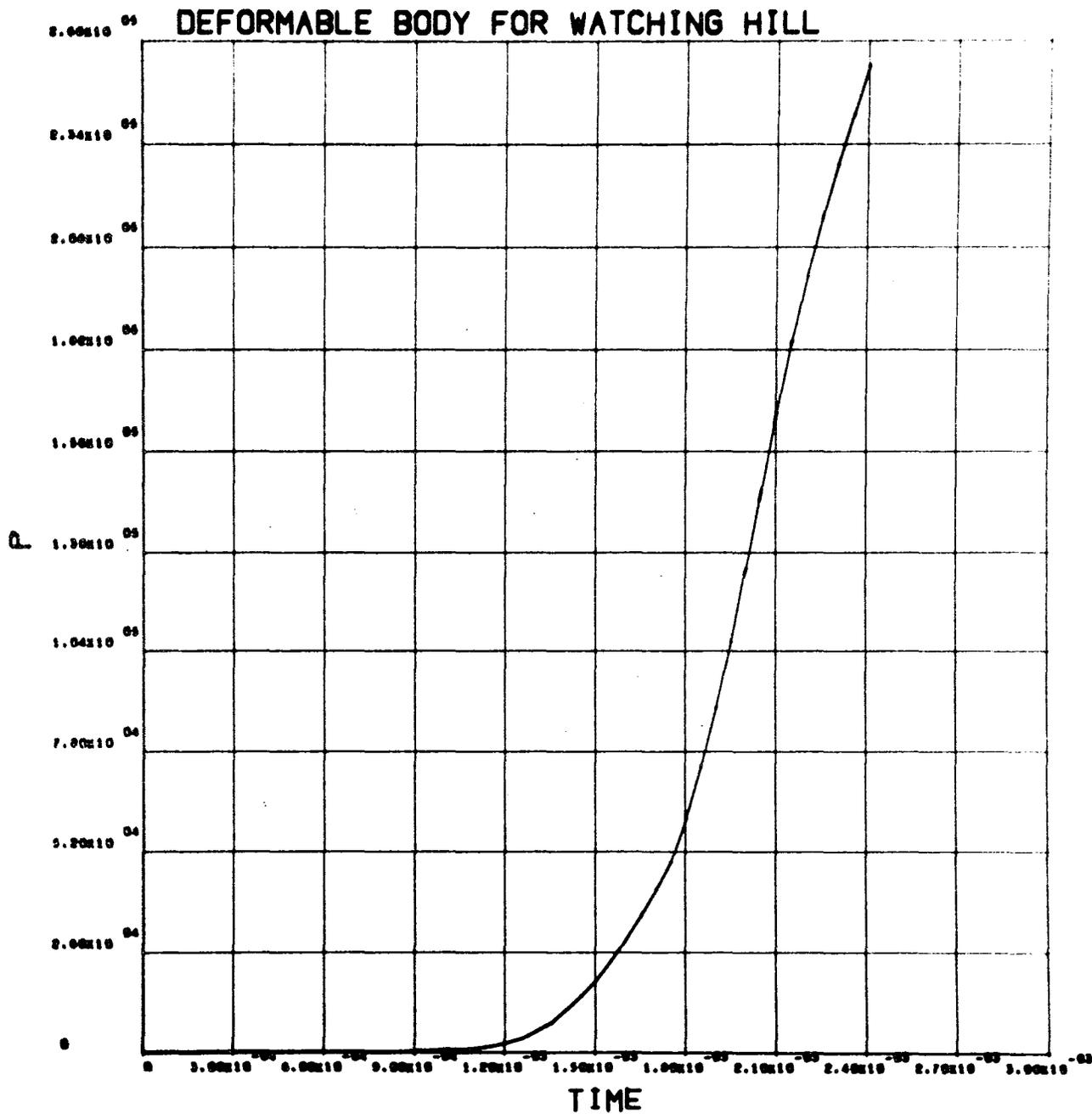


Figure B-87

Pressure history (Pa) in soil at range 0.28 m, depth 0.2 (deformable penetrator).

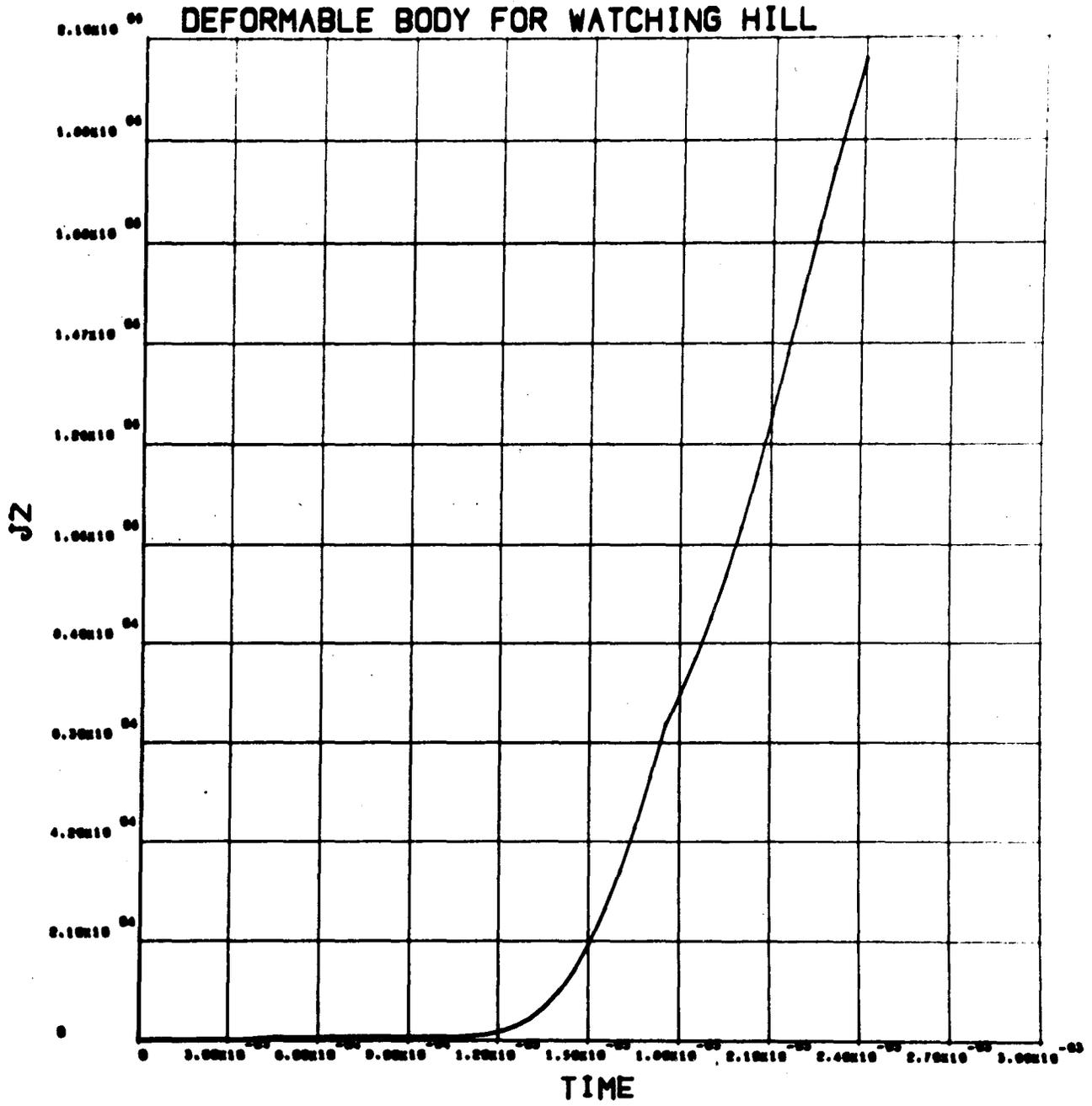


Figure B-88  
 Deviator stress, J2, history (Pa) in soil at range 0.28 m, depth 0.2 m (deformable penetrator).

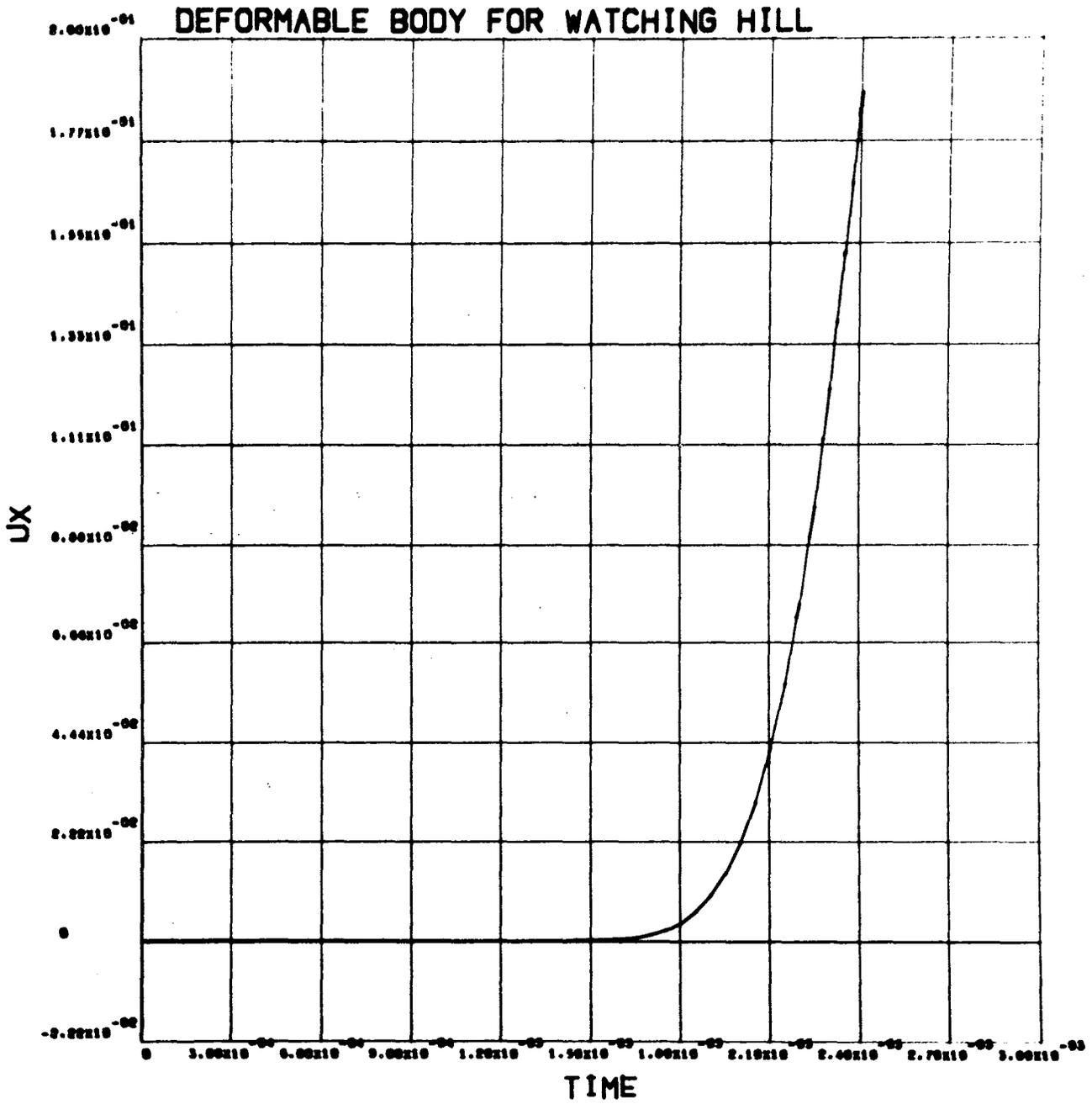


Figure B-89

Radial velocity history (m/s) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

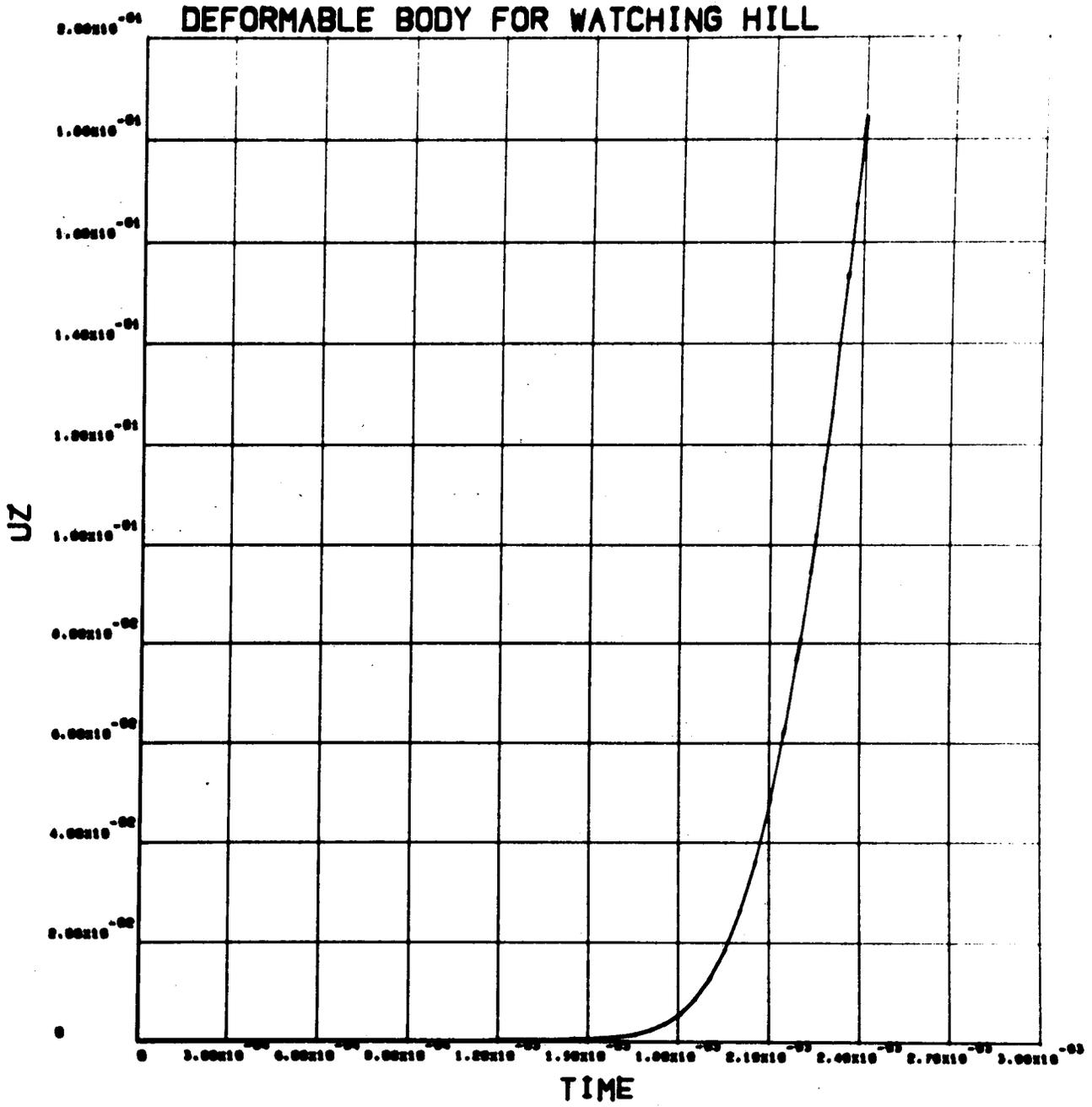


Figure B-90  
 Vertical velocity history (m/s) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

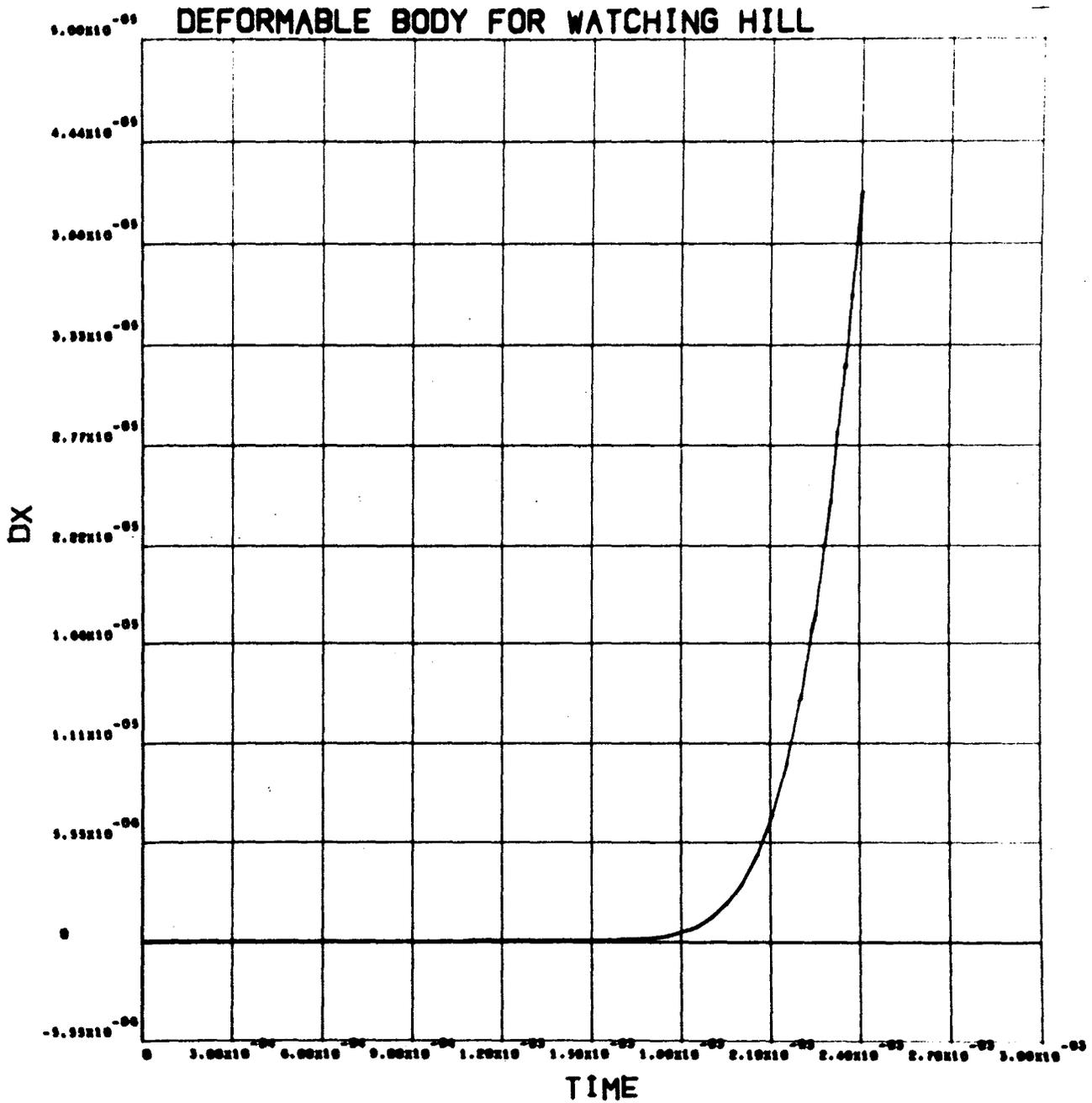


Figure B-91

Radial displacement history (m) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

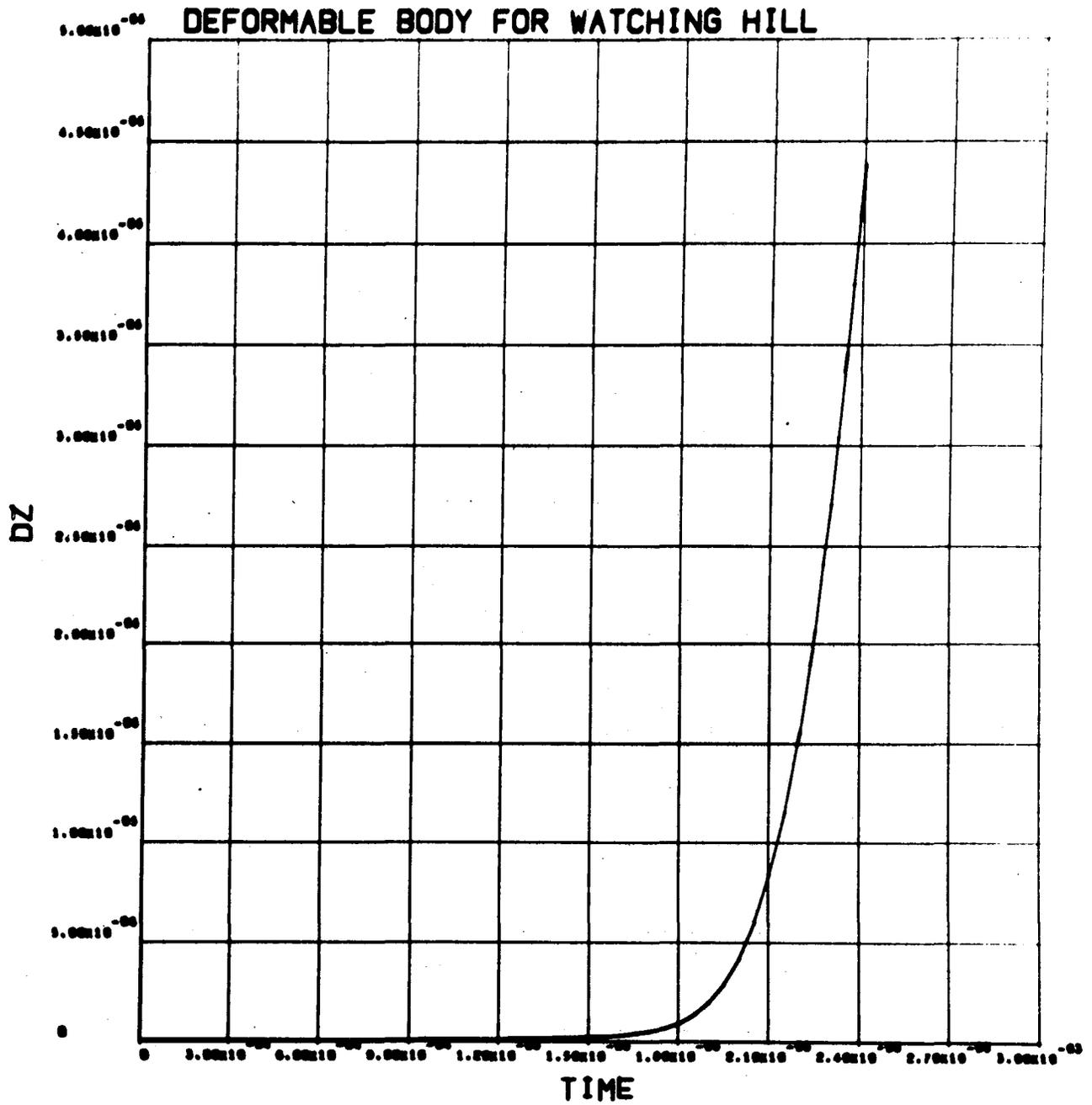


Figure B-92

Vertical displacement history (m) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

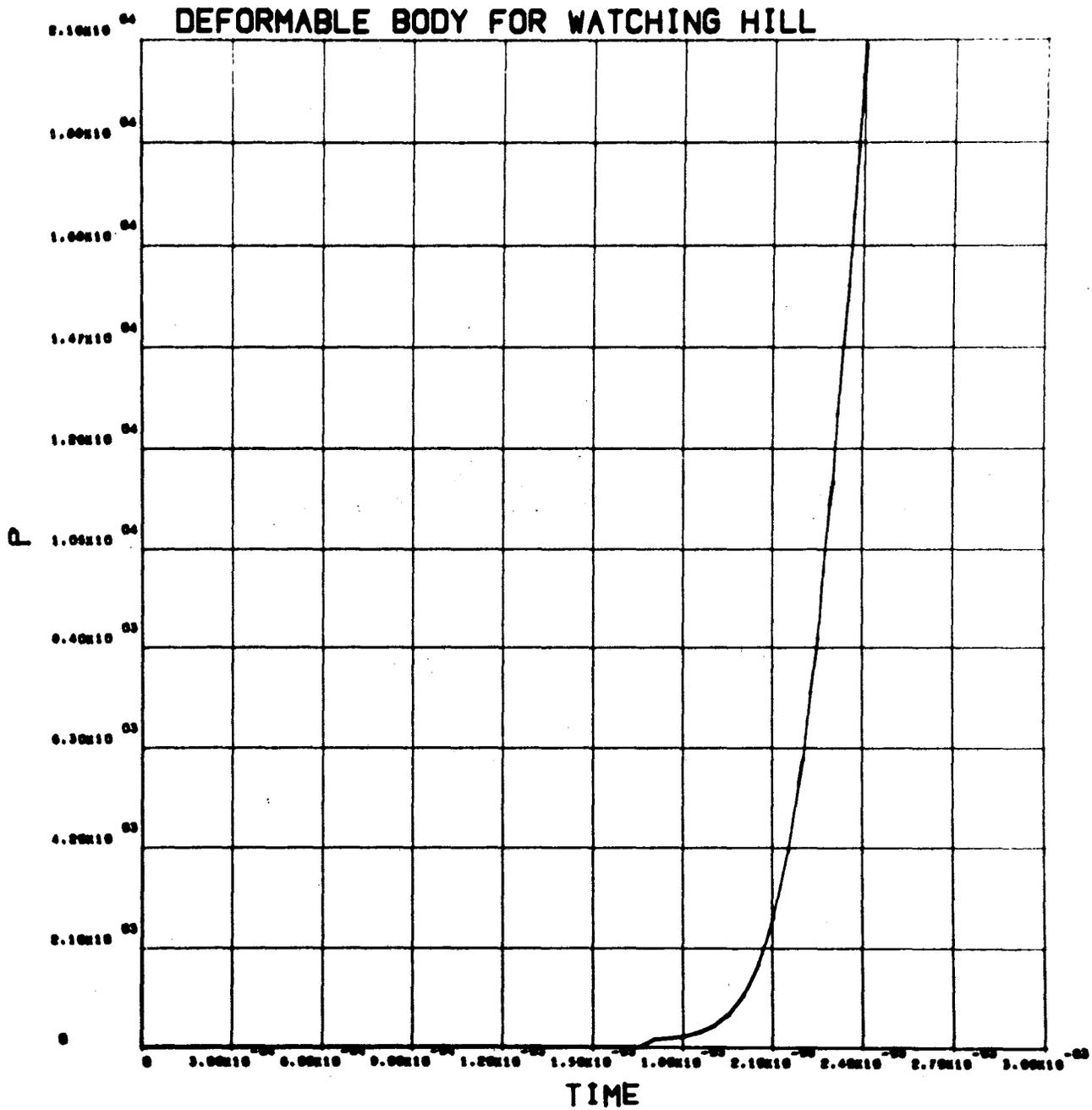


Figure B-93

Pressure history (Pa) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

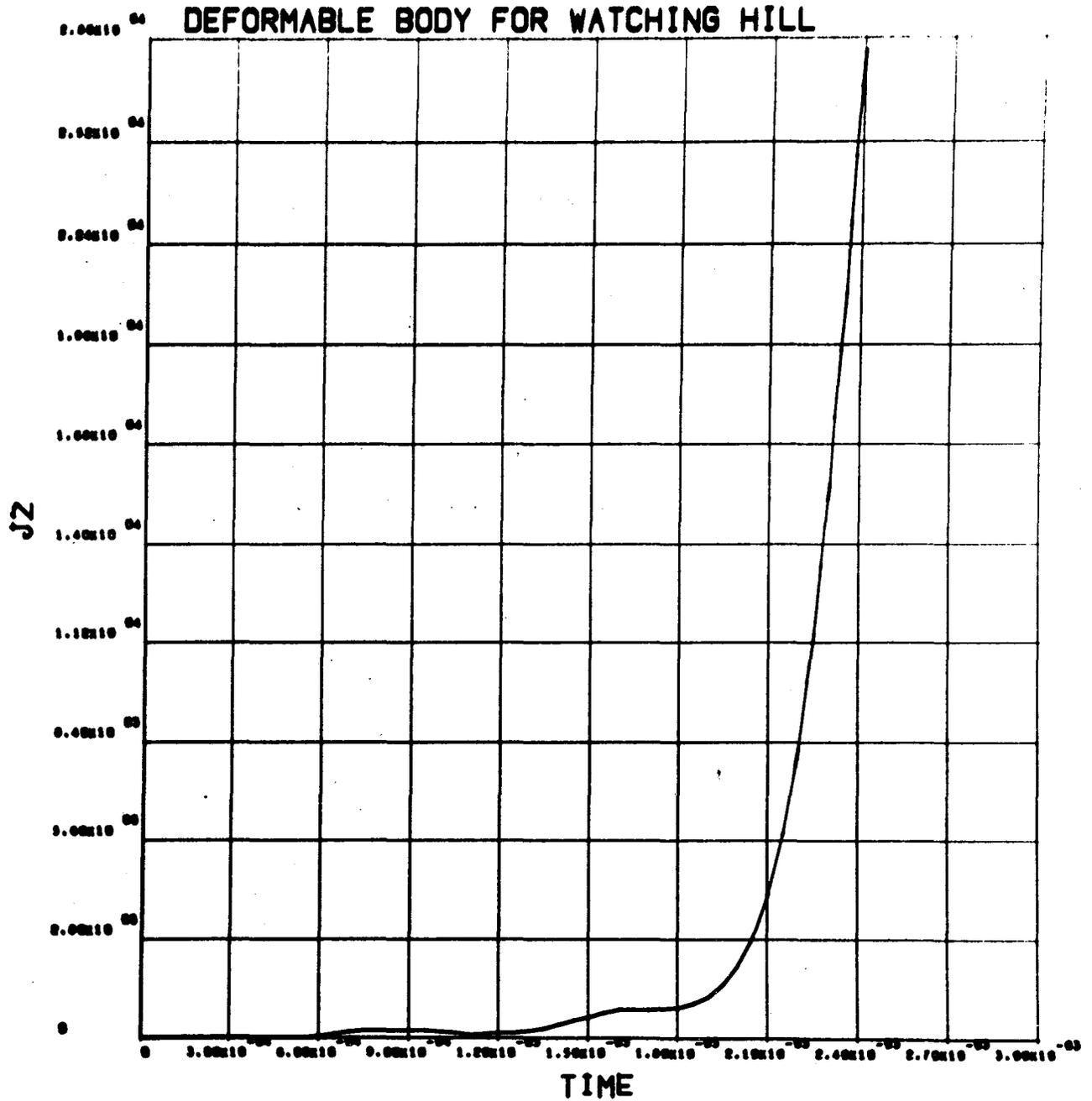


Figure B-94  
 Deviator stress, J2, history (Pa) in soil at range 0.28 m, depth 0.4 m (deformable penetrator).

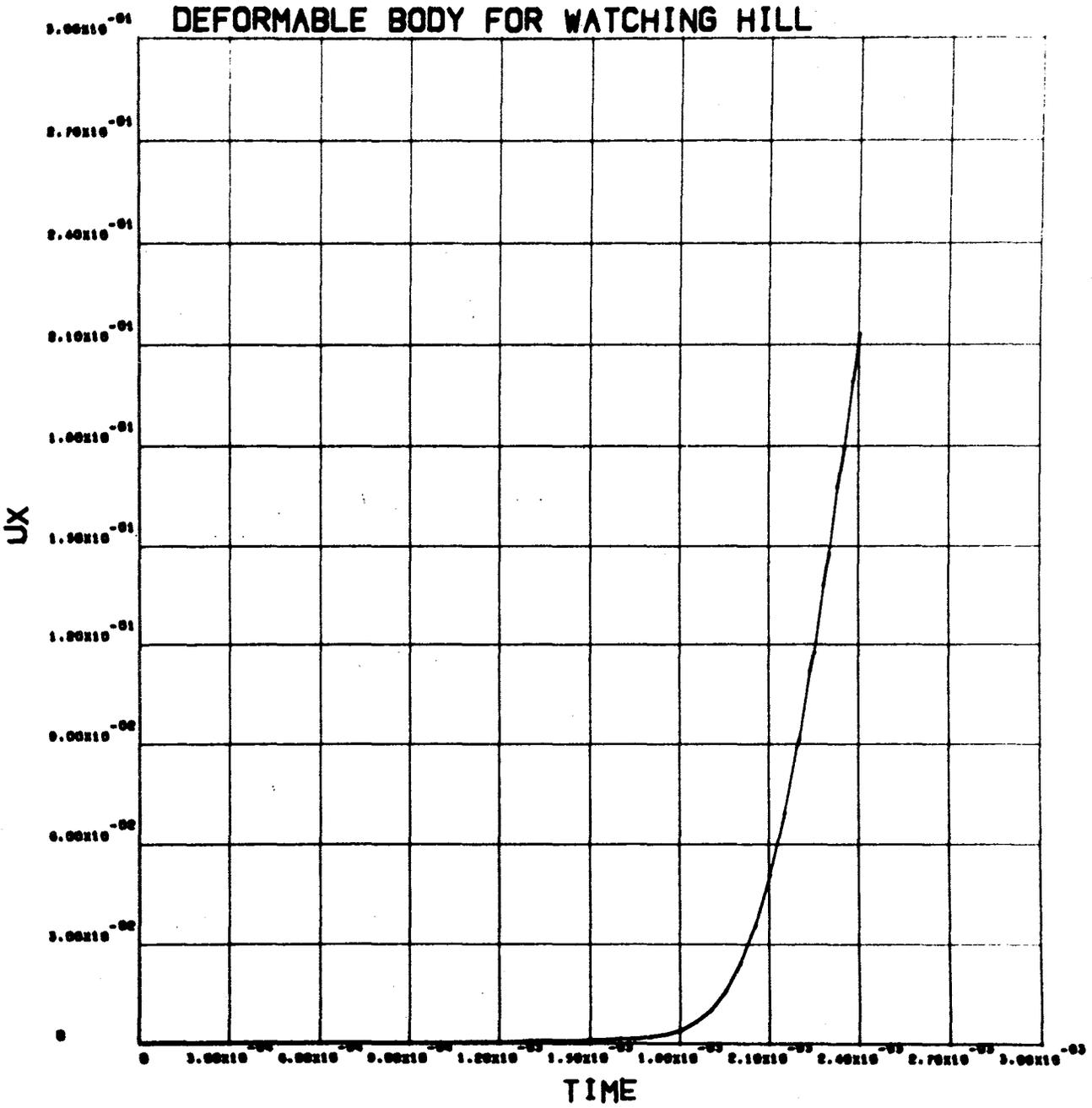


Figure B-95

Radial velocity history (m/s) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

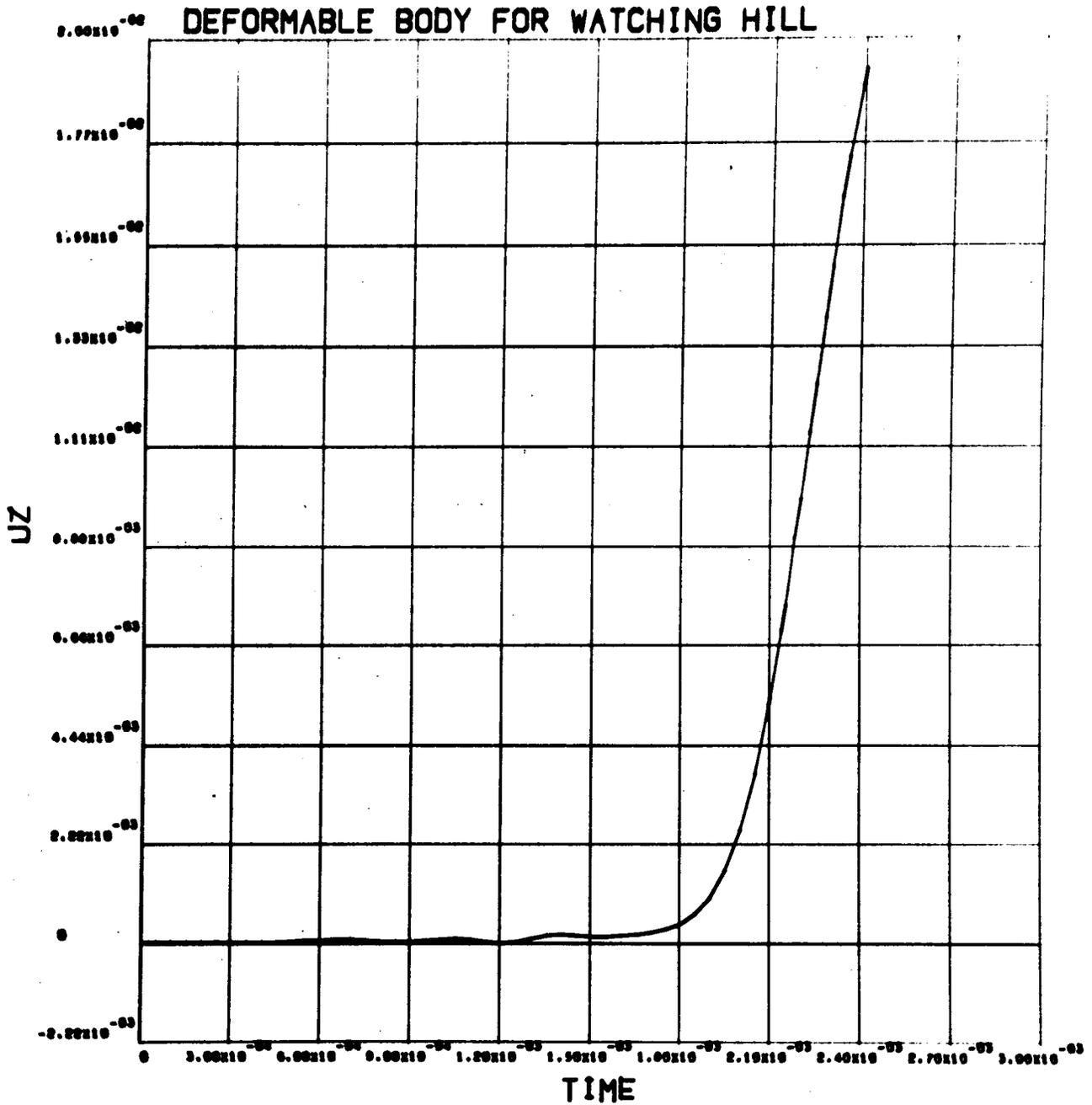


Figure B-96  
 Vertical velocity history (m/s) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

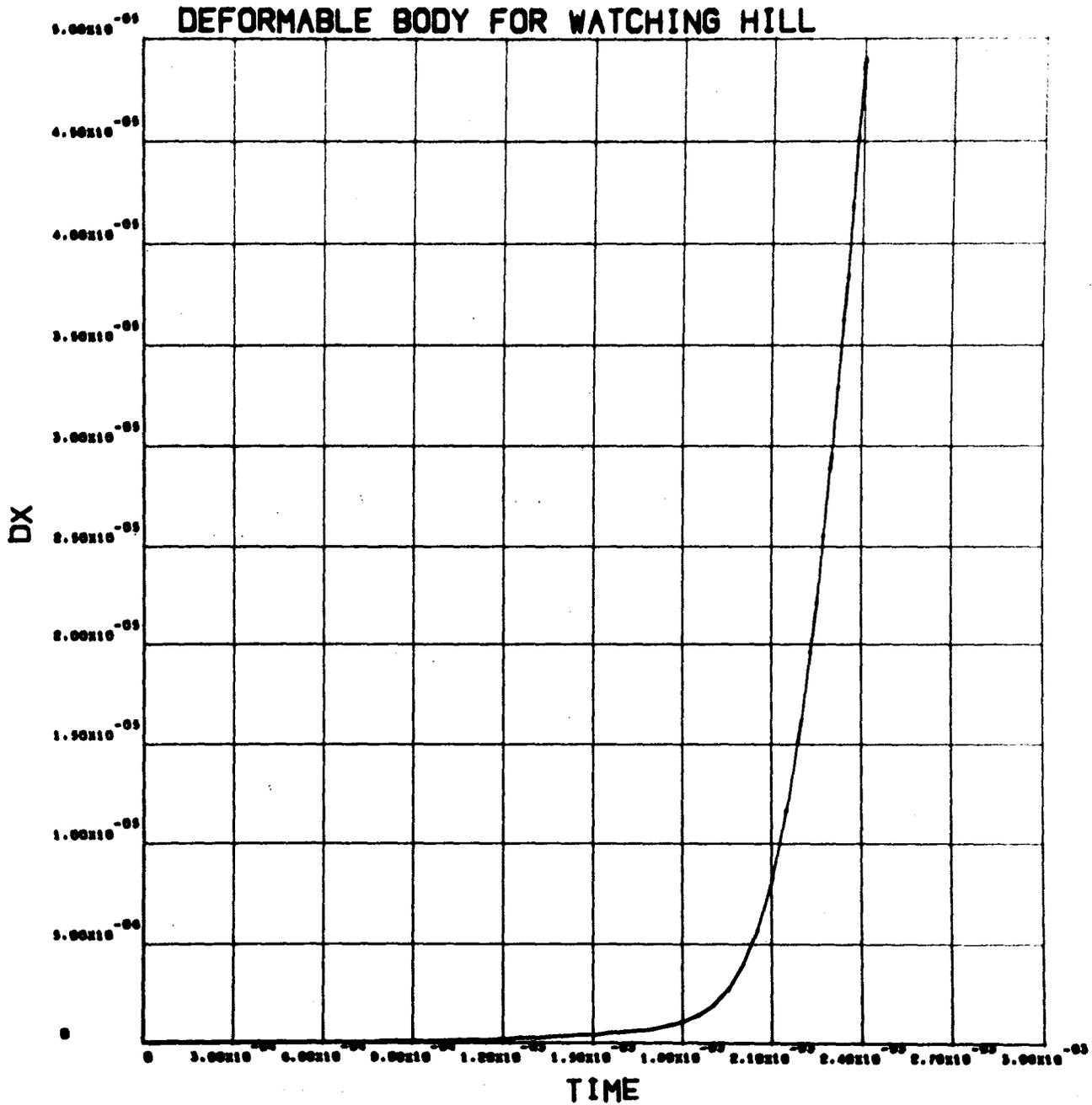


Figure B-97

Radial displacement history (m) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

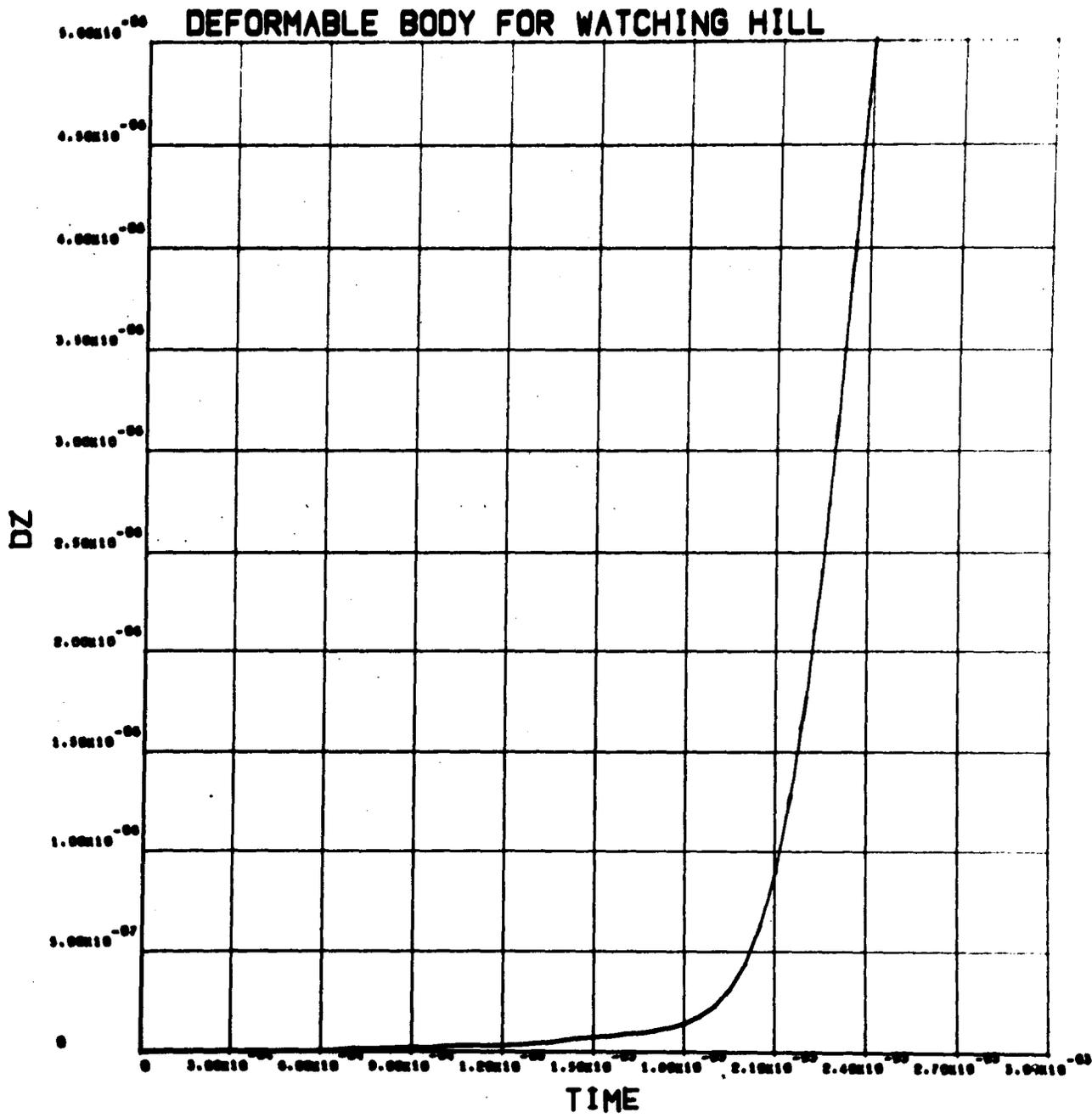


Figure B-98  
 Vertical displacement history (m) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

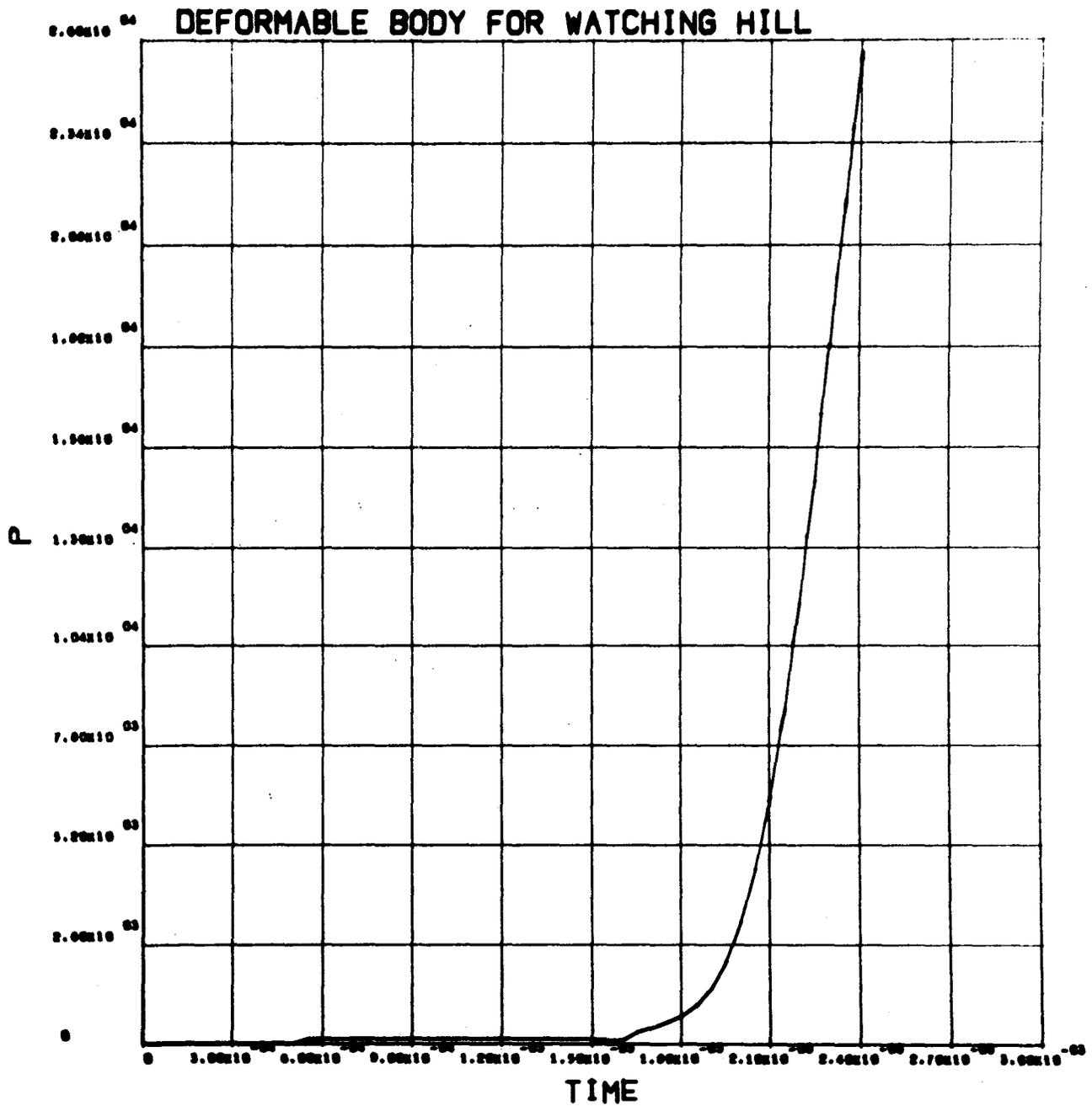


Figure B-99

Pressure history (Pa) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

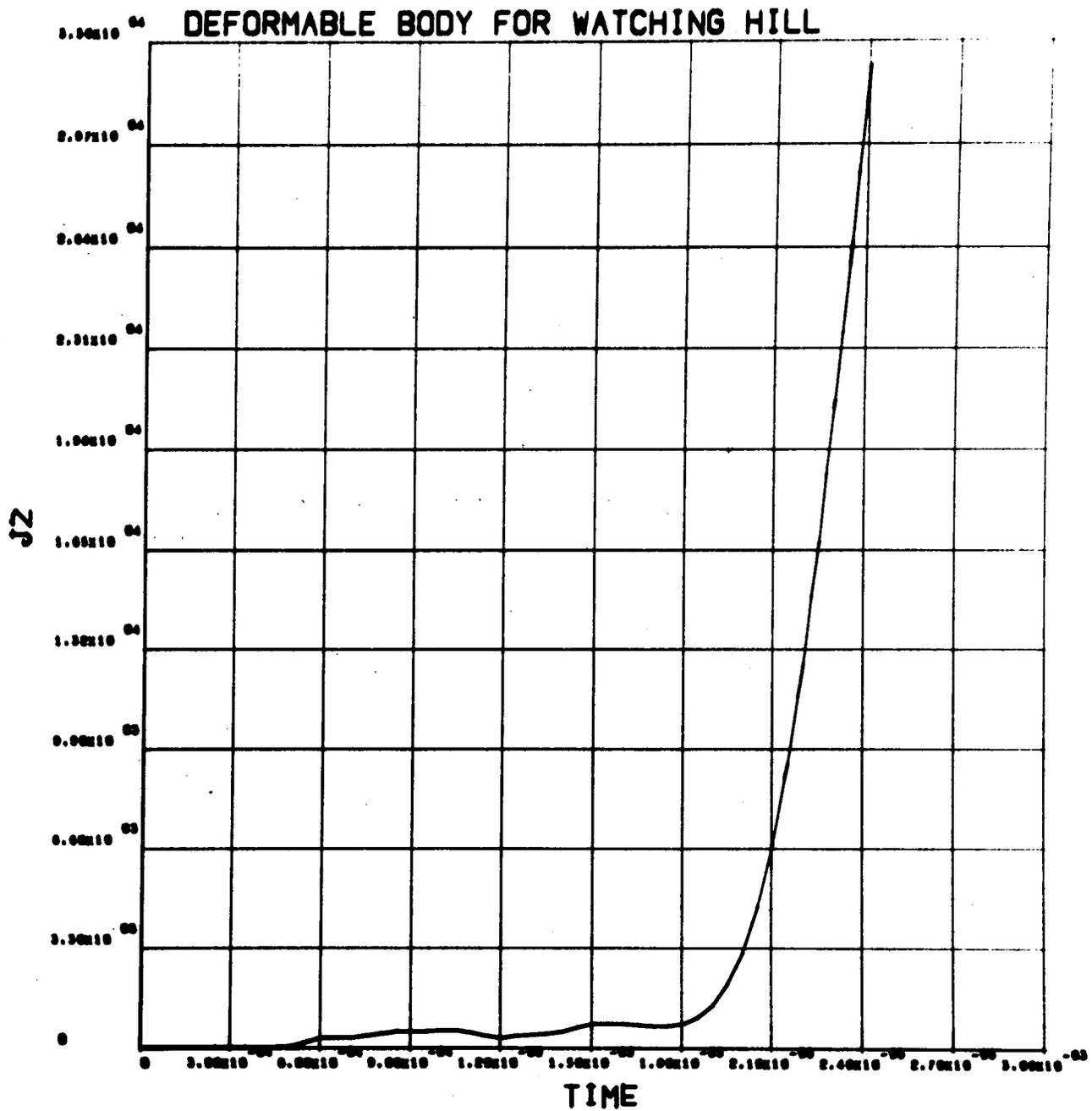


Figure B-100  
 Deviator stress, J2, history (Pa) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

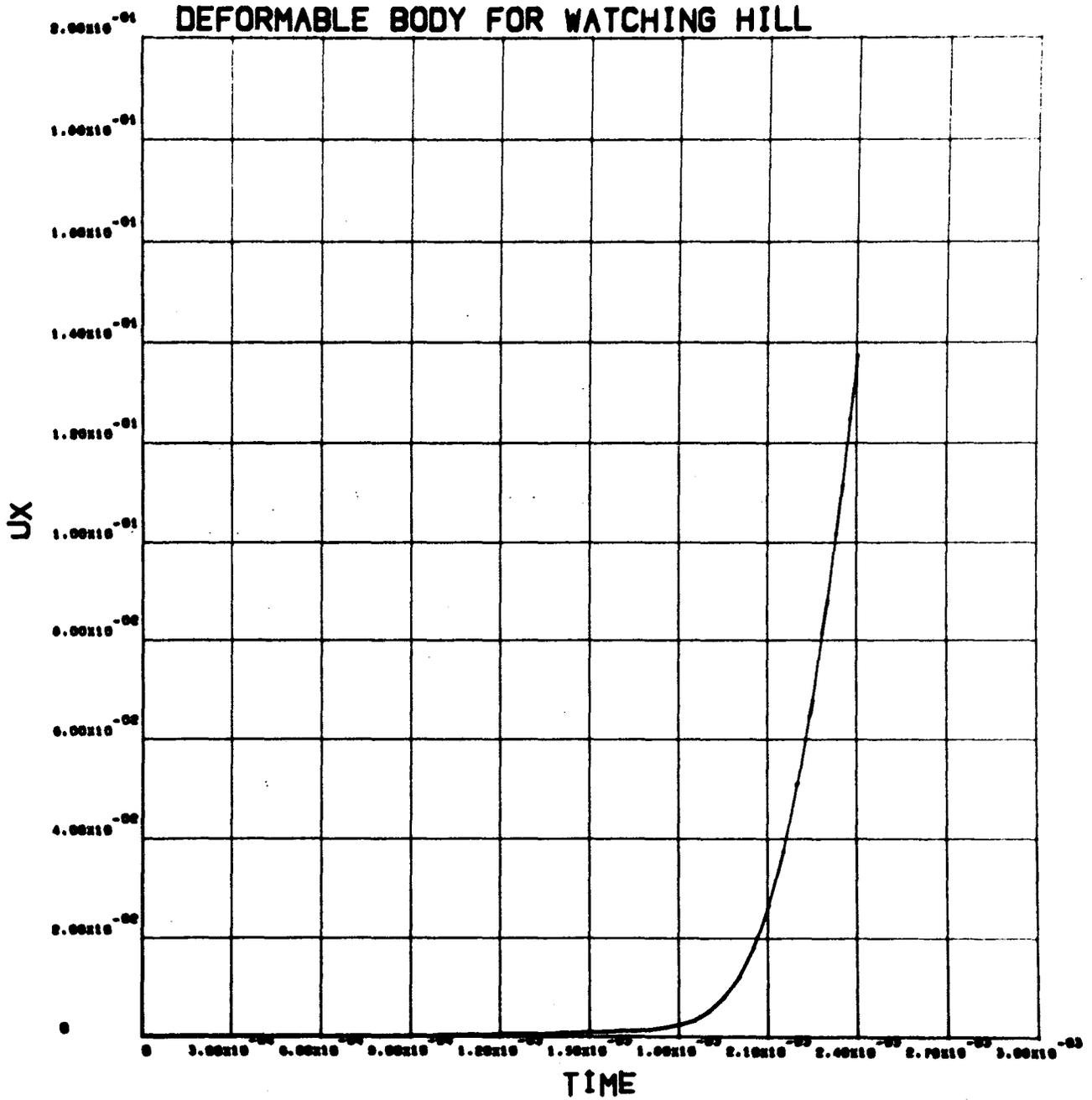


Figure B-101

Radial velocity history (m/s) in soil at range 0.44 m, depth 0.2 m (deformable penetrator).

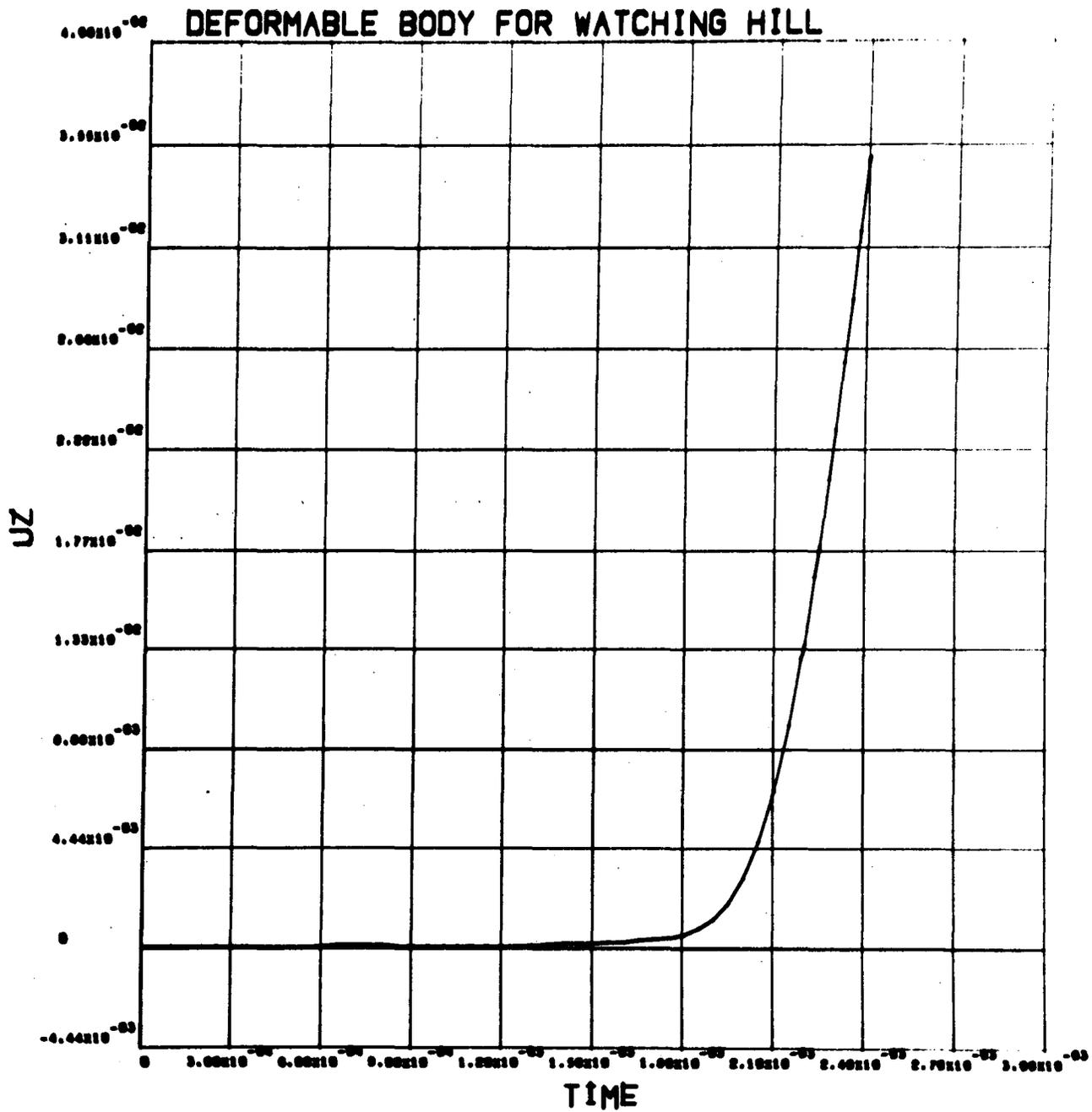


Figure B-102

Vertical velocity history (m/s) in soil at range 0.44 m, depth 0.2 m (deformable penetrator).

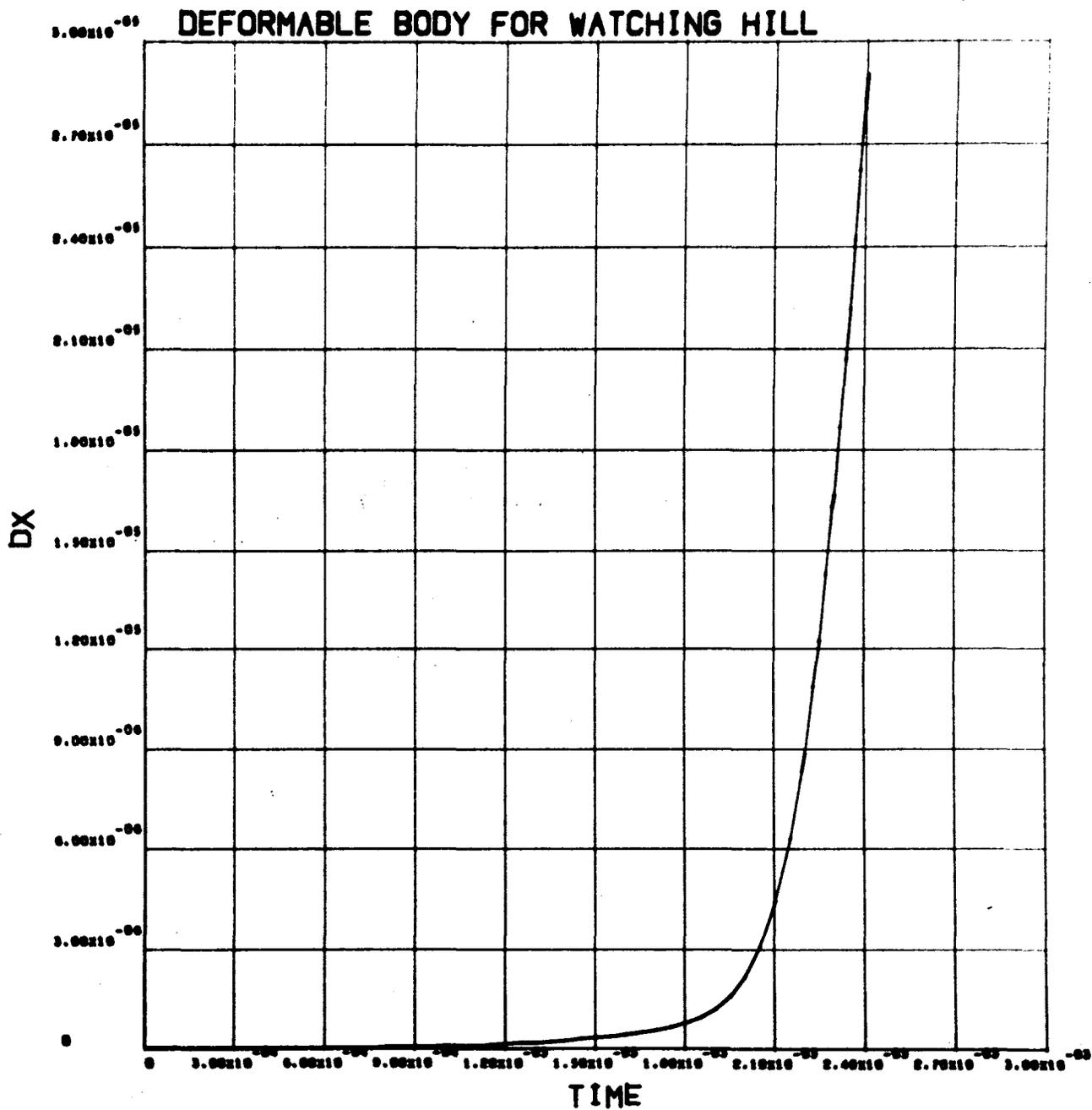


Figure B-103

Radial displacement history (m) in soil at range 0.44 m, depth 0.2 m (deformable penetrator).

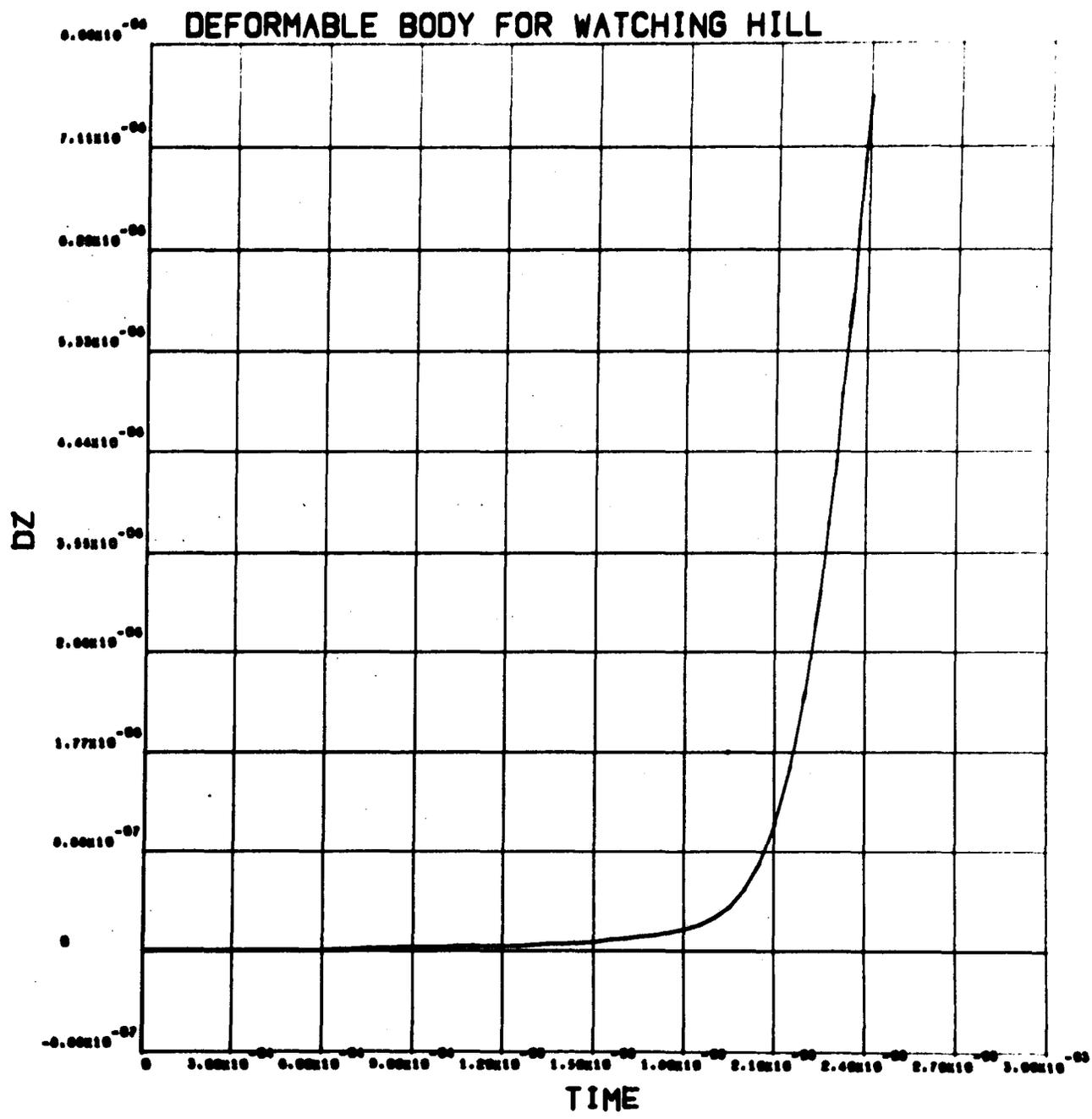


Figure B-104  
 Vertical displacement history (m) in soil at range 0.44 m, depth 0.2 m (deformable penetrator).

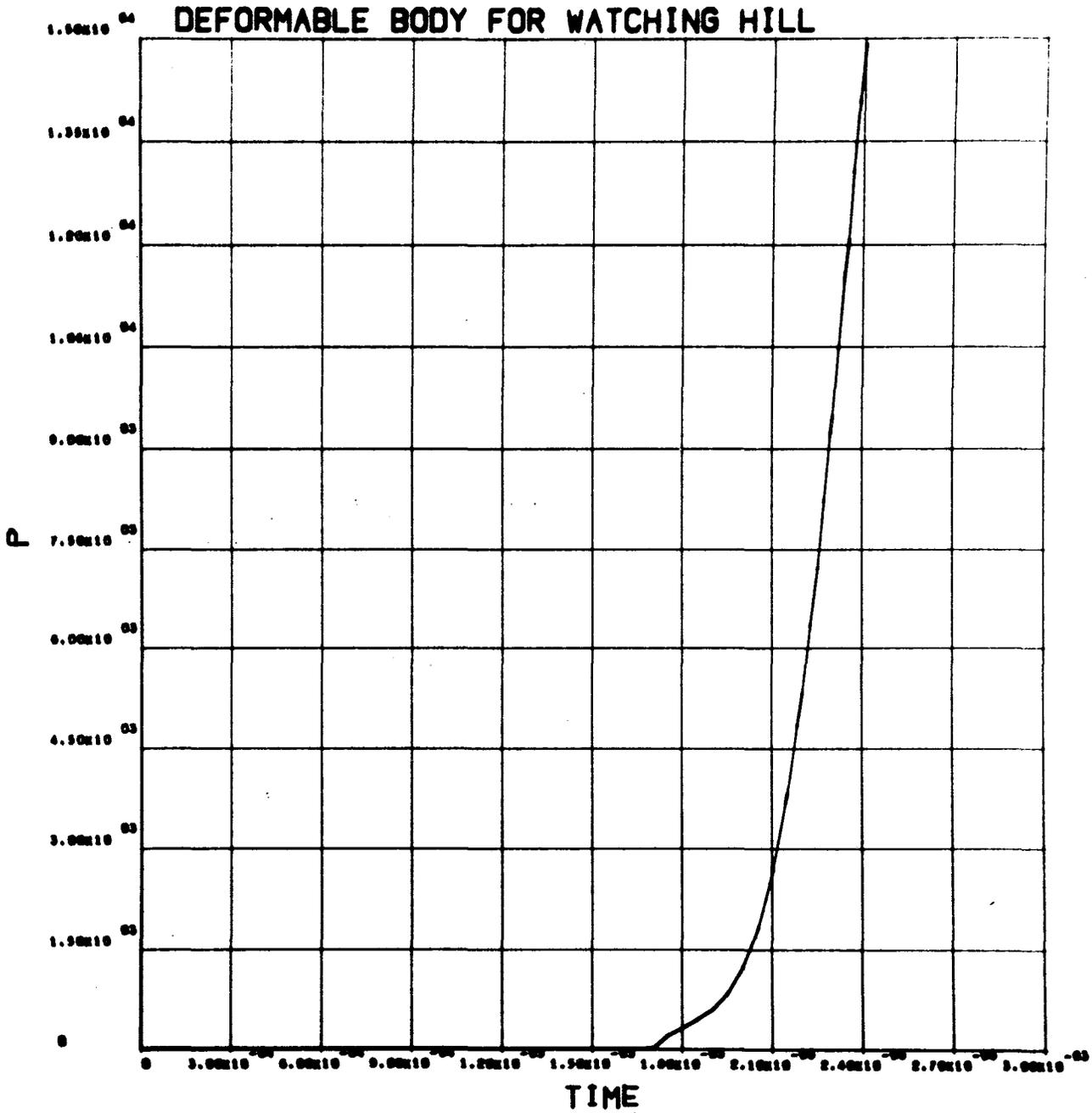


Figure B-105

Pressure history (Pa) in soil at range 0.44 m, depth 0.2 m (deformable penetrator).

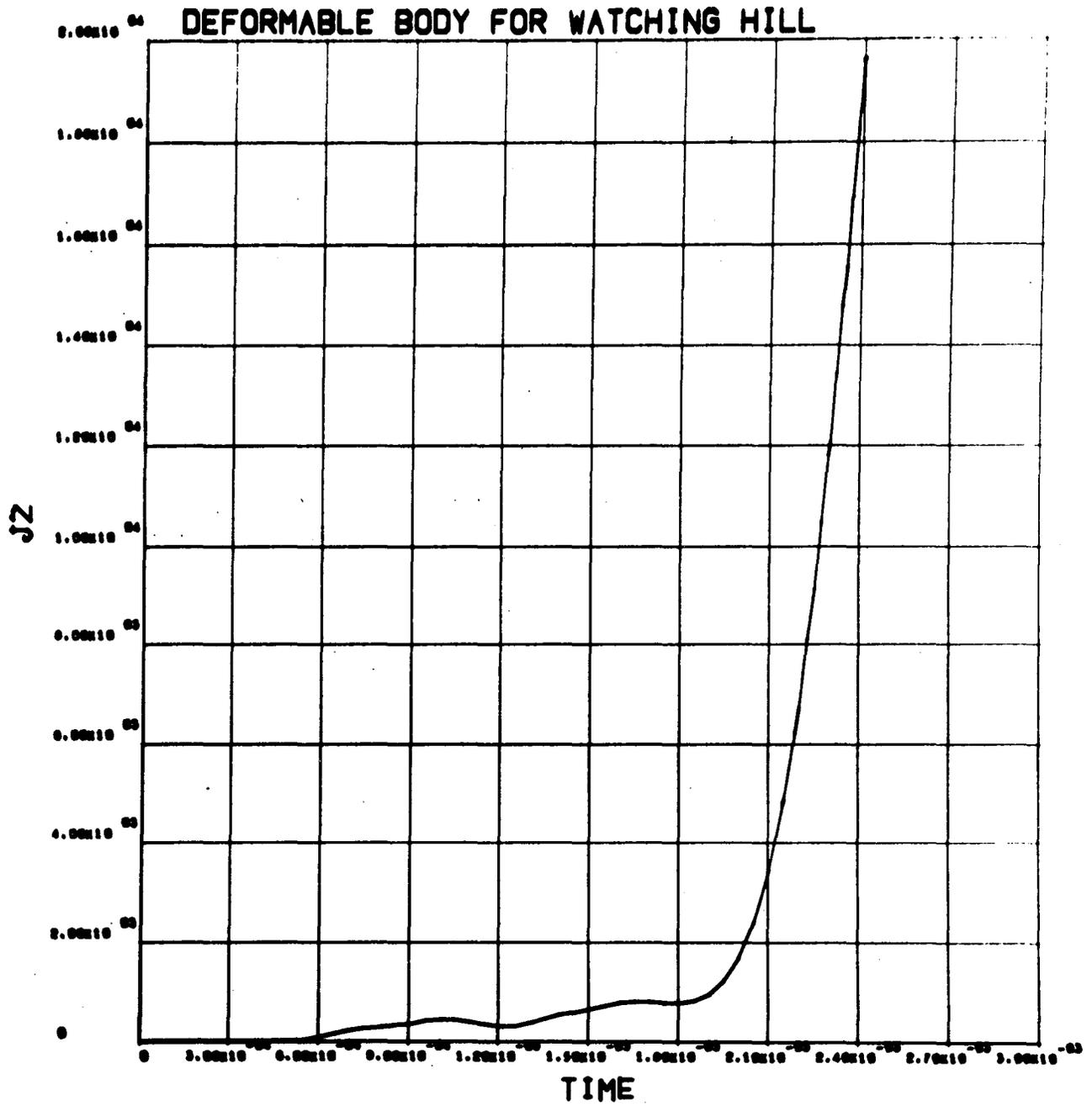


Figure B-106  
 Deviator stress,  $J_2$ , history (Pa) in soil at range 0.44 m, depth 0.1 m (deformable penetrator).

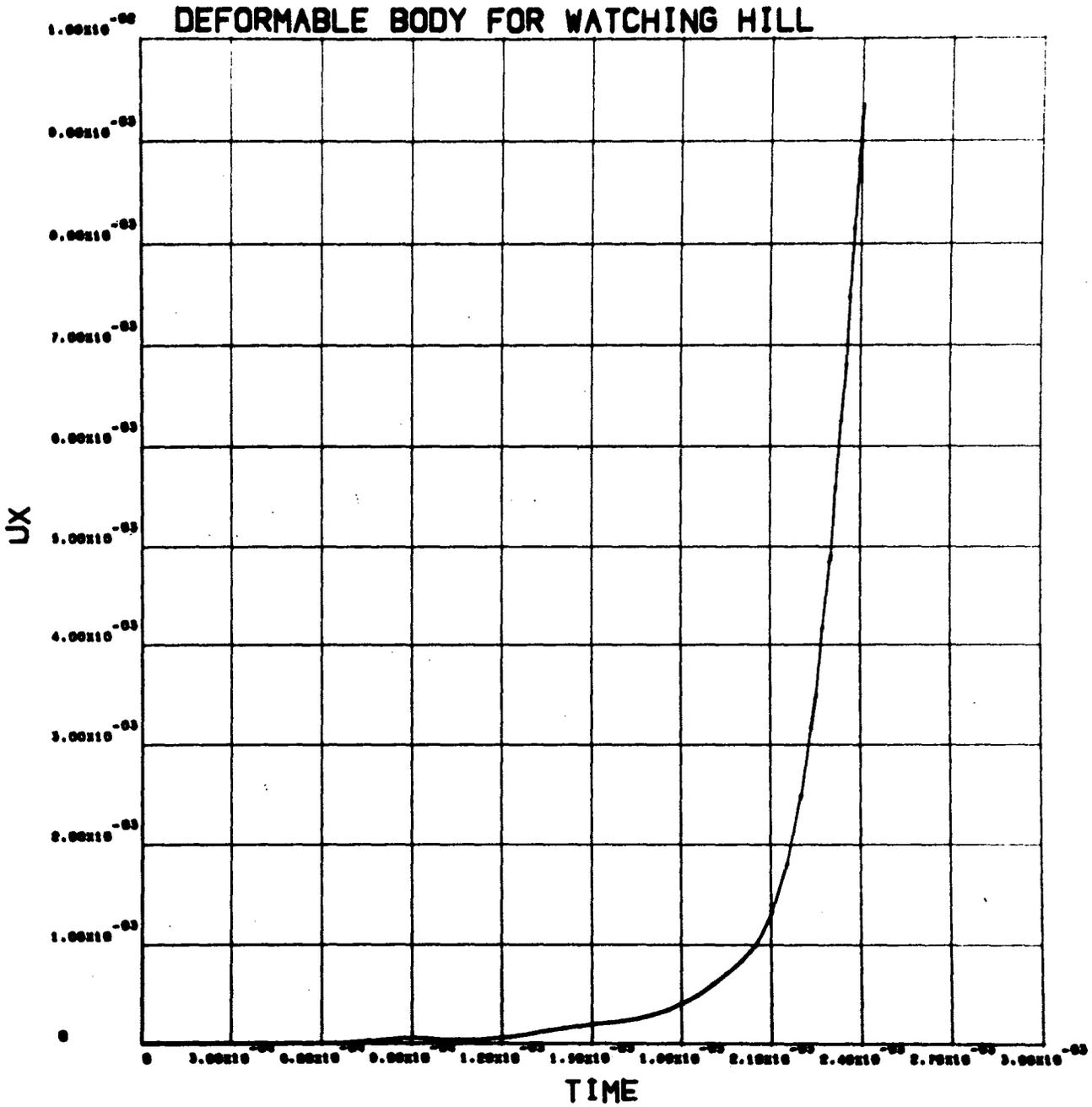


Figure B-107

Radial velocity history (m/s) in soil at range 0.44 m, depth 0.4 m (deformable penetrator).

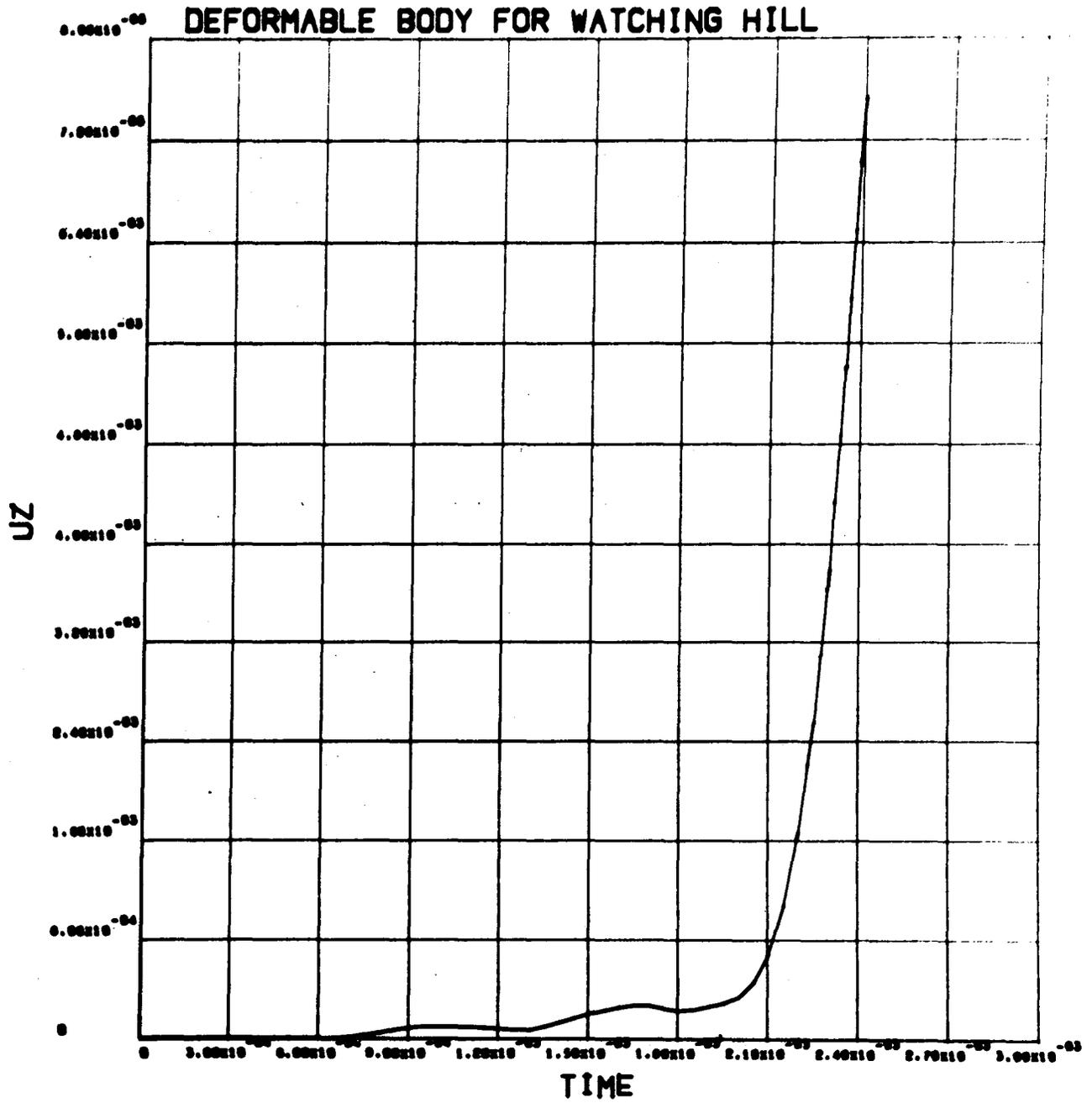


Figure B-108  
 Vertical velocity history (m/s) in soil at range 0.44 m, depth 0.4 m (deformable penetrator).

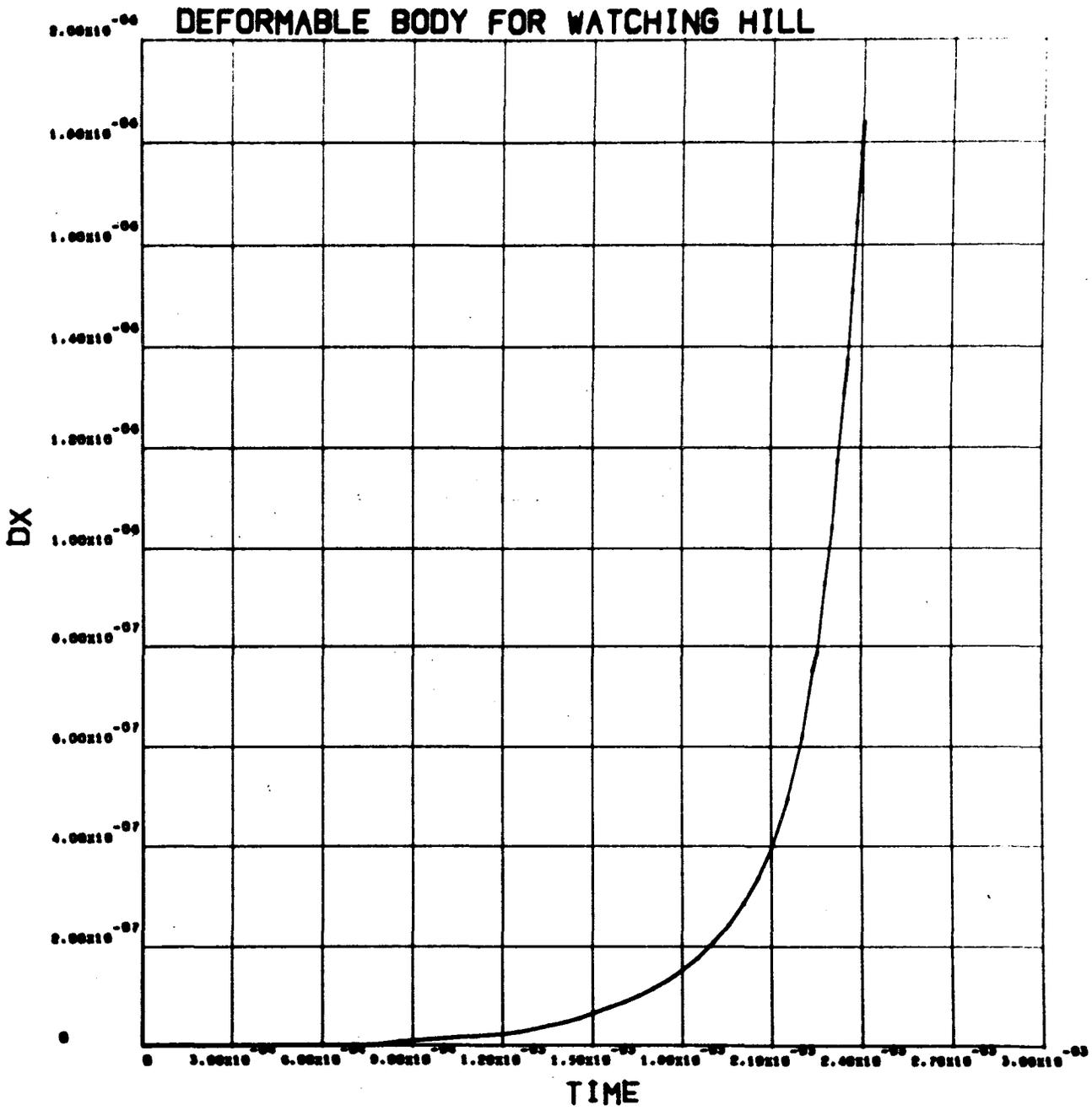


Figure B-109

Radial displacement history (m) in soil at range 0.44 m, depth 0.4 m (deformable)

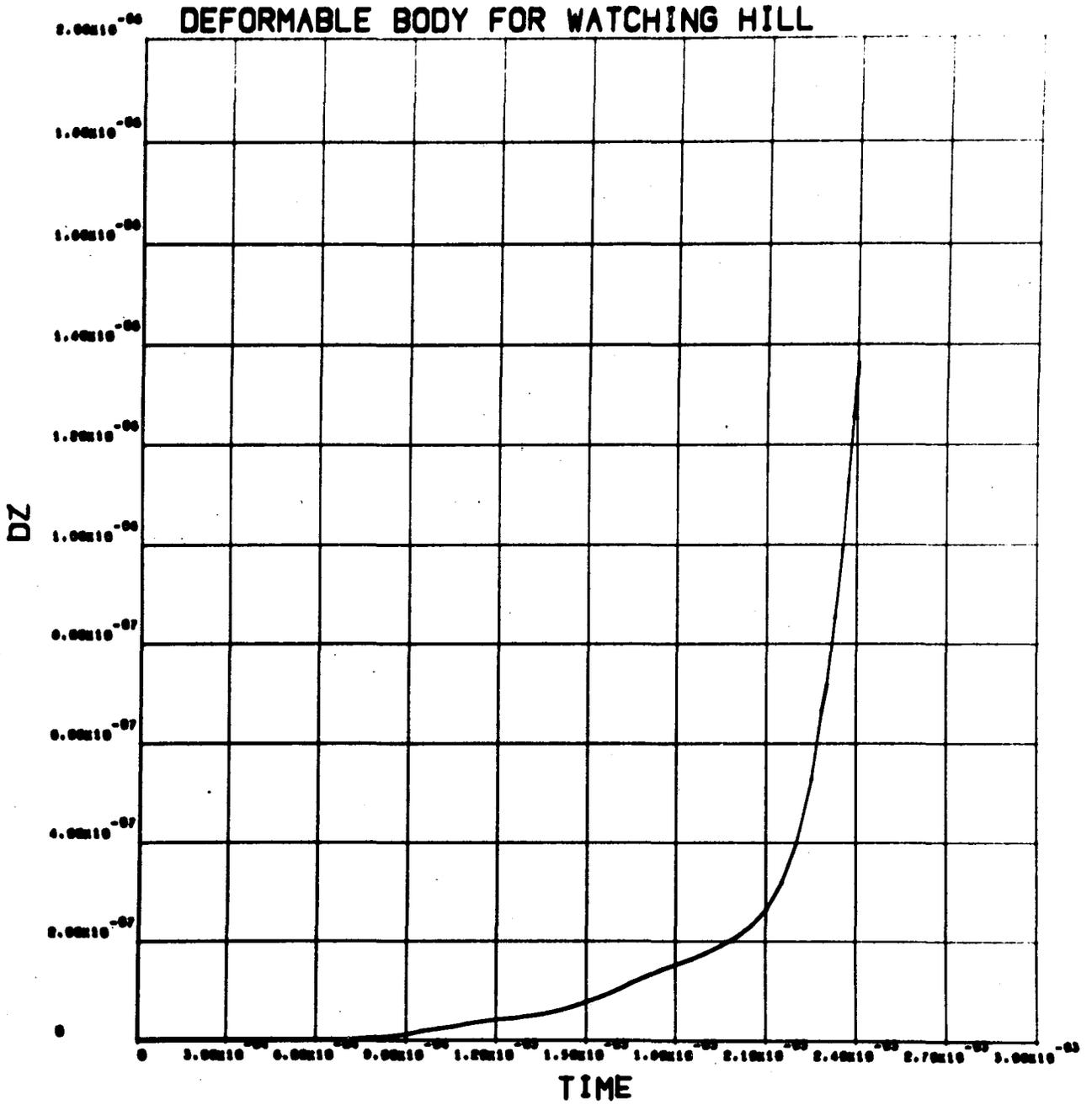


Figure B-110  
 Vertical displacement history (m) in soil at range 0.44 m, depth 0.4 m (deformable penetrator).

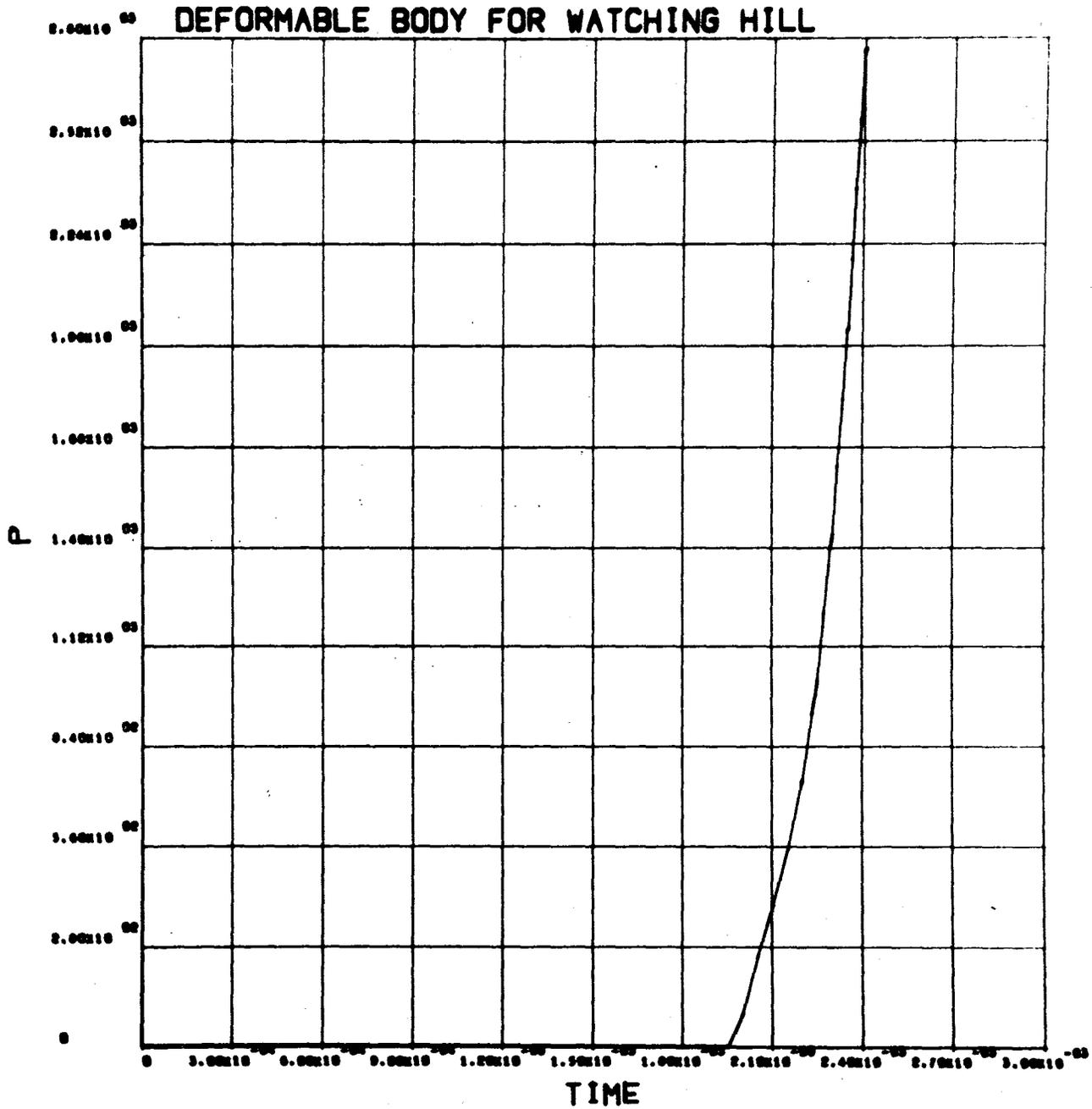


Figure B-111

Pressure history (Pa) in soil at range 0.44 m, depth 0.4 m (deformable penetrator).

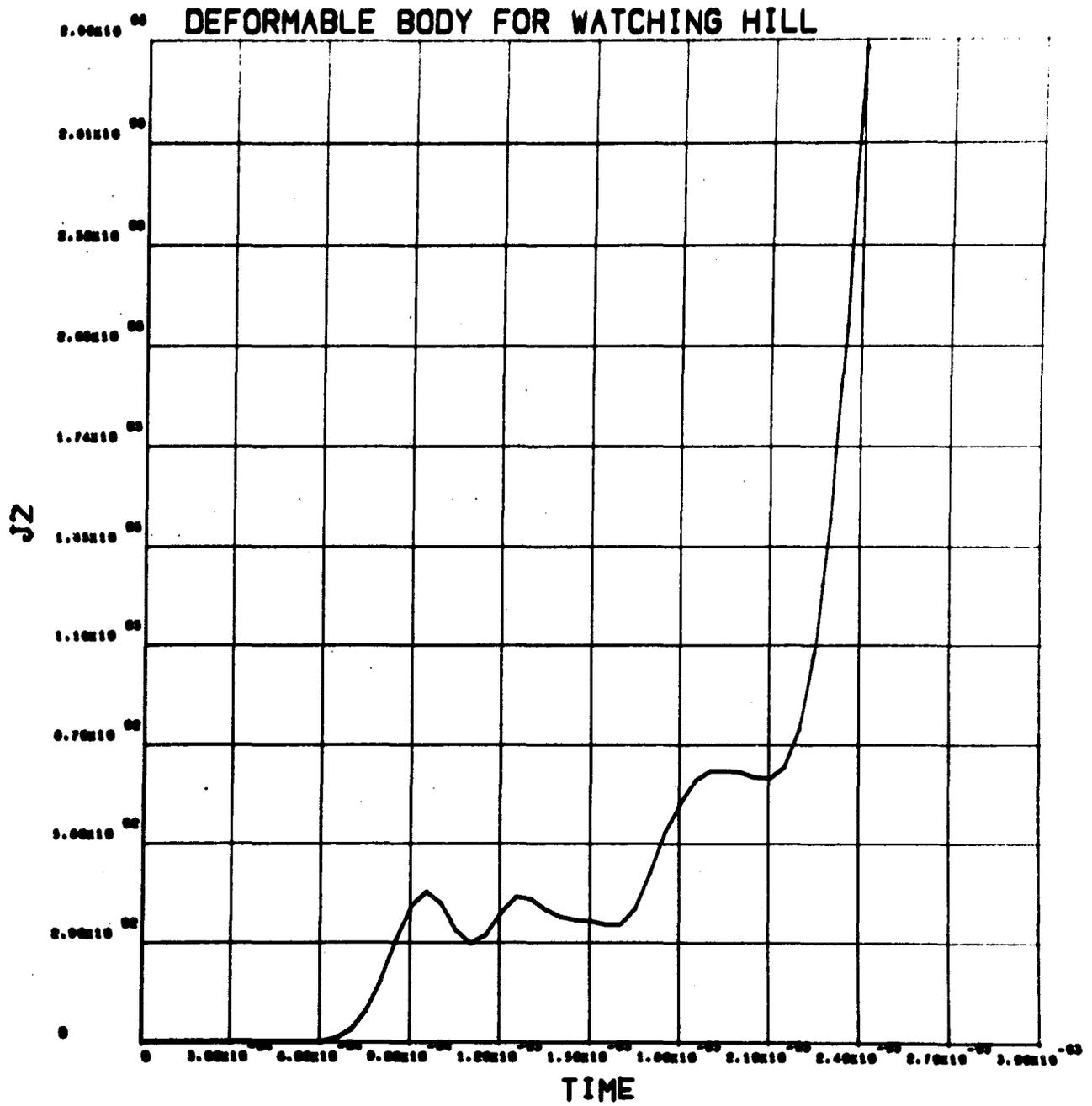


Figure B-112

Deviator stress,  $J_2$ , history (Pa) in soil at range 0.44 m, depth 0.4 m (deformable penetrator), (octahedral shear stress =  $\sqrt{2/3} (J_2)$ ).

Unlimited Release

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1563 D. L. McCoy  
1700 O. E. Jones  
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5160 W. Herrmann  
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